



Aerospace  
Systems Division

ALSEP A2/SP-3 Structural  
Dynamics Analysis

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ATM 918	
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This ATM presents the results of the structural dynamics analysis performed for the A2/SP-3 structural arrangement.

Section I describes the dynamics portion, and Section II presents the stress analysis.

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Section II. Stress Analysis

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Prepared by:

K. Wadleigh  
K. Wadleigh

H. Wiger  
H. Wiger

Approved by:

J. Mazzatorta  
J. Mazzatorta



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## SECTION I DYNAMICS ANALYSIS

### 1.0 INTRODUCTION

The results of dynamic analyses performed for the Subpack 3 experiment packages and associated structure are presented in this ATM. The objectives of the analyses have been to estimate the acceleration environment at selected locations throughout the structure and to compute the associated dynamic loads resulting from both sinusoidal and random excitations.

Several iterations in the supporting structure were carried out during the design, and the launch random vibration environment was increased when the installation in LEM was changed from QUAD I to QUAD III.

### 2.0 ANALYSIS MODEL

The physical arrangement of the complete package is shown in Figure 1.

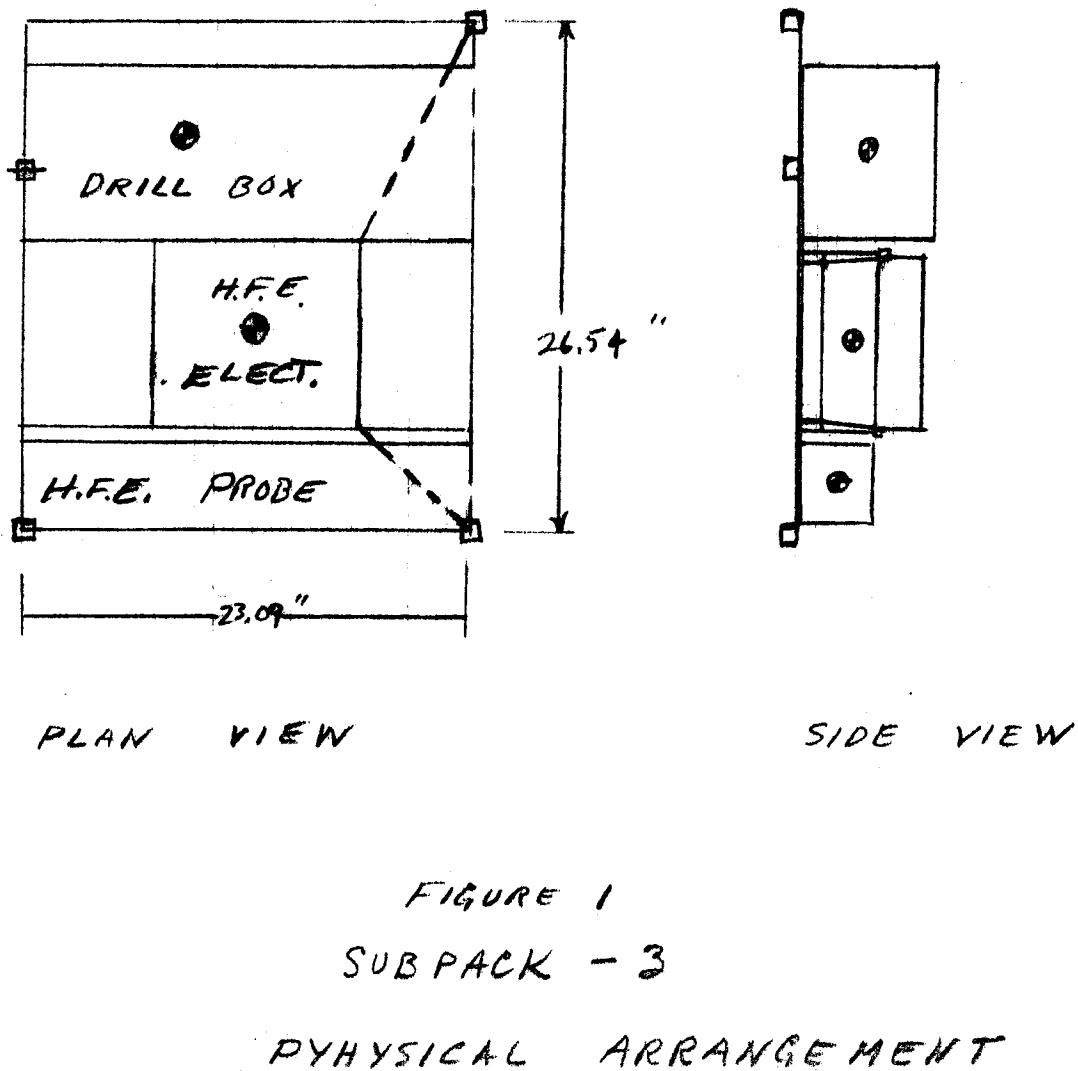
The mathematical model used in the analysis is a 15 degree of freedom, three-dimensional model which was derived from the coordinate definition drawing of Figure 2.

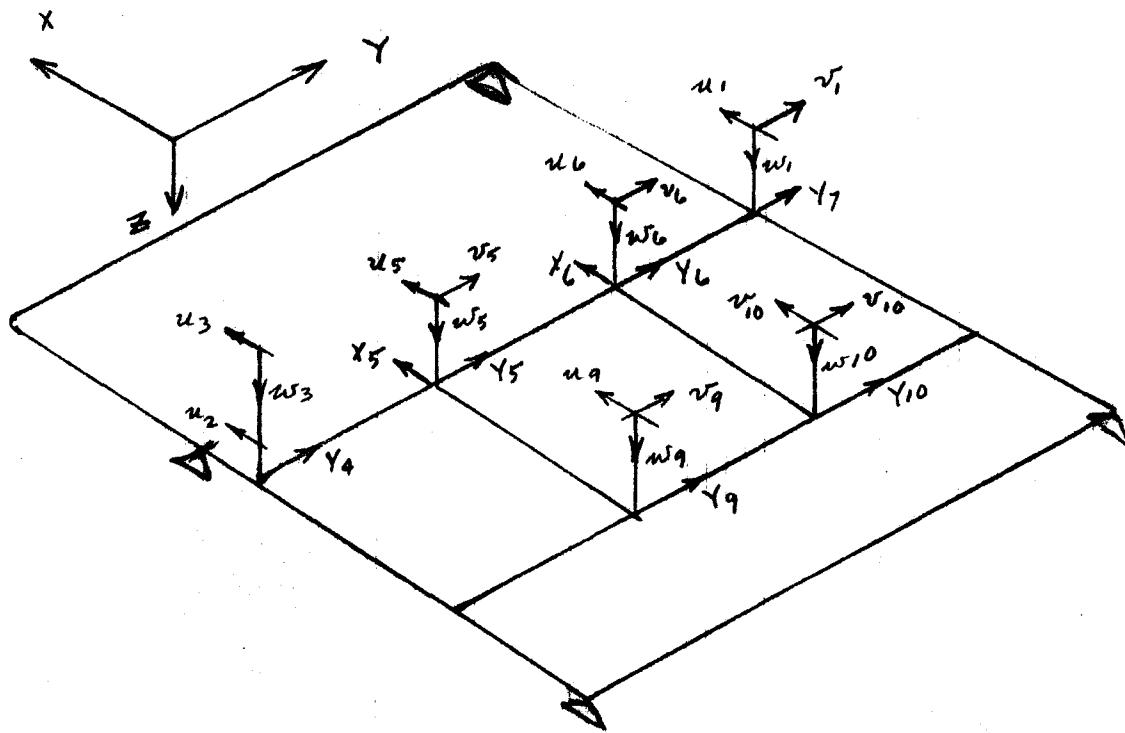
The drill box and structure is considered to be a rigid mass attached at 3 points having dimensions, mass and c.g. characteristics shown in Figure 3.

The H. F. E. electronic box is considered to be a rigid mass attached at four points and having the dimensions, mass-c.g. characteristics shown in Figure 4.

The H. F. E. probe box is not considered as part of the dynamics model since it is attached very close to the input or LEM attachment points and is relatively small in mass.

Structural support frame weight is lumped at four locations immediately below the electronics box attachments.





### FRAME COORDINATE RELATIONS

$z_4, z_5, z_6, z_7, z_9, z_{10}$  SAME AS  $w_4, w_5, \dots$

$$Y_5 = Y_4 = Y_6 = Y_7$$

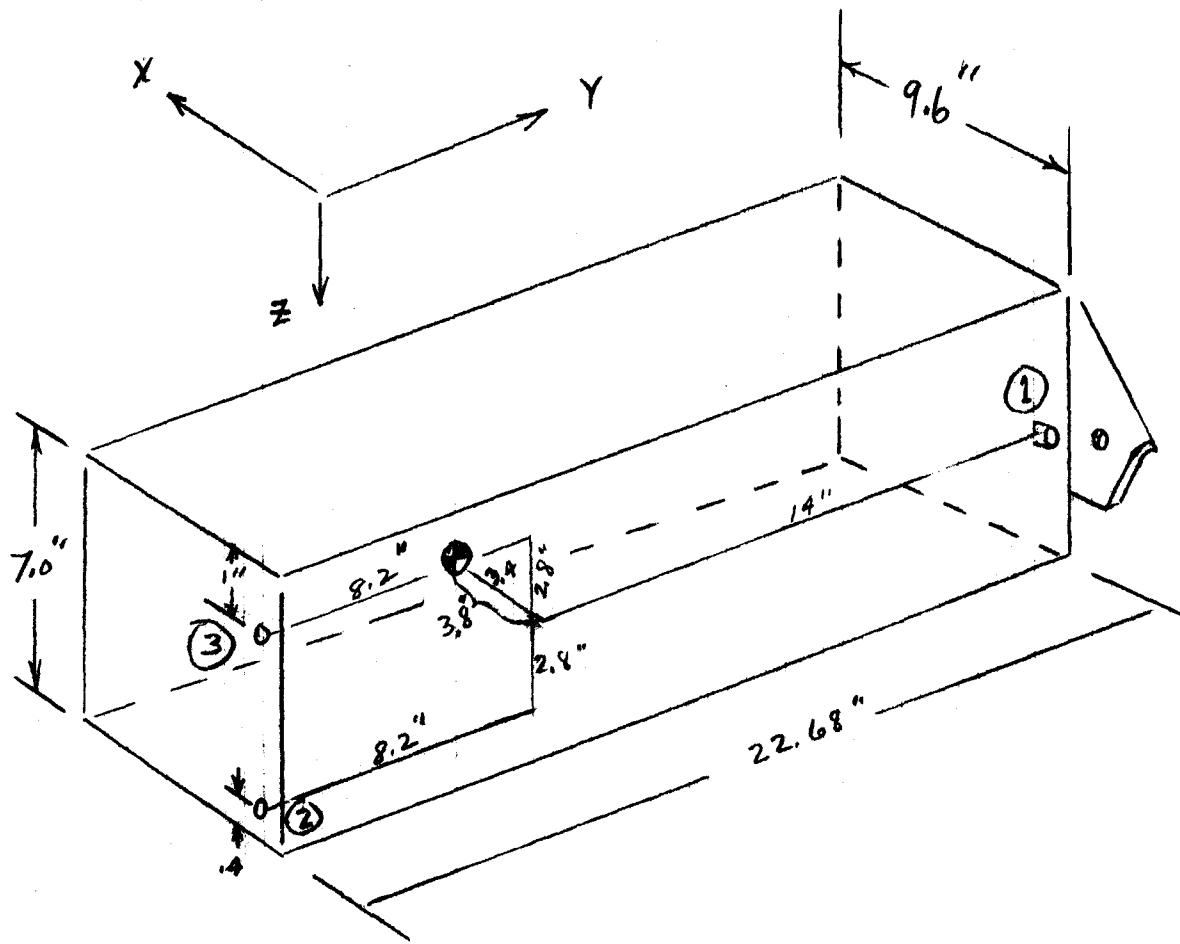
$$Y_9 = Y_{10}$$

$$X_5 = X_9$$

$$X_6 = X_{10}$$

FIGURE 2

COORDINATE SYSTEMS



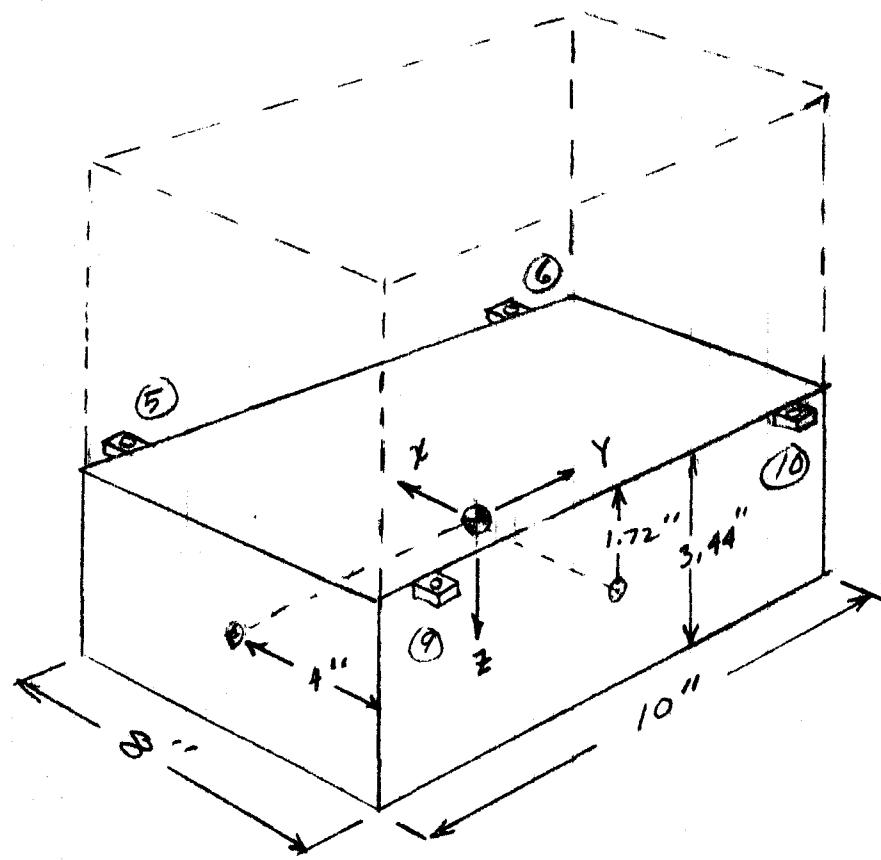
WEIGHT 30 LB.

$I_x$  3.65 lb-in-sec<sup>2</sup>

$I_y$  .915

$I_z$  3.93

FIGURE 3 DRILL BOX



WEIGHT 6.6 LB.

$$I_x = .159$$

$$I_y = .108$$

$$I_z = .234$$

FIGURE 4 H.F.E. ELECTRONICS



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Stiffness Matrix

The frame and experiment package attachment stiffness elements for use in the three-dimensional complete stiffness matrix were obtained mostly through the static structure analysis described in detail in Section II of this ATM.

There are 21 coordinates (and forces) associated with the unreduced stiffness matrix as follows:

TABLE 1

COORDINATES AND FORCES

<u>Location</u>	<u>Coordinate</u>	<u>Forces</u>
1	U <sub>3</sub>	F U <sub>3</sub>
2	U <sub>5</sub> = U <sub>9</sub>	F U <sub>5</sub> + F U <sub>9</sub>
3	V <sub>5</sub> = V <sub>6</sub>	F V <sub>5</sub> + F V <sub>6</sub>
4	U <sub>10</sub> = U <sub>6</sub>	F U <sub>10</sub> + F U <sub>6</sub>
5	V <sub>9</sub> = V <sub>10</sub>	F V <sub>9</sub> + F V <sub>10</sub>
6	U <sub>1</sub>	F U <sub>1</sub>
7	V <sub>1</sub>	F V <sub>1</sub>
8	X <sub>5</sub> '	F X <sub>5</sub> '
9	X <sub>6</sub> '	F X <sub>6</sub> '
10	Y <sub>5</sub> '	F Y <sub>5</sub> '
11	Y <sub>9</sub> '	F Y <sub>9</sub> '
12	W <sub>3</sub> = W <sub>4</sub>	F W <sub>3</sub> , W <sub>4</sub>
13	W <sub>5</sub>	F W <sub>5</sub>
14	W <sub>6</sub>	F W <sub>6</sub>
15	W <sub>1</sub>	F W <sub>1</sub>
16	W <sub>9</sub>	F W <sub>9</sub>
17	W <sub>10</sub>	F W <sub>10</sub>
18	X <sub>5</sub>	F X <sub>5</sub>
19	X <sub>6</sub>	F X <sub>6</sub>
20	Y <sub>5</sub>	F Y <sub>5</sub>
21	Y <sub>9</sub>	F Y <sub>9</sub>



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Rigid body corner displacement relationships and attachment of the electronics box and drill package to the frame reduces the number of coordinates to 15 independent ones. This is defined by the matrix [B] and the following equation:

$$\{S\} = [B] \{q\}$$

where the vector  $\{q\}$  is defined

$$\left\{ \begin{array}{l} U_1 \\ V_1 \\ W_1 \\ U_3 \\ W_3 \\ X_5 \\ X_6 \\ Y_5 \\ Y_9 \\ U_5 \\ V_5 \\ V_9 \\ W_6 \\ W_{10} \\ W_5 \end{array} \right\} = \{q\} = \left\{ \begin{array}{l} q_1 \\ q_2 \\ q_3 \\ q_2 \\ q_5 \\ q_6 \\ q_7 \\ q_8 \\ q_9 \\ q_{10} \\ q_{11} \\ q_{12} \\ q_{13} \\ q_{14} \\ q_{15} \end{array} \right\}$$

See Figure 2 for coordinate direction and location. Subscript on  $q_i$  is computer program location number also.

The input matrices [K] and [B] are shown in Figures 5 and 6, and the reduced stiffness matrix [k] is shown in Figure 7. This is arrived at as follows:

$$[k] = [B]^T [K] [B] \quad (1)$$

#### Mass Matrix

The mass matrix is formed to the 15 generalized coordinates by transforming the drill box six degrees of freedom to 5 by constraining the heavy end (U3, W3) to one translation and one rotation. Also the electronics box six degrees of freedom at the c.g. were transformed to six coordinates at the attachment points. Finally, the remaining four coordinates are the frame motion in the plane of the frame.

The mass matrix is shown in Figure 8.

## K MATRIX

ROW 1	0.327000CE 05 0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 2	0.0	0.782000CE 04 0.0	0.0	0.0	0.0	0.0	-0.782000E 04	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 3	0.0	0.0	0.2670000E 05 0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	-0.267000CE 05 0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 4	0.0	0.0	0.0	0.1666000E 05 0.0	0.0	0.0	0.0	0.0
	0.0	0.0	-0.166600CE 05 0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 5	0.0	0.0	0.0	0.0	0.2670000E 05 0.0	0.0	0.0	0.0
	0.0	0.0	-0.2670000E 05 0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 6	0.0	0.0	0.0	0.0	0.0	0.8620000E 05 0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 7	0.0	0.0	0.0	0.0	0.0	0.0	0.2045000E 05 0.0	0.0
	0.0	0.0	-0.204500CE 05 0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 8	0.0	0.0	-0.782000CE 04 0.0	0.0	0.0	0.0	0.0	0.782000E 04
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 9	0.0	0.0	0.0	-0.1666000E 05 0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 10	0.0	0.0	0.0	-0.2670000E 05 0.0	0.0	0.0	-0.2045000E 05 0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 11	0.0	0.0	0.0	0.0	-0.2670000E 05 0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 12	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.1202900E 05	-0.2910400E 05	0.1507800E 05	-0.4744000E 04	-0.2960700E 05
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 13	0.0	0.0	0.0	0.0	0.0	v.v	v.v	0.0
	0.0	0.0	0.0	-0.2910400E 05	0.5034800E 05	-0.3468700E 05	0.1250000E 05	-0.4000000E 02
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 14	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.1507800E 05	-0.3468700E 05	0.5013200E 05	-0.2288600E 05	0.3012998E 03
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

FIGURE 5

ROW 15	0.0	0.0	0.0	0.0	-0.4744000E 04	-0.1250000E 05	-0.2288600E 05	0.2795200E 05	0.2023000E 04	0.0
	0.0	0.0	0.0	0.0	-0.4086000E 04	0.0	0.0	0.0	0.0	0.0
	-0.4086000E	04	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 16	0.0	0.0	0.0	0.0	-0.2960700E 05	-0.4000000E 02	0.3012000E 01	0.302000E 04	0.3673500E 05	0.0
	0.0	0.0	0.0	0.0	-0.2665100E 05	0.0	0.0	0.0	0.0	0.0
	-0.2665100E	05	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 17	0.0	0.0	0.0	0.0	0.1503600E 05	0.2180000E 03	-0.657000E 04	-0.4086000E 04	-0.2665100E 05	0.0
	0.0	0.0	0.0	0.0	0.4936900E 05	0.0	0.0	0.0	0.0	0.0
	0.4936900E	05	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 18	0.0	0.0	0.0	0.0	0.1856800E 05	-0.4634098E 04	0.3608000E 04	0.3823000E 04	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.1856800E 05	-0.4634098E 04	0.3608000E 04	0.3823000E 04	0.0	0.0
ROW 19	0.0	0.0	0.0	0.0	0.4634098E 04	0.2152670E 06	0.6941400E 05	-0.5107100E 05	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.4634098E	04	0.2152670E	06	0.6941400E	05
ROW 20	0.0	0.0	0.0	0.0	0.3608000E 04	0.6941400E 05	0.5151800E 05	-0.1095200E 05	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.3608000E	04	0.6941400E	05	0.5151800E	05
ROW 21	0.0	0.0	0.0	0.0	0.3823000E 04	-0.5107100E 05	-0.1095200E 05	0.1002400E 06	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.3823000E	-0.5107100E	-0.1095200E	0.1002400E	06	0.0

FIGURE 5 (CONTINUED)

## B MATRIX

ROW 1	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0	0.0
ROW 2	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 3	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0	0.0
ROW 4	0.0	0.0	0.0	0.1000000E 01-0.7880000E 00	0.7880000E 00	0.0	0.0	0.0
ROW 5	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0	0.0
ROW 6	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 7	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 8	0.0	0.0	0.0	0.0	0.0	0.1000000E 01	0.0	0.0
ROW 9	0.0	0.0	0.0	0.0	0.0	0.0	0.1000000E 01	0.0
ROW 10	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.1000000E 01
ROW 11	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 12	0.0	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0
ROW 13	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.1000000E 01
ROW 14	0.0	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0
ROW 15	0.0	0.0	0.0	0.1000000E 01	0.0	0.0	0.0	0.0
ROW 16	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 17	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 18	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
ROW 19	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.1000000E 01
ROW 20	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.1000000E 01
ROW 21	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

FIGURE 6

-3 S/P 70 NEW LEVELS  
STIFFNESS MATRIX\* C.1CCCCCCC-C3

1980 MARCH 14, 1980 FORM 73

1	C.662000 C1	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
2	0.0	0.204500 01	0.0	0.0	0.0	0.0
	0.0	-0.204500 01	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
3	0.0	0.0	0.279520 01	0.0	-0.474400 00	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	-0.249090 C1	-0.206300 00	0.145230 01			
4	0.0	0.0	0.0	0.327000 01	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	-0.474400 00	0.0	0.120280 02	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	C.446850 C1	-0.145710 01	-0.587110 01			
6	0.0	0.0	0.0	0.0	0.0	0.263880 01
	-0.463410 C0	0.360800 00	0.382300 00	-0.782000 00	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
7	0.0	0.0	0.0	0.0	0.0	-0.463410 00
	0.231930 C2	0.694140 01	-0.510710 01	-0.166600 01	0.131280 01	-0.131280 01
	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	-0.204500 01	0.0	0.0	0.0	0.360800 00
	0.694140 01	C.966800 01	-0.109520 01	0.0	-0.267000 01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0	0.0	0.382300 00
	-C.510710 01	-C.109520 01	0.126940 02	0.0	0.0	-0.267000 01
	0.0	0.0	0.0	0.0	0.0	0.0
10	0.0	0.0	0.0	0.0	0.0	-0.782000 00
	-0.131280 01	0.0	0.0	0.244800 01	-0.131280 01	0.131280 01
	0.0	0.0	0.0	0.0	0.0	0.0
11	0.0	0.0	0.0	0.0	0.0	0.0
	0.131280 01	-0.267000 01	0.0	-0.131280 01	0.370450 01	-0.103450 01
	0.0	0.0	0.0	0.0	0.0	0.0
12	0.0	0.0	0.0	0.0	0.0	0.0
	-0.131280 C1	0.0	-0.267000 01	0.131280 01	-0.103450 01	0.370450 01
	0.0	0.0	0.0	0.0	0.0	0.0
13	0.0	0.0	-0.249090 01	0.0	0.446850 01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	C.662640 C1	-0.163530 C1	-0.710810 C1			
14	0.0	0.0	-0.206300 00	0.0	-0.145710 C1	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	-0.163530 C1	0.328020 01	0.102620 01			
15	0.0	0.0	0.145230 01	0.0	-0.587110 01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	-C.710810 C1	C.102620 01	0.870030 01			

FIGURE 7

MASS	X	Y	Z	W	V	U
1	0.203500-C1	-0.133000-01	0.0	0.111800-01	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
2	-0.133000-C1	0.777000-01	0.0	0.190500-01	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
3	0.0	0.0	0.180000-01	-0.161400-C1	0.106800-01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
4	0.111800-C1	0.190500-01	-0.161400-01	0.129200-00	-0.264000-01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
5	0.0	0.0	0.106800-01	-0.264000-01	0.384000-01	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
6	0.0	0.0	0.0	0.0	0.0	0.259000-02
	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
7	0.0	0.0	0.0	0.0	0.0	0.0
	0.259000-C2	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
8	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.324000-02	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
9	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.324000-02	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.0	0.0
10	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.170900-01	-0.683600-02	0.683600-02
	-0.336300-C2	C.363000-02	0.0			
11	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	-0.683600-02	0.100600-01	-0.151900-02
	-0.756700-C3	-C.134500-02	0.210200-02			
12	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.683600-02	-0.151900-02	0.100600-01
	-0.344700-C2	0.134500-02	0.210200-02			
13	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	-0.336300-02	-0.756700-03	-0.344700-02
	0.598400-C2	-C.274600-02	-0.323800-02			
14	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.363000-02	-0.134500-02	0.134500-02
	-0.274600-02	0.701900-02	0.427300-02			
15	0.0	0.0	0.0	0.0	0.0	0.0
	0.0	0.0	0.0	0.0	0.210200-02	0.210200-02
	-0.323800-C2	C.427300-02	0.751060-02			

FIGURE 8



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### 3.0 COMPUTED RESPONSES

A normal mode analysis was performed using the stiffness and mass matrices of Figures 7 and 8 to obtain the natural frequencies and mode shapes given in Figure 9.

Then, using an assumed damping factor of 10% of critical, the responses to sine and random base motion inputs at selected locations were computed by summing the responses of the normal modes. The sine input is shown in Figure 10 and the random inputs are shown in Figure 11. The higher curve of Figure 11 is the latest assessment of the environment in QUAD III. The analysis was also performed for the lower levels of QUAD I.

MODE 1	MODE 2	MODE 3	MODE 4
EIGENVALUE= 0.712980-05 FREQUENCY= 0.596050 02	EIGENVALUE= 0.391060-05 FREQUENCY= 0.804210 02	EIGENVALUE= 0.106660-05 FREQUENCY= 0.154110 03	EIGENVALUE= 0.927890-06 FREQUENCY= 0.165220 03
EIGENVECTOR	EIGENVECTOR	EIGENVECTOR	EIGENVECTOR
-0.128550-01 0.100000 01 -0.307940-01 0.188270 00 -0.864560-02 -0.611440-01 -0.153430 00 0.440780 00 -0.175160-01 0.824700-01 0.421360 00 0.218450-01 -0.1e9210-01 -0.125040-01 -0.134610-01	0.579230-01 -0.538930 00 -0.342040 00 0.100000 01 -0.112520 00 0.359870-01 0.861400-01 -0.244330 00 0.930650-02 -0.375460-01 -0.239250 00 -0.152910-01 -0.221320 00 -0.129990 00 -0.187610 00	0.452600-01 -0.552880-01 0.100000 01 0.222030 00 0.161170 00 -0.111130 00 -0.141410-01 -0.246520-01 -0.197140-02 -0.344980 00 -0.951100-01 0.120760-01 0.762150 00 0.403950 00 0.568660 00	0.892810-02 0.516160-02 0.227470 00 0.533660-01 0.682730-01 0.360670 00 0.612460-01 -0.632950-01 -0.224160-01 0.100000 01 0.442900-01 -0.181450 00 0.893160-01 0.232930 00 0.646010-01
MODE 5	MODE 6	MODE 7	MODE 8
EIGENVALUE= 0.532090-06 FREQUENCY= 0.218190 02	EIGENVALUE= 0.405000-06 FREQUENCY= 0.250090 03	EIGENVALUE= 0.263930-06 FREQUENCY= 0.298680 03	EIGENVALUE= 0.148620-06 FREQUENCY= 0.319190 03
EIGENVECTOR	EIGENVECTOR	EIGENVECTOR	EIGENVECTOR
0.575560-01 -0.640710-01 -0.415410 00 0.526650-01 0.455150 00 -0.833580-01 -0.697320-01 0.371620 00 0.159470 00 0.731940-01 0.100000 01 0.729C50 00 0.525470-02 0.226500 00 0.540900 00	0.245520-01 -0.371660-01 0.688410 00 -0.153320-01 -0.495450 00 0.102730-01 -0.969260-01 0.381580 00 0.110300 00 0.313670 00 0.100000 01 0.521680 00 -0.192830 00 -0.427310 00 -0.635420 00	-0.275710-01 0.204400-01 0.641180-01 0.153770-01 0.337090-01 -0.205840 00 0.234320 00 -0.356660 00 0.307630 00 -0.613310 00 -0.726260 00 0.100000 01 -0.186770 00 -0.120250 00 -0.142810 00	-0.313130 00 -0.340790-01 0.416670-01 -0.627750-01 -0.473800 00 -0.535980-01 0.469440-01 -0.257850-01 0.110590 00 -0.959120-01 0.165340-01 0.384e50 00 0.100000 01 0.632060 00 0.683440 00

FIGURE 9. FREQUENCIES AND MODE SHAPES

MODE 9  
EIGENVALUE= 0.18271D-06  
FREQUENCY= 0.37234D 03

EIGENVECTOR  
0.10000D 01  
0.22618D 00  
-0.10566D 00  
-0.18713D 00

MODE 10  
EIGENVALUE= 0.10880D-06  
FREQUENCY= 0.48251D 03

EIGENVECTOR  
0.13618D-01  
0.78060D-02  
-0.64346D-01  
-0.46881D-02

MODE 11  
EIGENVALUE= 0.91579D-07  
FREQUENCY= 0.52592D 03

EIGENVECTOR  
0.48285D-02  
0.38876D-02  
0.51960D-01  
-0.97110D-03

MODE 12  
EIGENVALUE= 0.43307D-07  
FREQUENCY= 0.76479D 03

EIGENVECTOR  
-0.16074D-01  
-0.15767D-01  
-0.18287D-01  
0.58552D-02

-0.22217D 00  
-0.67549D-01  
0.33557D-02  
0.36327D-01  
0.39005D-01  
-0.71652D-01  
-0.82227D-01  
0.12855D 00  
0.25035D 00  
0.24711D 00  
0.12256D 00

0.28427D-01  
0.10000D 01  
0.93559D-01  
-0.14322D 00  
0.11522D-01  
0.21440D 00  
0.88055D-02  
0.64899D-01  
0.61982D 00  
-0.64251D 00  
0.61196D 00

-0.31558D-01  
0.10000D 01  
0.34512D-01  
-0.11322D 00  
-0.21371D-01  
-0.32528D 00  
-0.29312D-01  
0.50327C-01  
-0.52527D 00  
0.50548D 00  
-0.47742D 00

0.21338D-01  
0.17926D 00  
-0.42367D 00  
0.10000D 01  
-0.13601D 00  
-0.12048D 00  
-0.19043D 00  
0.16035D 00  
0.10069D 00  
0.85586D-01  
-0.83918D-01

MODE 13  
EIGENVALUE= 0.30035D-07  
FREQUENCY= 0.91835D 03

EIGENVECTOR  
-0.55040D-02  
-0.32584D-02  
-0.68186D-01  
0.51138D-02  
0.61841D-01  
0.46129D-01  
0.27911D 00  
0.13116D 00  
0.16000D 01  
0.15666D-01  
0.26942D 00  
0.13336D 00  
0.42720D 00  
0.52505D 00  
-0.53008D 00

MODE 14  
EIGENVALUE= 0.25201D-07  
FREQUENCY= 0.10026D 04

EIGENVECTOR  
0.25910D-02  
-0.94378D-03  
0.95897D-01  
-0.54498D-02  
-0.85324D-01  
0.50894D-01  
0.17497D 00  
0.40948D 00  
0.10000D 01  
0.77024D-01  
-0.43665D 00  
-0.55607D 00  
-0.76362D 00  
-0.86599D 00  
0.86379D 00

MODE 15  
EIGENVALUE= 0.97061D-08  
FREQUENCY= 0.16155D 04

EIGENVECTOR  
-0.80340D-03  
-0.98447D-03  
0.20660D-03  
0.25693D-03  
0.12478D-03  
-0.18405D-01  
0.10000D 01  
0.30499D 00  
-0.26352D 00  
-0.14803D-01  
-0.25686D-02  
0.12152D-02  
-0.69232D-02  
0.92997D-02  
-0.68127D-02

FIGURE 9. (CONTINUED).

SINUSOIDAL VIBRATION INPUT

Axis: X, Y, Z

Sweep Rate:

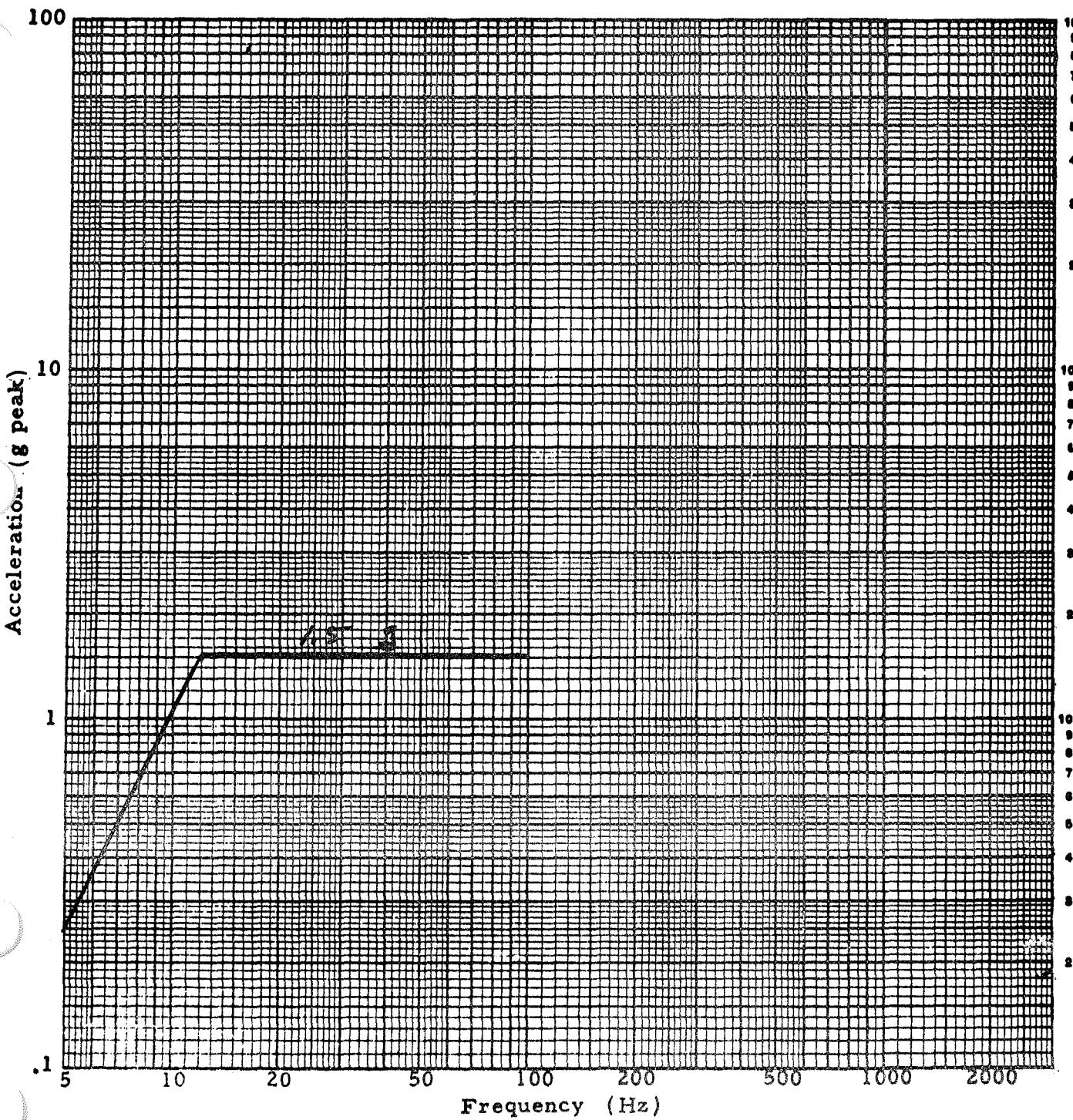
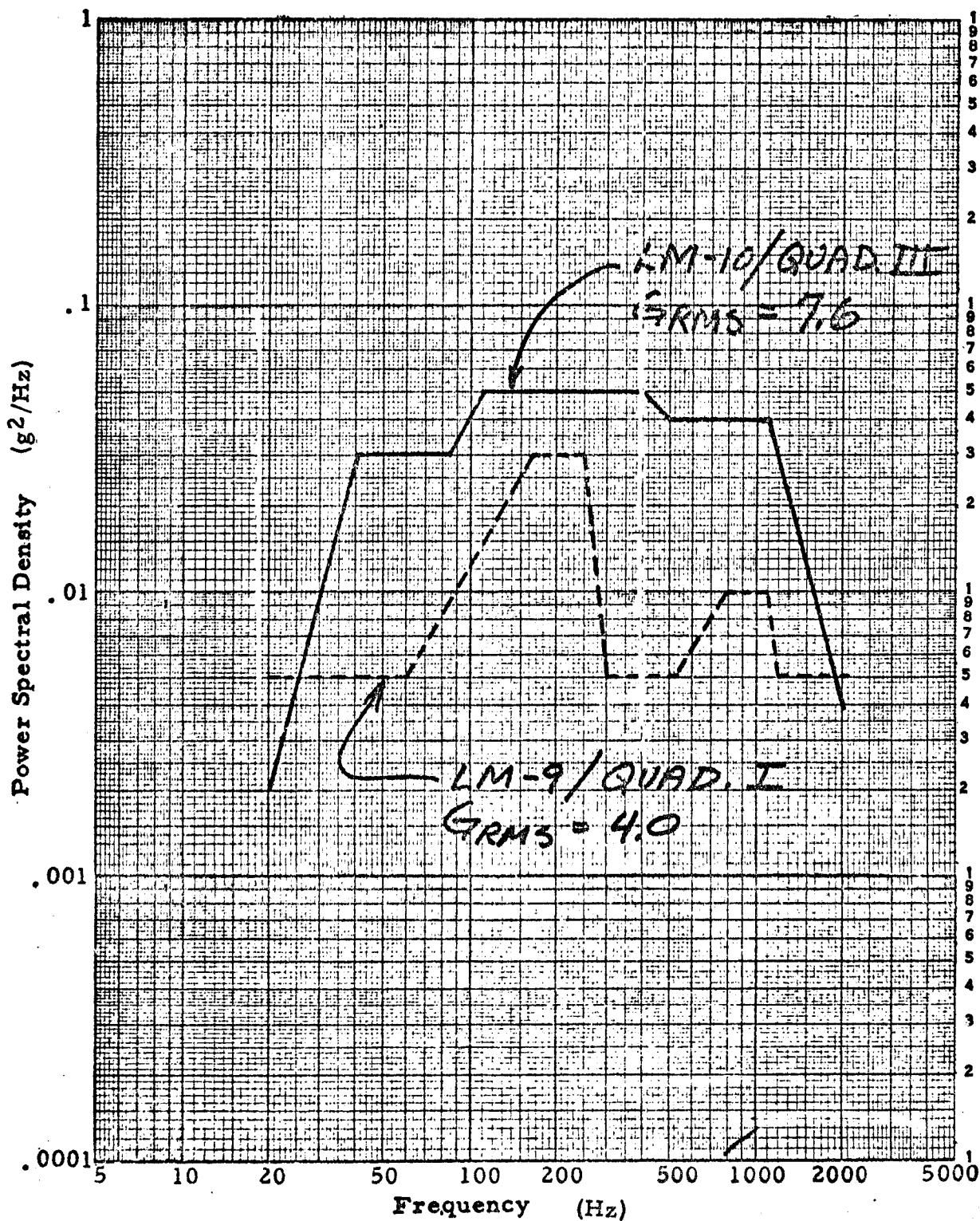


Figure 11

*SP-3 L&B*  
RANDOM VIBRATION SPECTRUM

Axis:  $x, y, z$ 

Duration: 60 sec.





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Figures 12 through 28 present the computed plots of transmissibility sine response and random response at selected locations having the largest overall response. The figures are in 3 or 4 parts depending on whether both QUAD I and QUAD III levels were calculated for the random response. If the words "New Levels" appear in the random response curve title, QUAD III levels were used as input.

A summary of all the computed overall rms values is given in Table 2. The maximum sine responses can be observed on the sine response curves. None of the calculations indicate levels higher than 8g peak (Figure 18 b) for the sine accelerations, therefore the most attention is paid to the random vibration results.

#### 4.0 DYNAMIC LOADS

As discussed previously the flexibility and stiffness influence coefficients were developed for the support structure in the three axes of loading. These results were then incorporated into the three-dimensional program from which the reduced stiffness matrix is determined for use in the dynamics analysis program.

The computed accelerations and the redundant frame stiffness matrix provide all the necessary information for computing the dynamic loads at the attachment points and in the frame.

The three-dimensional stiffness matrix for the structural system is shown in Figure 5. This is a 21 x 21 matrix with the displacement coordinates shown in Table 1. The forces associated with these coordinates are in the corresponding direction and location in the 21 locations.

This stiffness matrix is reduced in size to correspond to the selected 15 generalized coordinates by the transformation

$$[k] = [B]^T [K] [B] \quad (1)$$

where  $[B]$  is a 21 x 15 matrix relating the coordinates of Figure 5 to the 15 generalized coordinates. This is given in Figure 6.

The internal loads on the structure and the associated displacements can be determined from the following relations:

$$\{P\} = [K] [B] [k]^{-1} \{Q\} \quad (2)$$

and

$$\{S\} = [B] [k]^{-1} \{Q\} \quad (3)$$

where  $P_n$  is an internal load and  $S_n$  is the displacement.



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TABLE 2  
OVERALL RESPONSES TO RANDOM EXCITATION G-RMS

Computer Location Number	Coordinate	X		Y		Z	
		(a)*	(b)*	(a)	(b)	(a)	(b)
1	U <sub>4</sub>	5.50	11.2		.54		1.54
2	V <sub>1</sub>		2.73		3.6		1.1
3	W <sub>1</sub>		5.55		2.2	8.24	11.3
4	U <sub>3</sub>	2.22	4.46		.88		3.1
5	W <sub>3,4</sub>		3.74		1.76	4.02	6.05
6	X <sub>5</sub>	4.64	9.0		2.10		1.02
7	X <sub>6</sub>		11.5		3.07		.614
8	Y <sub>5</sub>		3.87	4.84	5.98		1.96
9	Y <sub>9</sub>		3.73	6.80	13.1		1.40
10	U <sub>5</sub>	5.24	8.79		2.47		2.57
11	V <sub>5</sub>		2.43	4.95	7.06		4.4
12	V <sub>9</sub>		2.28	6.34	8.38		3.1
13	W <sub>6</sub>	4.15	6.99		2.61	6.30	9.35
14	W <sub>10</sub>	3.73	6.37		2.94	4.64	7.19
15	W <sub>5</sub>		5.28		3.33	6.07	9.11

(a)\* QUAD I environment excitation

(b)\* QUAD III environment excitation



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The next step is to compute the load vectors,  $\{Q\}$ , resulting in this case from the dynamics environment.

#### Calculation of Load Vectors

##### Random Loading

The expression for the load vectors,  $\{Q\}$ , for the random loading case is

$$[Q]^T \equiv [m] [A] \quad (4)$$

where

$[m]$  = mass matrix (Figure 8)

$[A]$  = a diagonal matrix composed of the local rms acceleration computed with the dynamics analysis program, i.e., Table 2 type values multiplied by the acceleration of gravity.

When the  $\{Q\}$ -column vectors have been determined, they are applied to equations (2) and (3) to compute the internal loads and displacements at the attachment points and on the array. For the random case the rms internal loads and displacements are computed for each modal equation giving 15 sets of rms values at the 21 coordinate locations. Then for each location the 15-modal rms values are combined by taking the square root of the sum of the squares of the 15 values, thus reducing the number to 21 load and 21 displacement values.

##### Sinusoidal Loading

The load vectors,  $\{Q\}$ , are again formed by Equation (4), but real and imaginary steps are computed separately and combined into one load vector for each frequency where a maximum sine response occurs.

For the sinusoidal loading case there is only one  $\{Q\}$  vector per frequency selected and each one will produce a set of internal loads and displacements.



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Application of the foregoing procedure to the present structure results in the load and deflection sets due to the random excitation shown in Table 3. Loads due to sinusoidal excitation are all less than the 3-sigma random values obtained by multiplying the Table 3 loads by 3 and are therefore not shown.

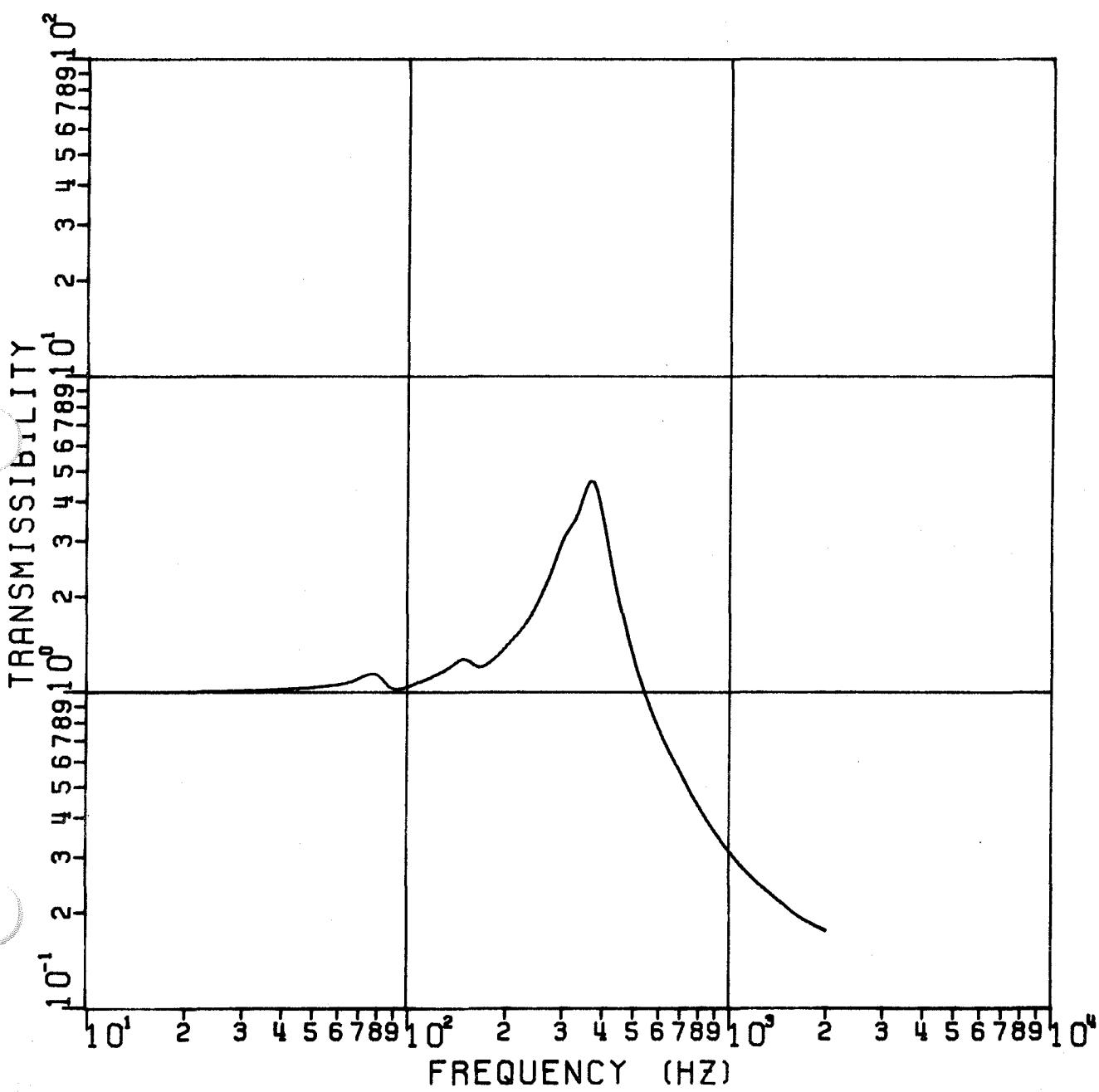
1 X AXIS SUBPACK 3 SEP 1970

FIGURE 12a TRANSMISSIBILITY

LOCATION

1

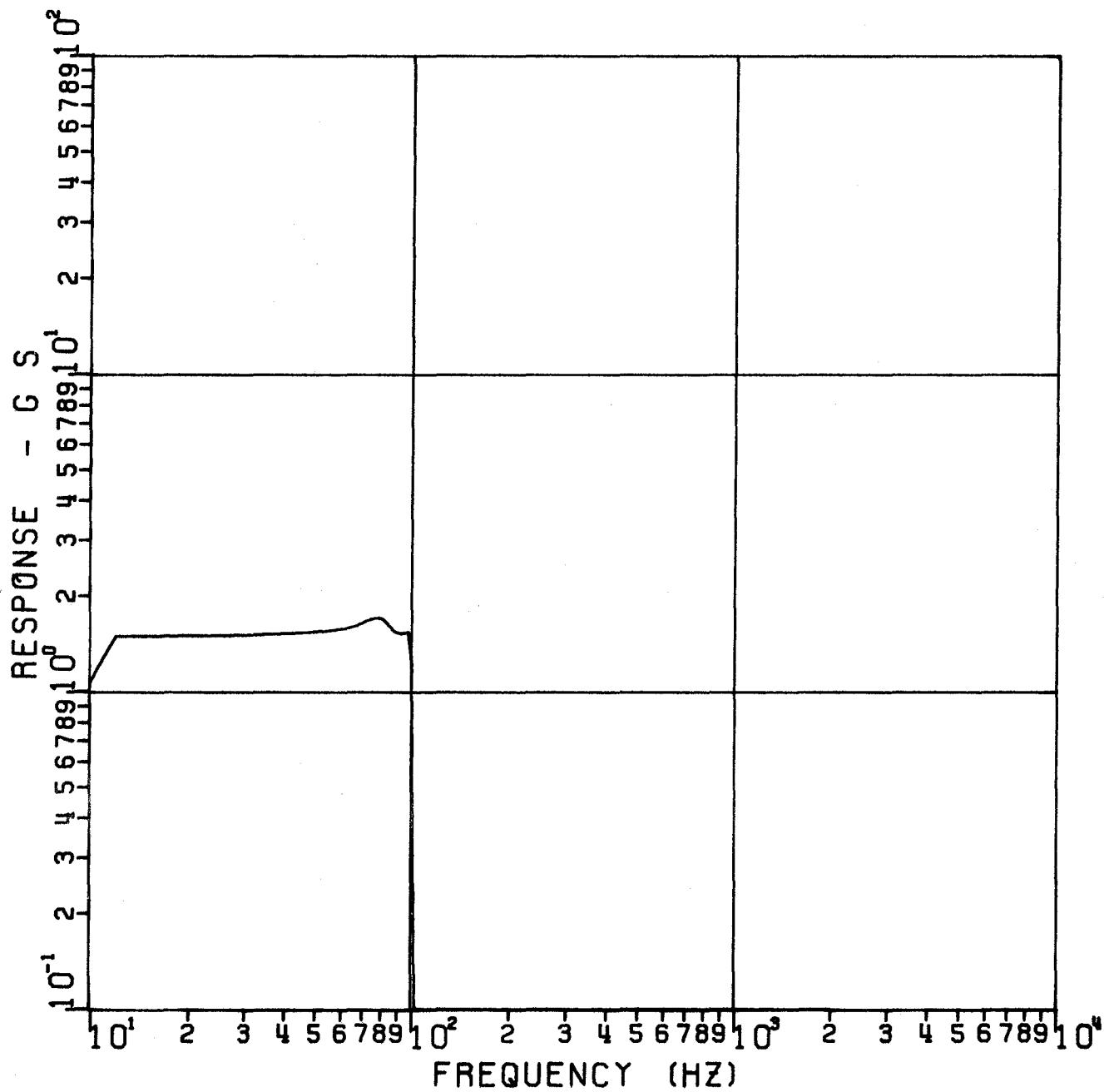
$u_1$



1 X AXIS SUBPACK 3 SEP 1970

FIGURE 12 b SINE RESPONSE

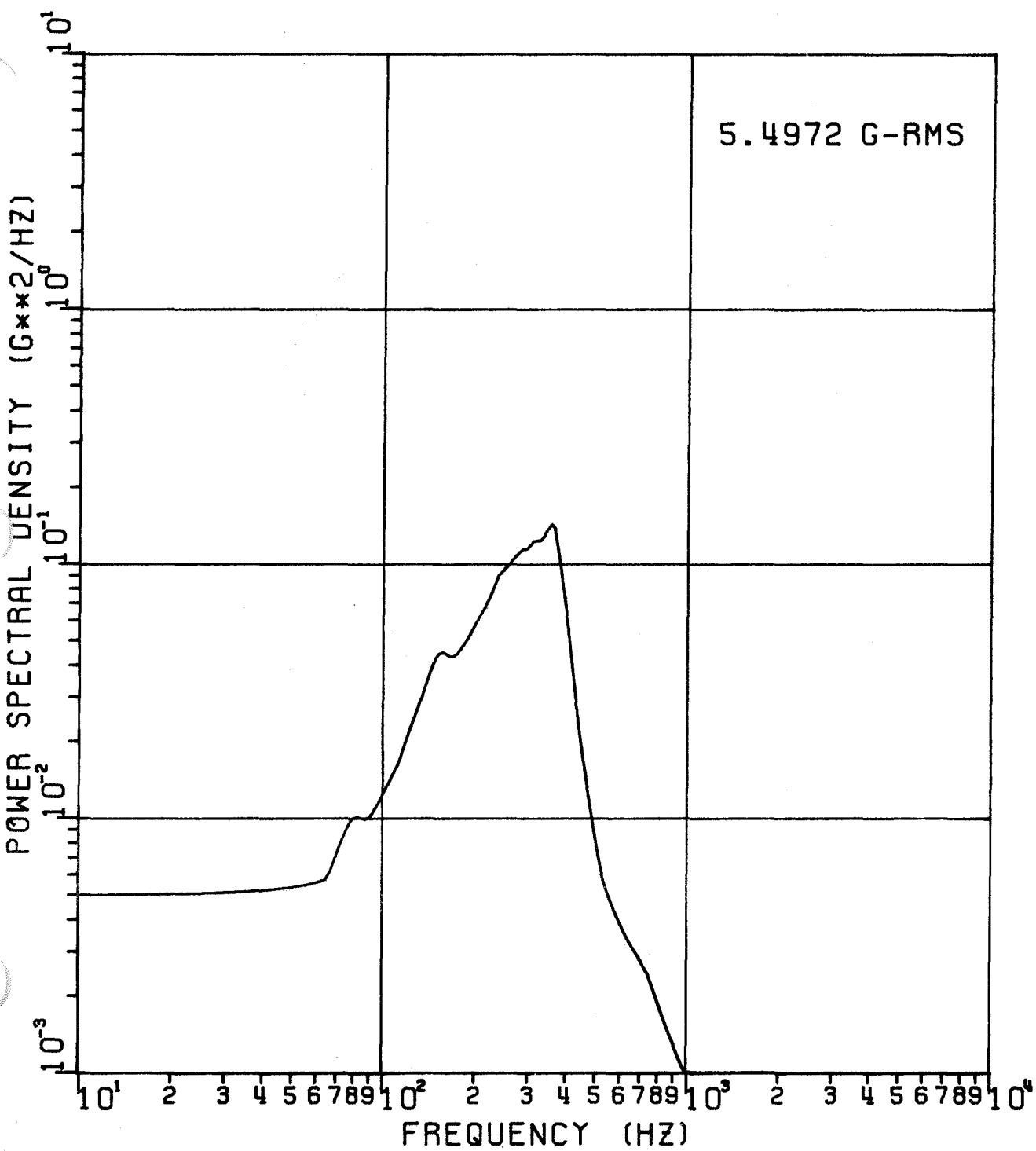
LOCATION 1



1 X AXIS SUBPACK 3 SEP 1970

## FIGURE 12c RANDOM VIBRATION SPECTRUM

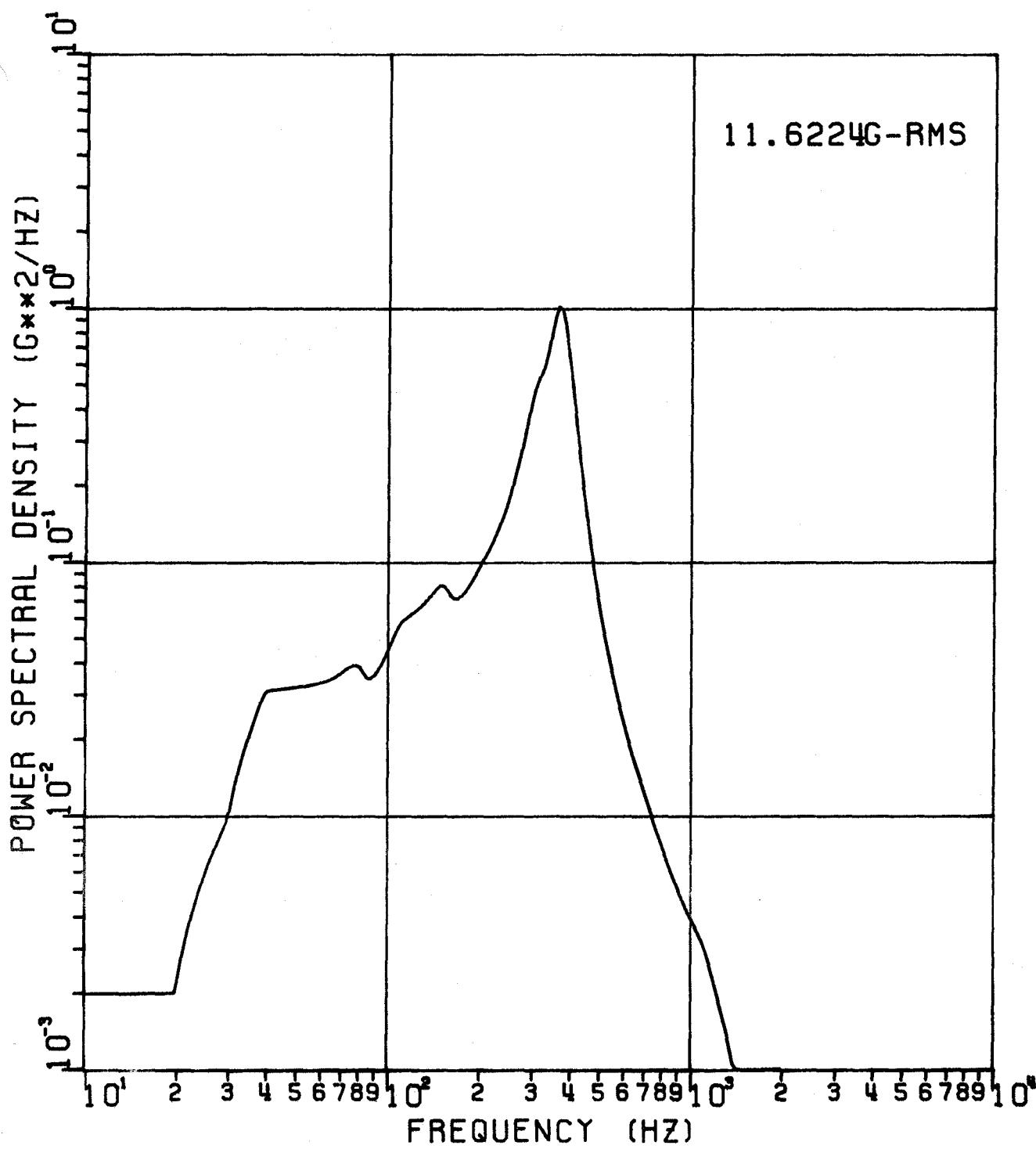
LOCATION 1



1 X AXIS SUBP. 3 SEP 70 NEW LEVELS

## FIGURE 12d RANDOM VIBRATION SPECTRUM

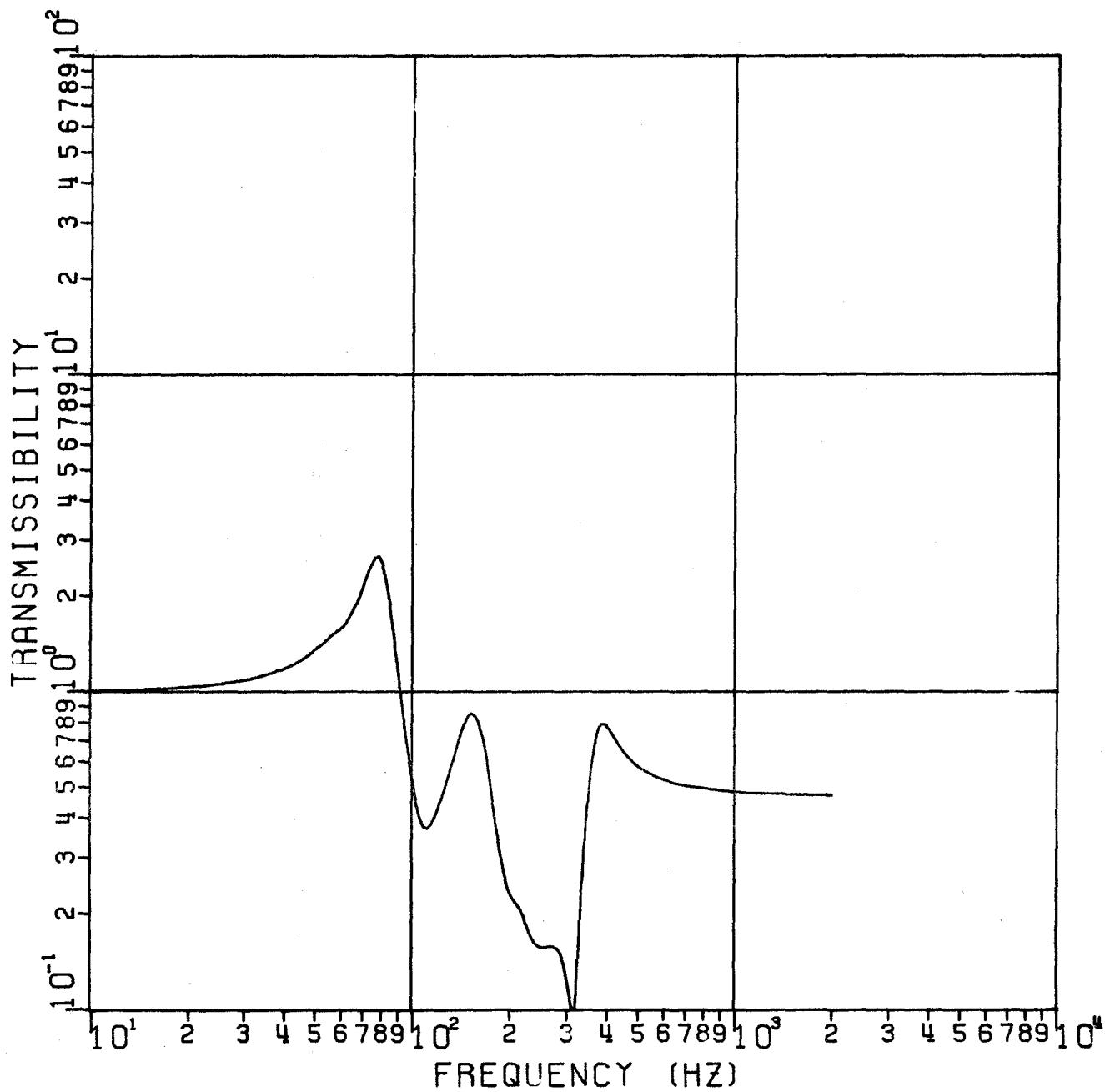
LOCATION 1



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 13a TRANSMISSIBILITY

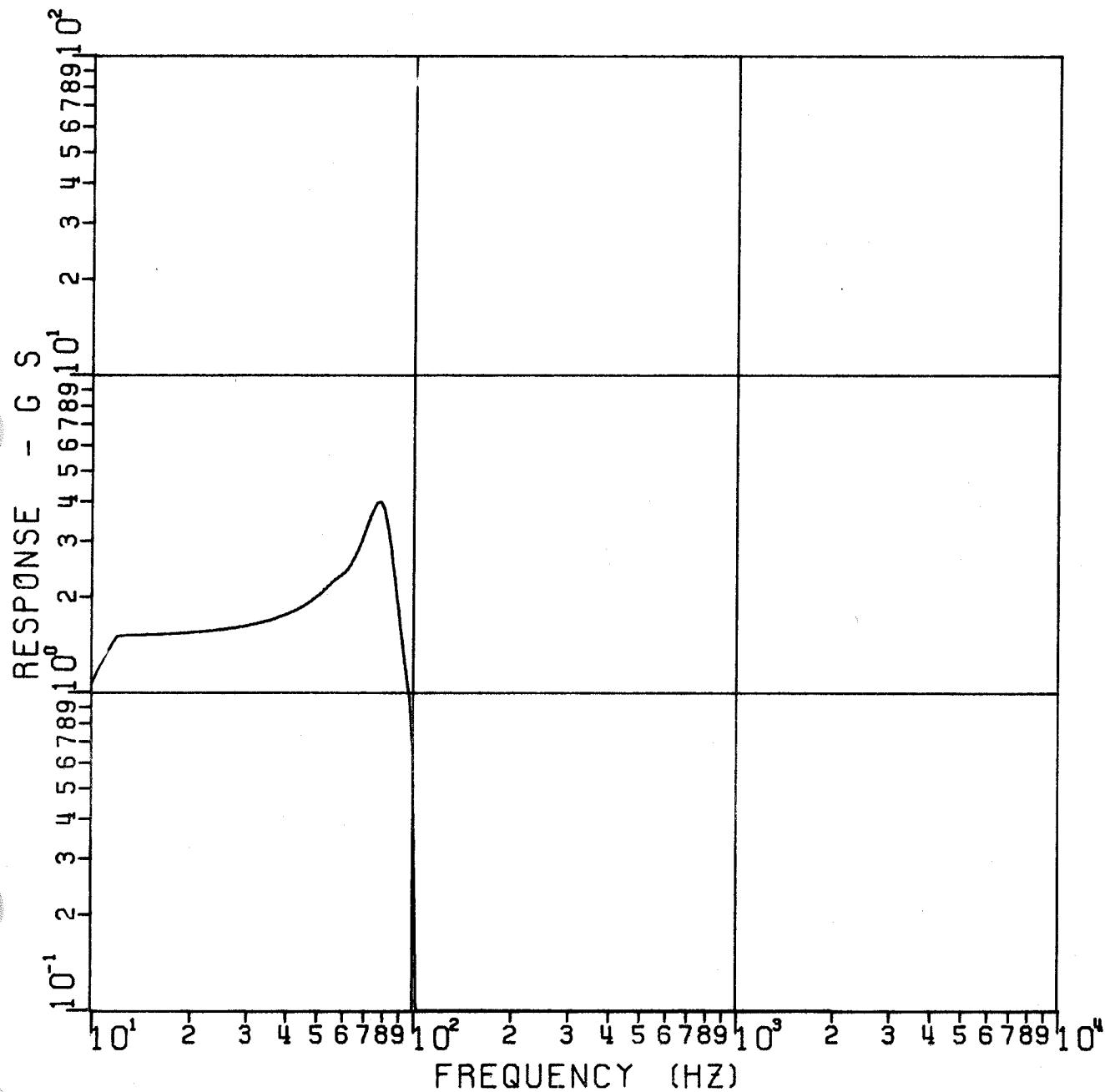
LOCATION 4



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 13b SINE RESPONSE

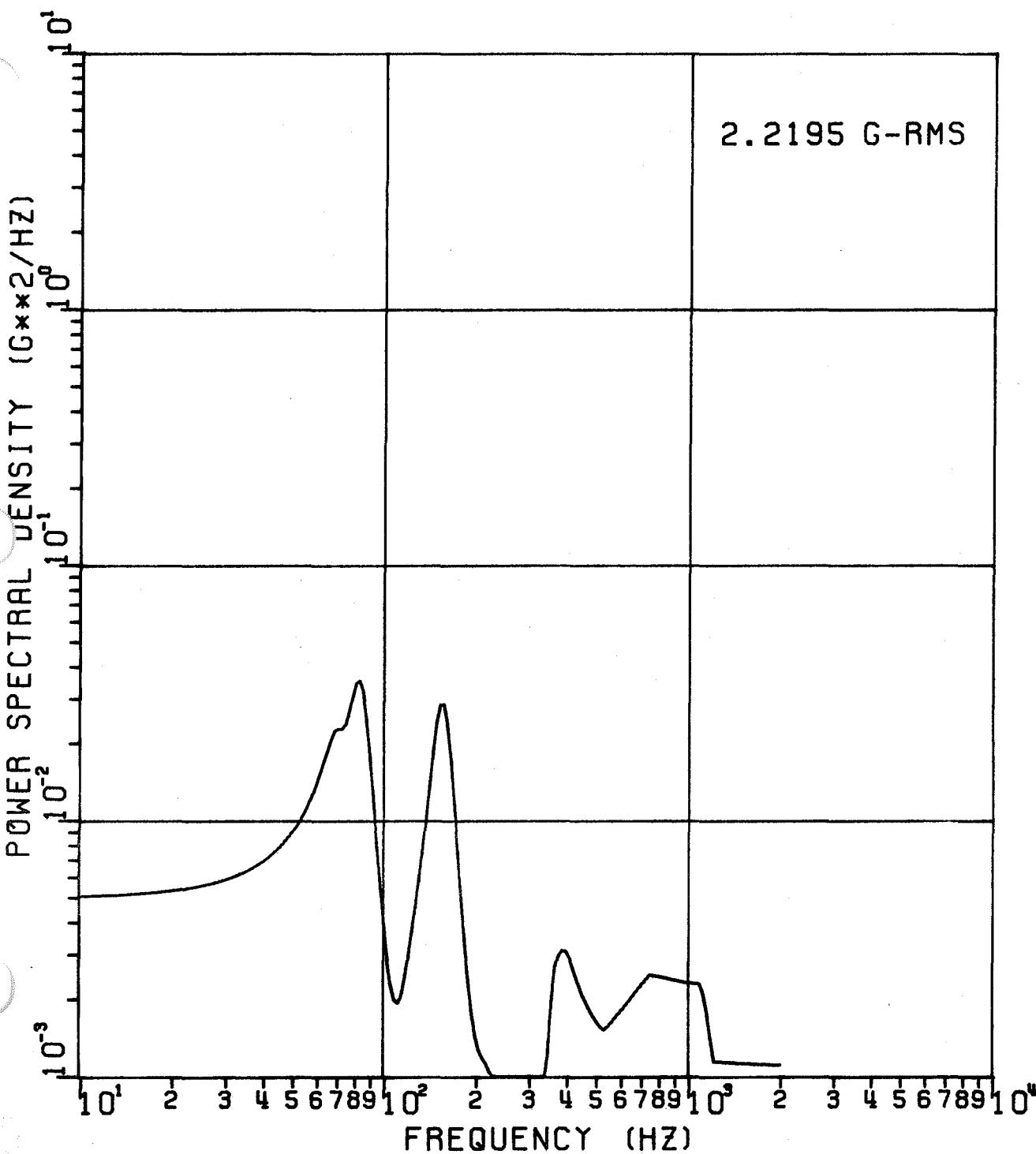
LOCATION 4



1 X AXIS SUBPACK 3 SEP 1970

## FIGURE 13c RANDOM VIBRATION SPECTRUM

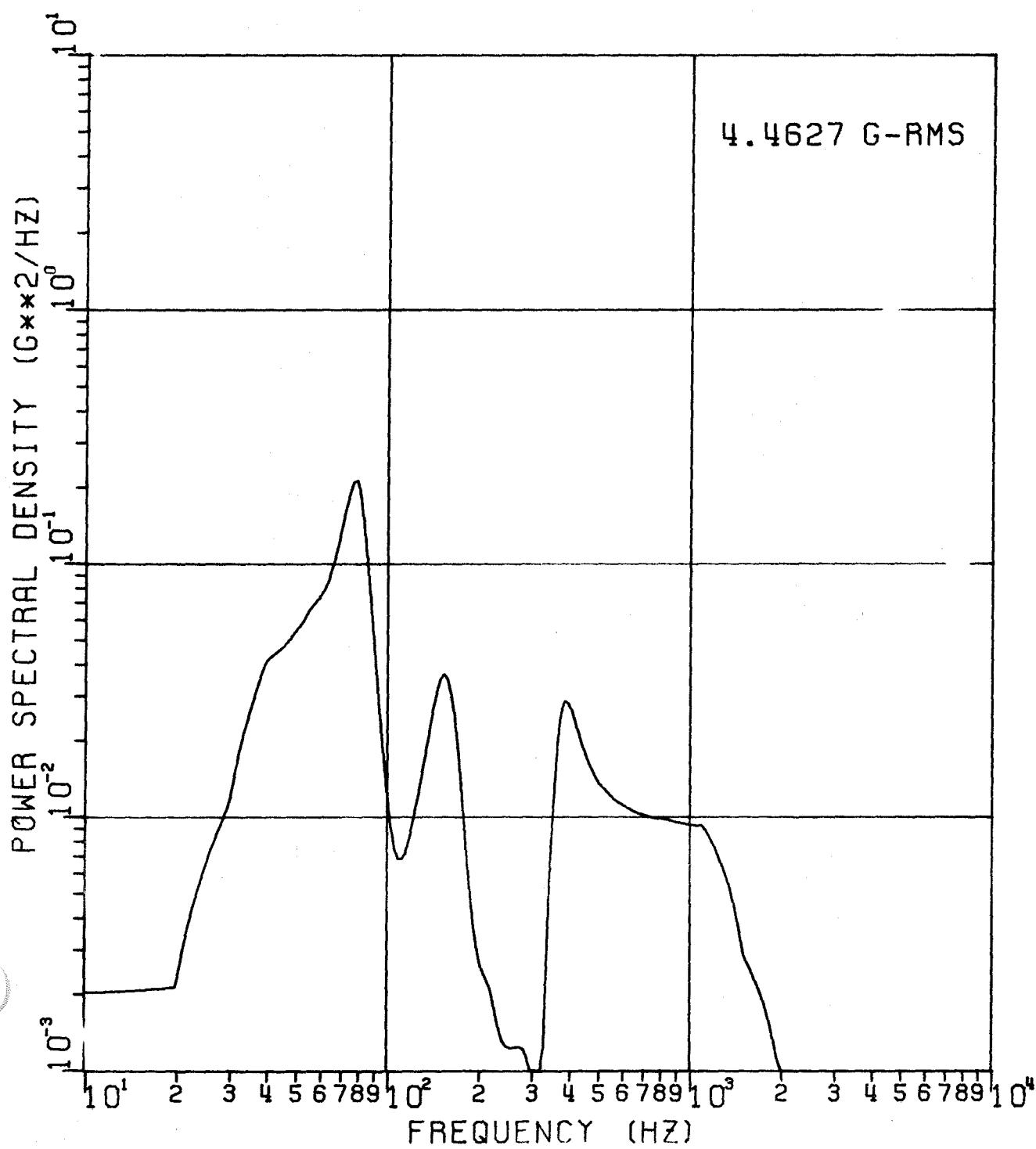
LOCATION 4



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 13d RANDOM VIBRATION SPECTRUM

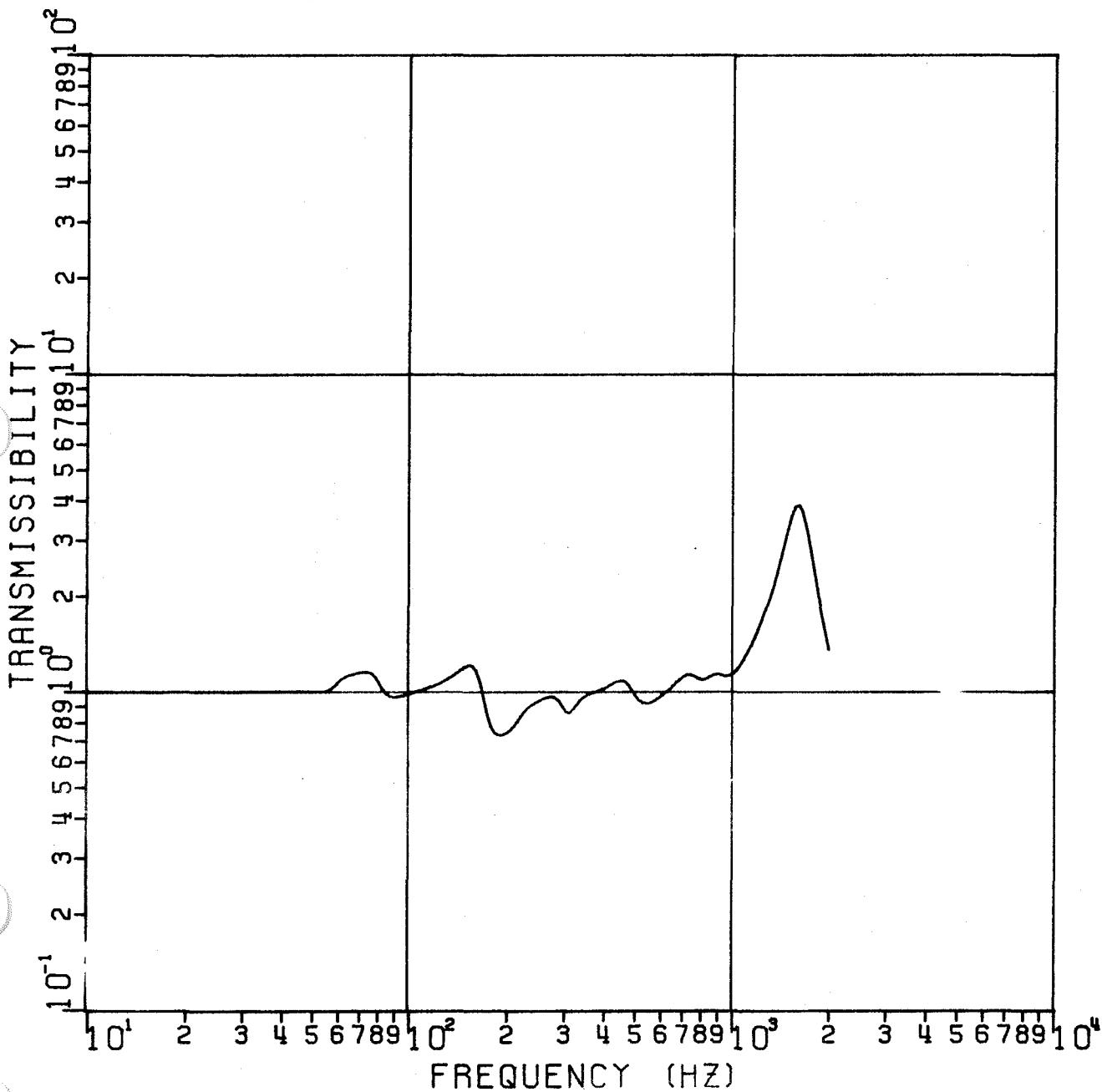
LOCATION 4



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 14a TRANSMISSIBILITY

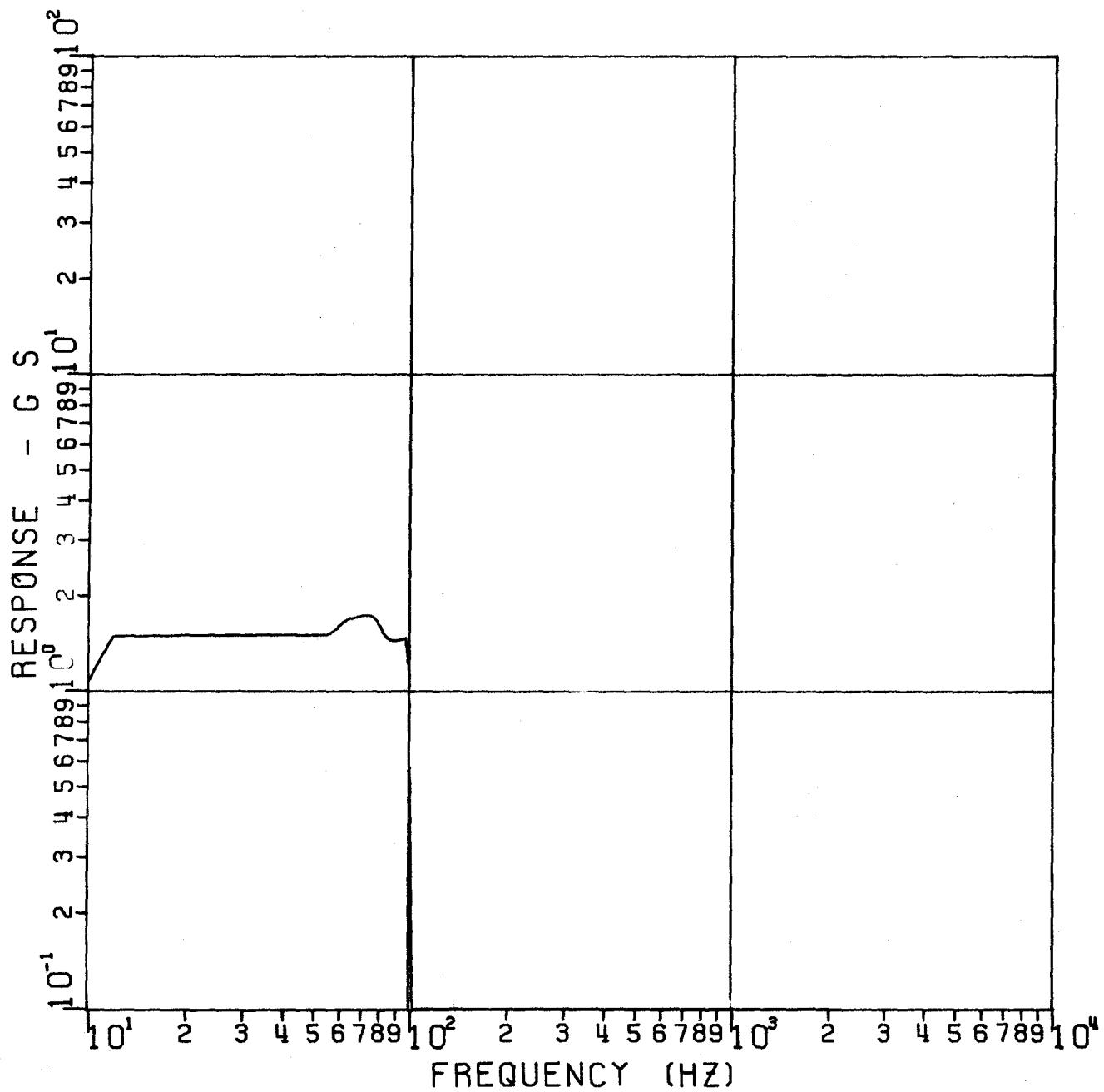
LOCATION 7



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 14b SINE RESPONSE

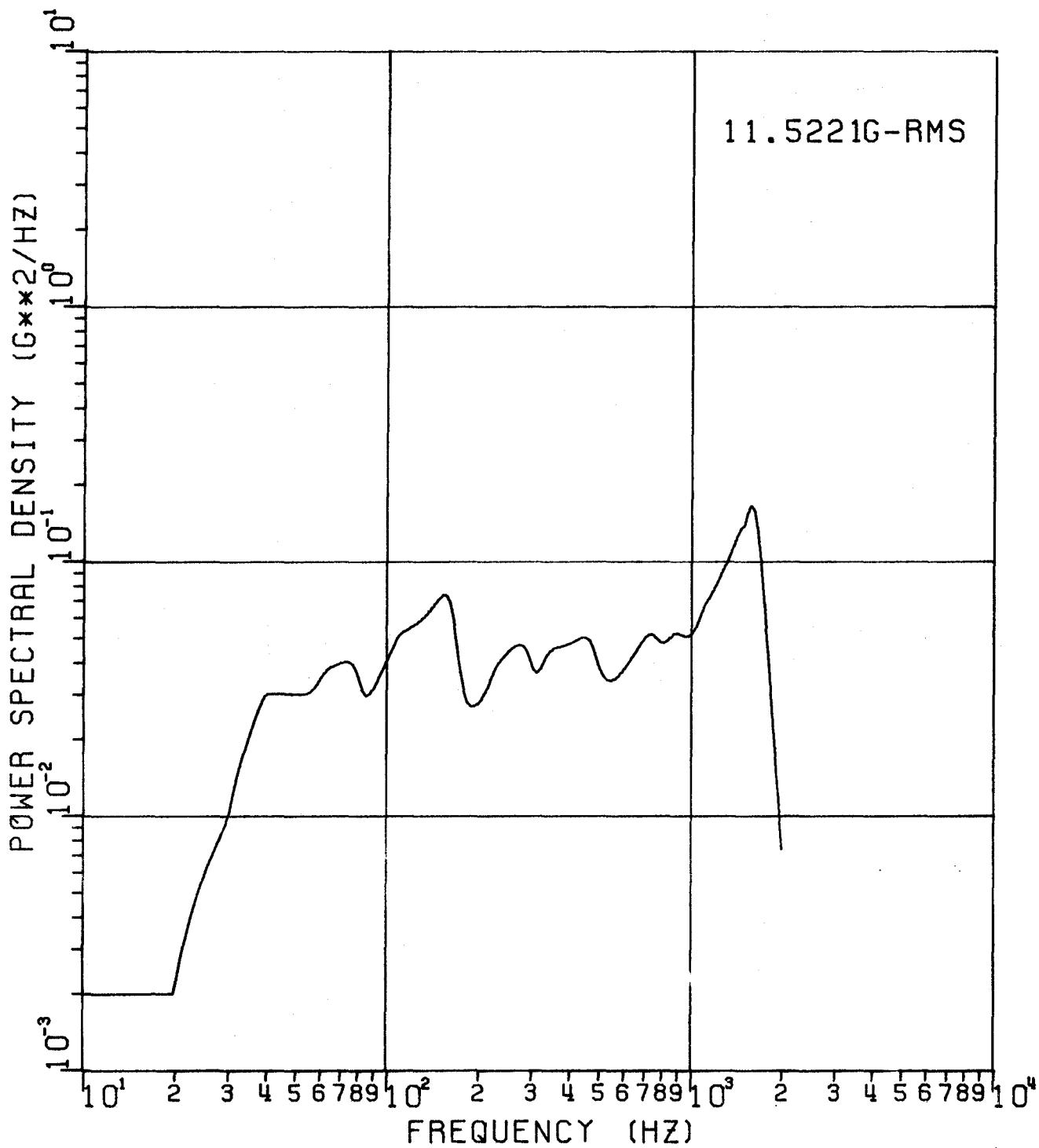
LOCATION 7



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 14C RANDOM VIBRATION SPECTRUM

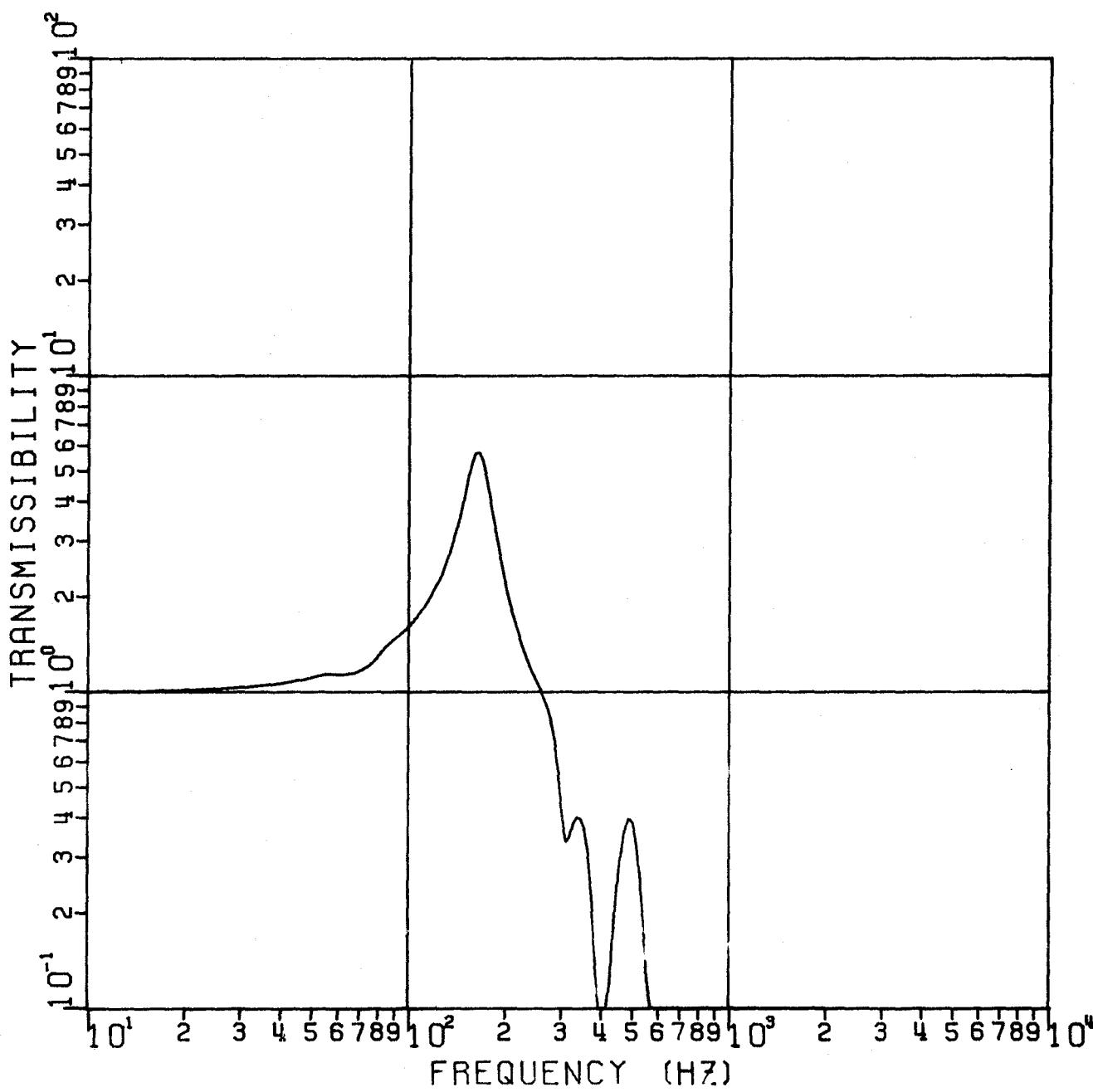
LOCATION 7



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 15a TRANSMISSIBILITY

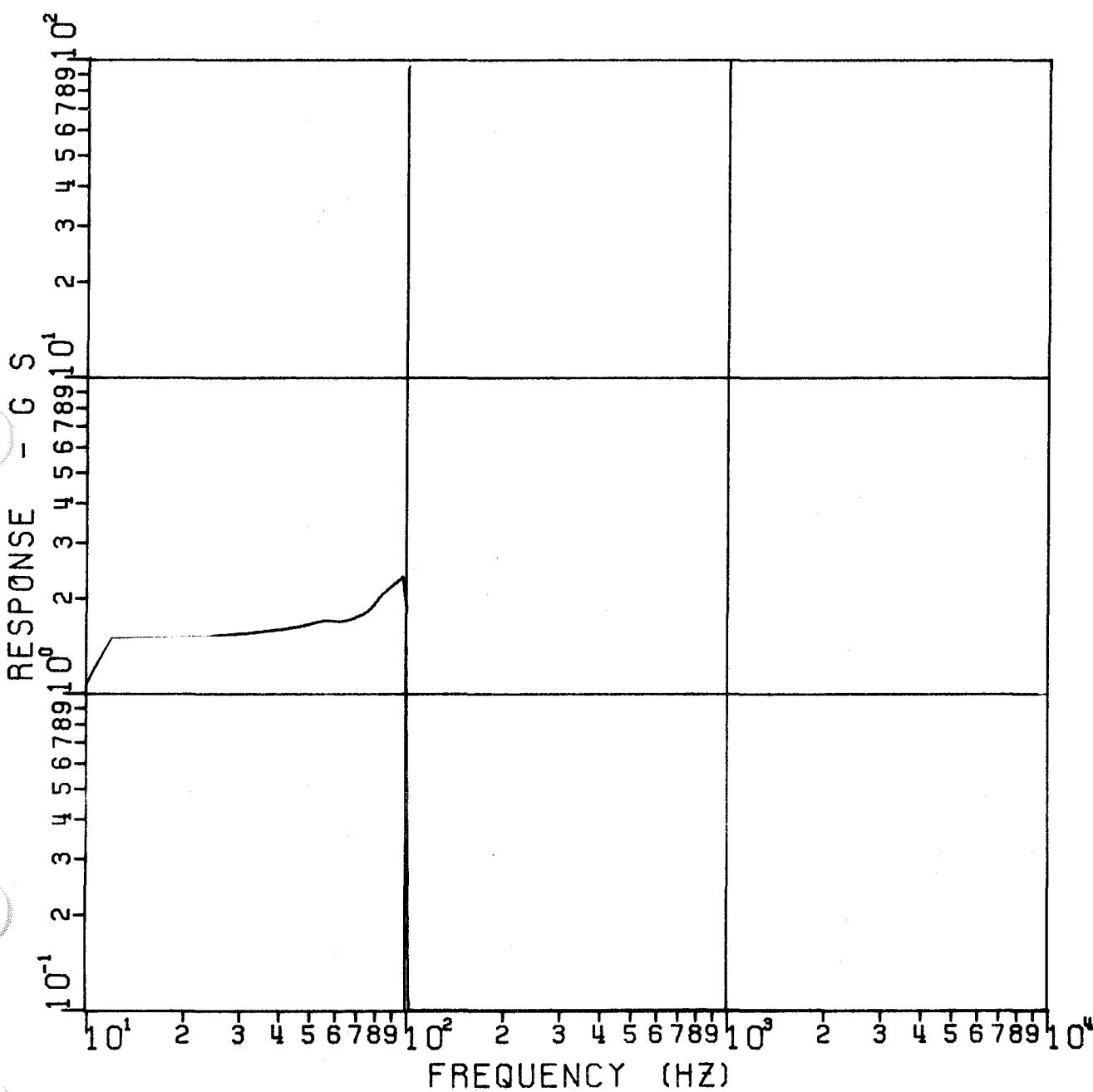
LOCATION 10



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 15b SINE RESPONSE

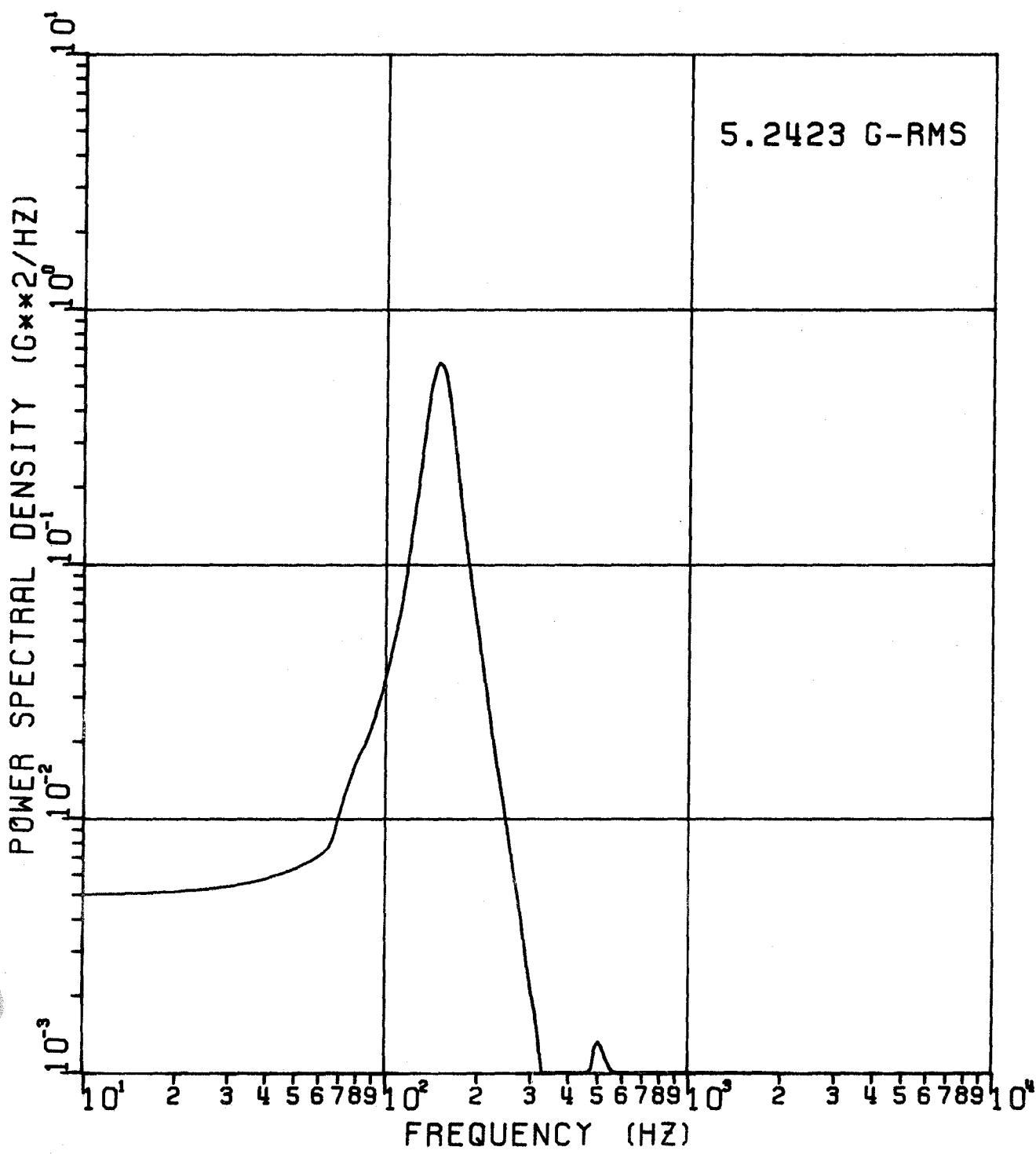
LOCATION 10



1 X AXIS SUBPACK 3 SEP 1970

## FIGURE 15c RANDOM VIBRATION SPECTRUM

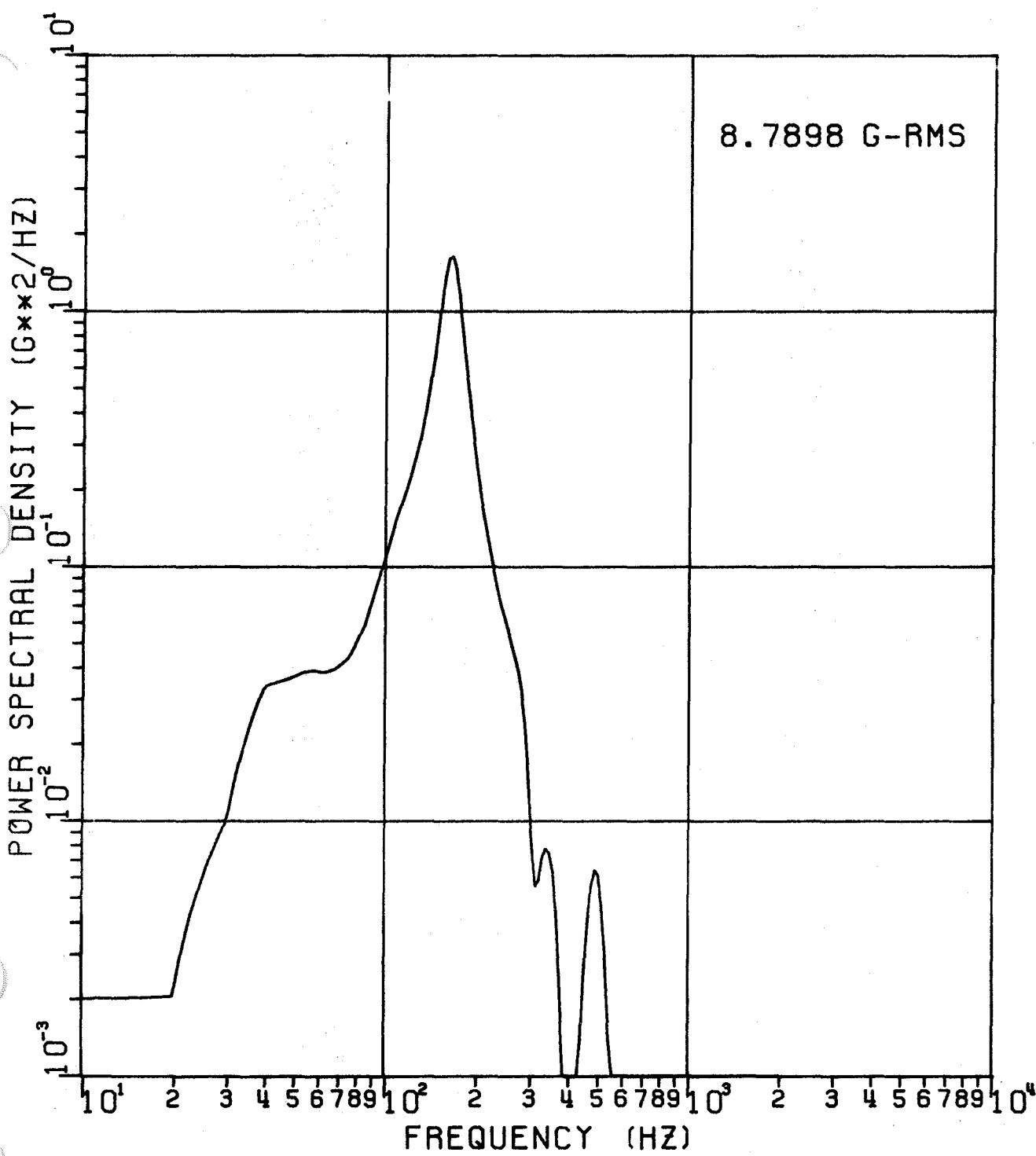
LOCATION 10



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 15d RANDOM VIBRATION SPECTRUM

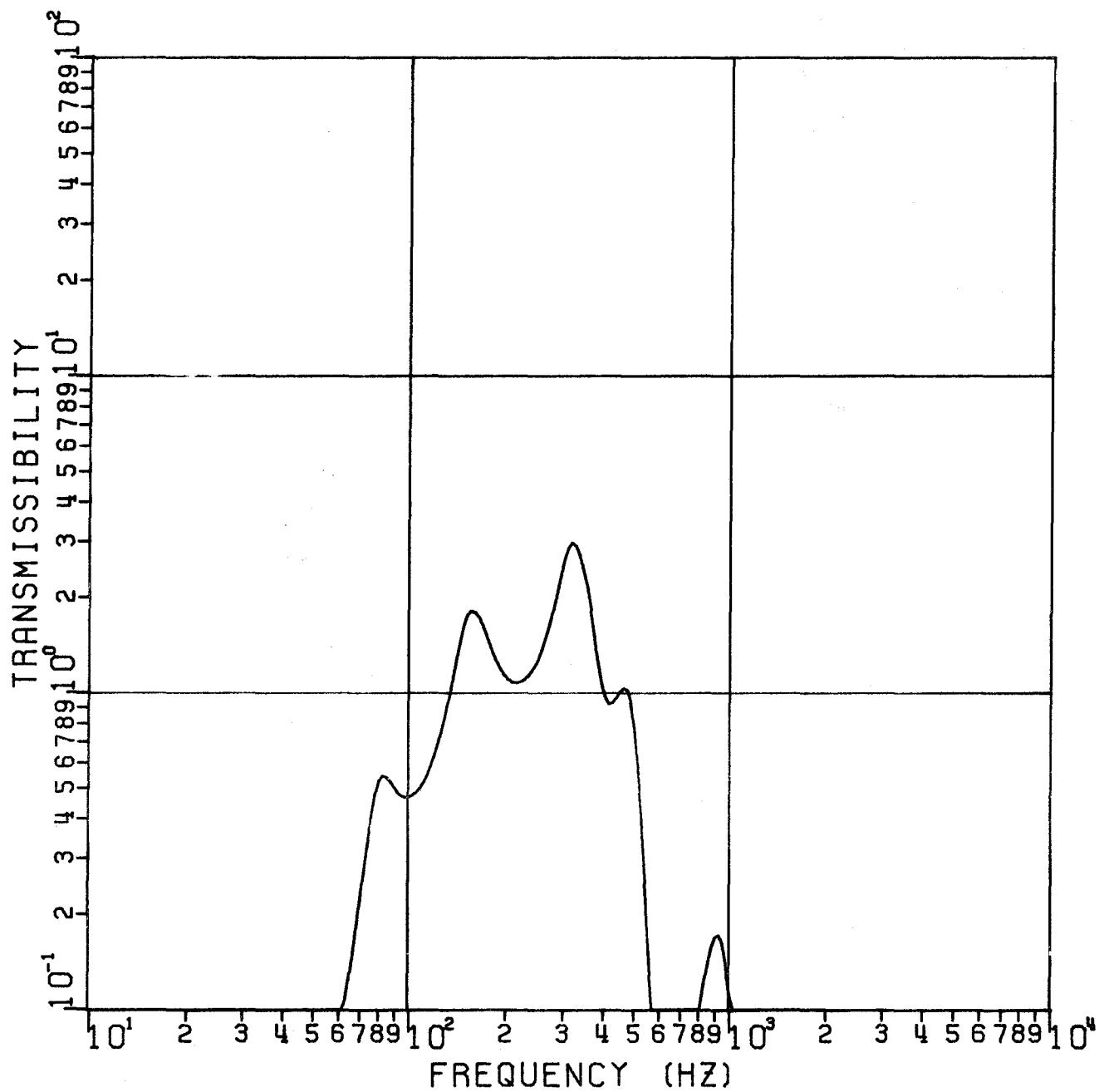
LOCATION 10



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 16a TRANSMISSIBILITY

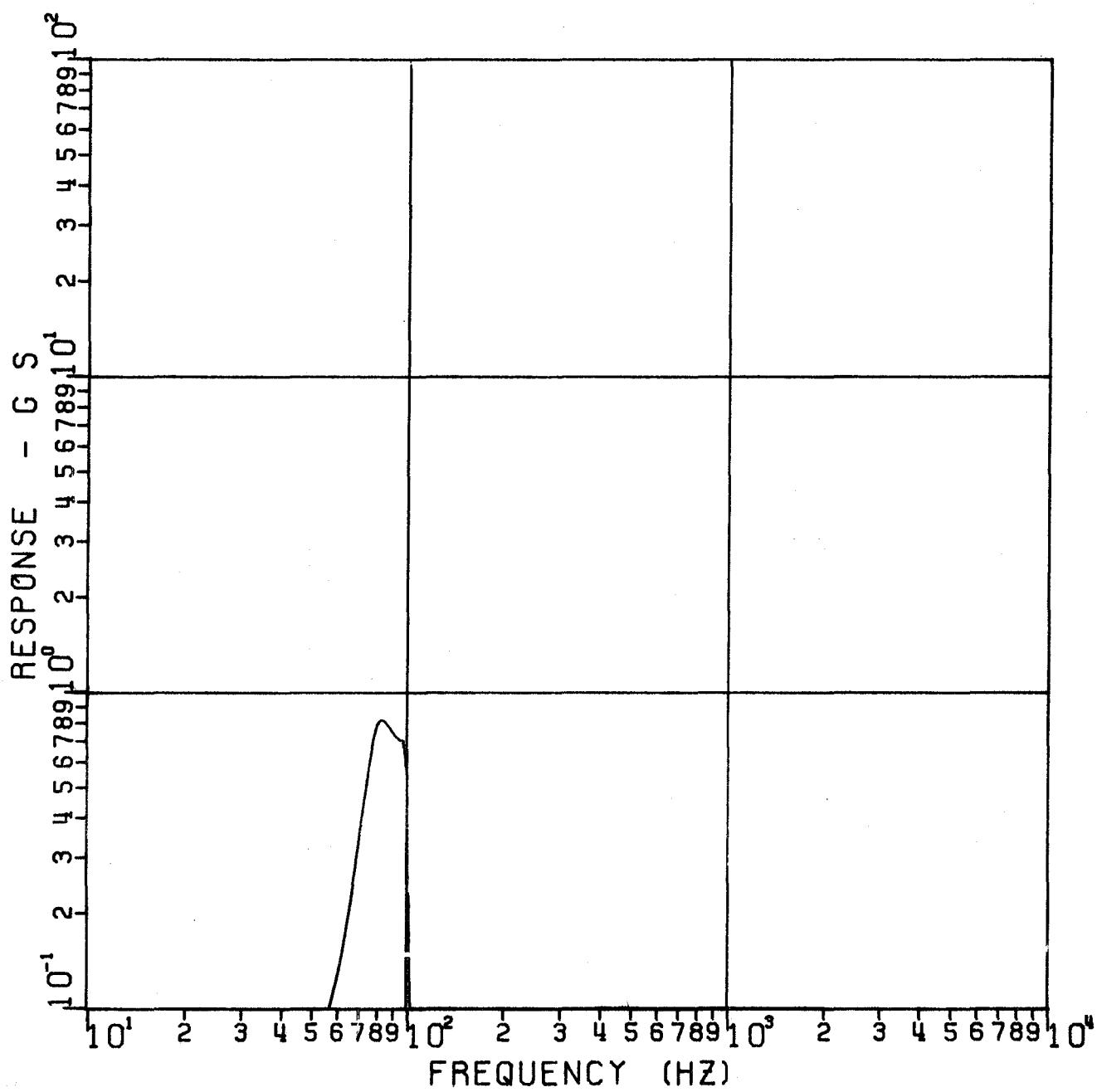
LOCATION 13



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 16 b SINE RESPONSE

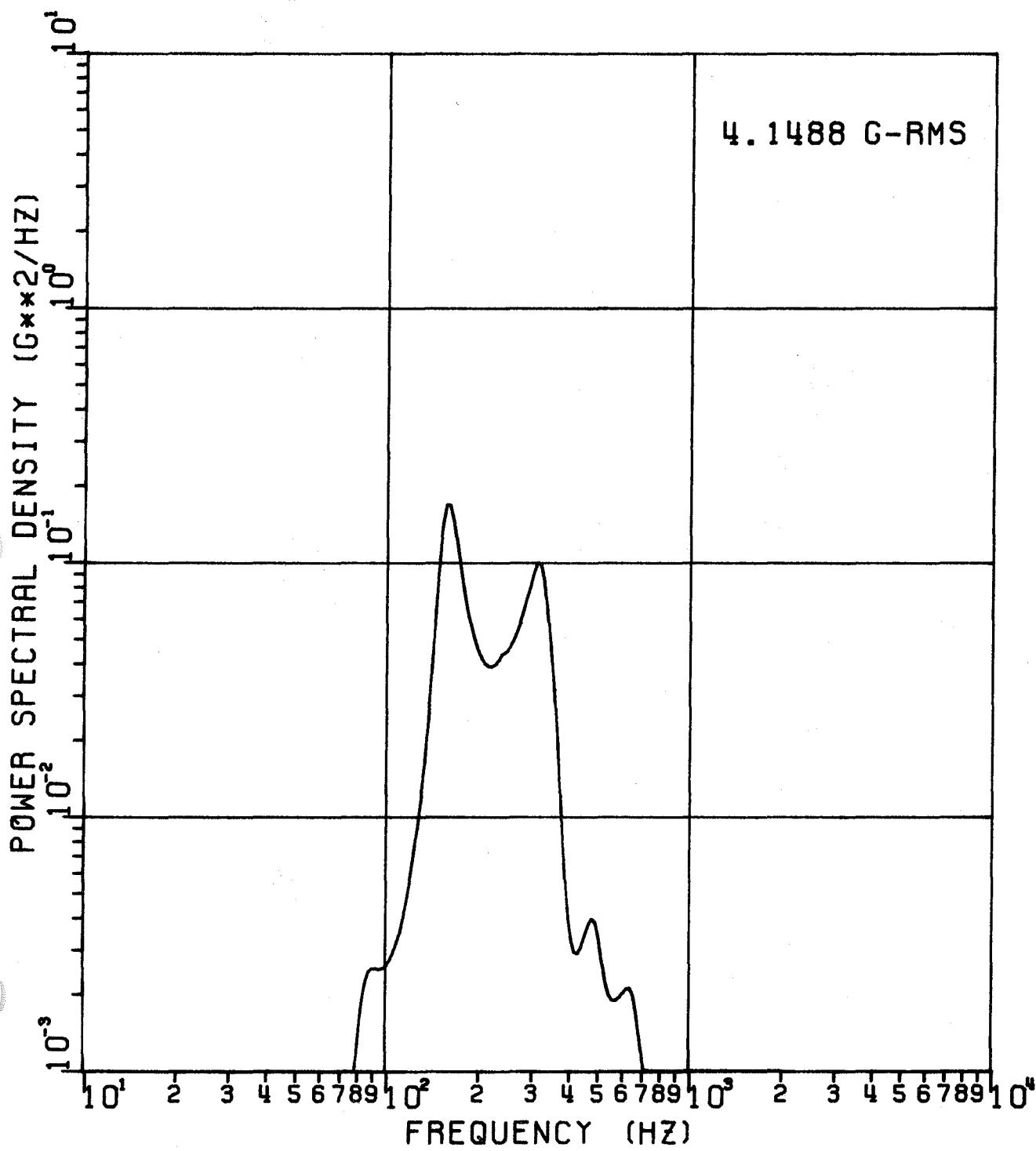
LOCATION 13



1 X AXIS SUBPACK 3 SEP 1970

## FIGURE 16c RANDOM VIBRATION SPECTRUM

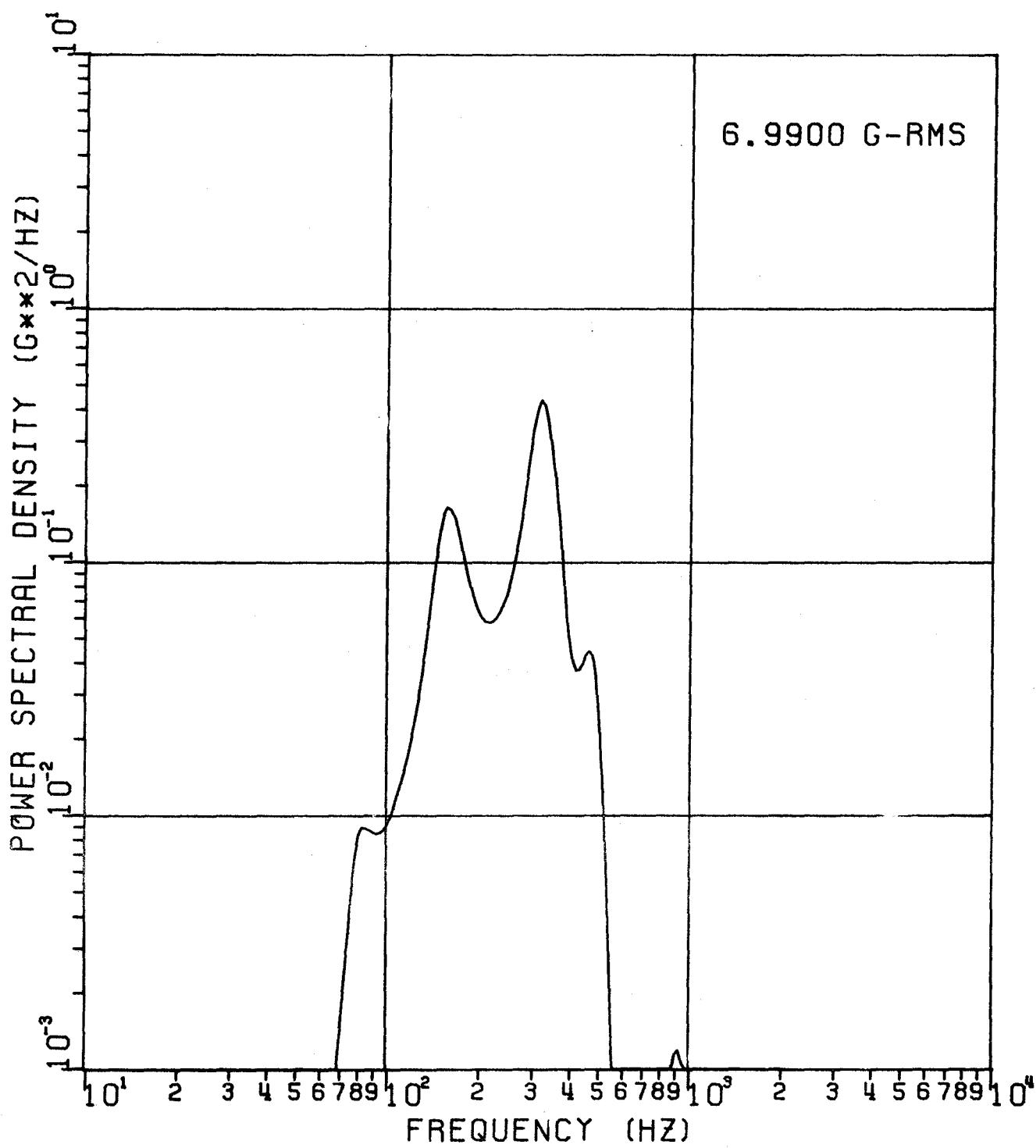
LOCATION 13



1 X AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 16d RANDOM VIBRATION SPECTRUM

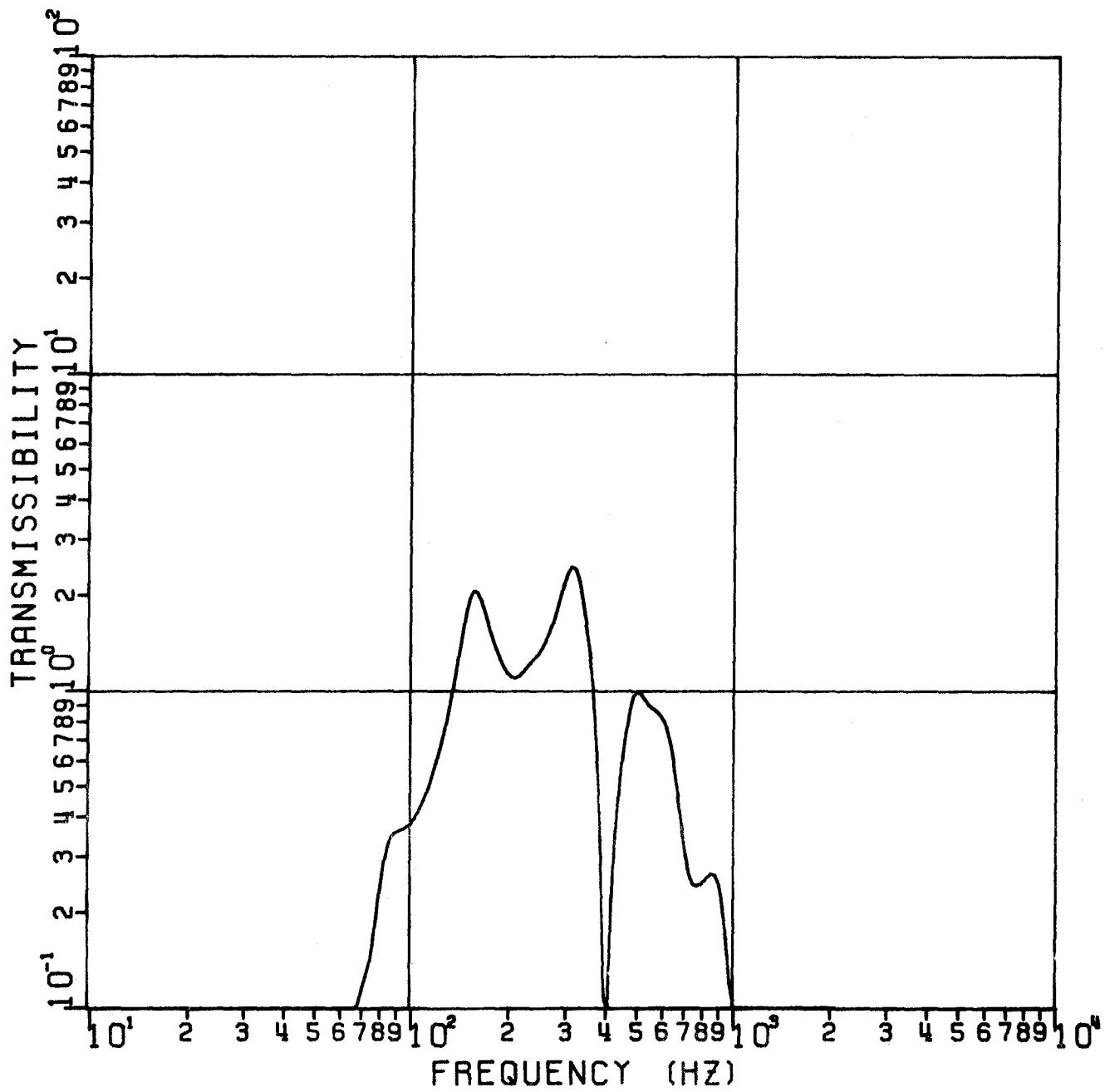
LOCATION 13



1 X AXIS SUBPACK 3 SEP 1970

FIGURE 17a TRANSMISSIBILITY

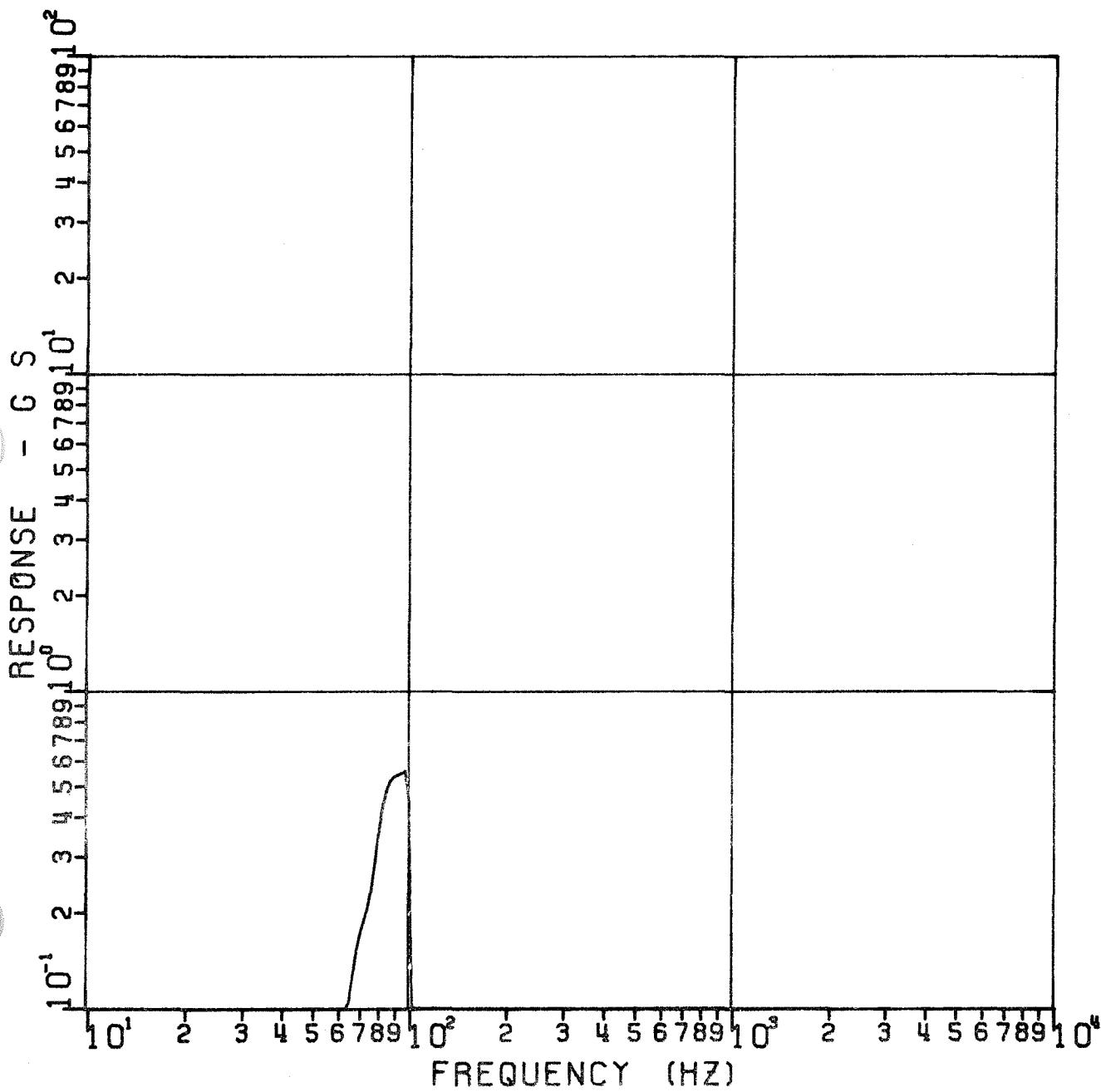
LOCATION 14



1 X AXIS SUBPACK 3 SEP 1970

FIGURE 17b SINE RESPONSE

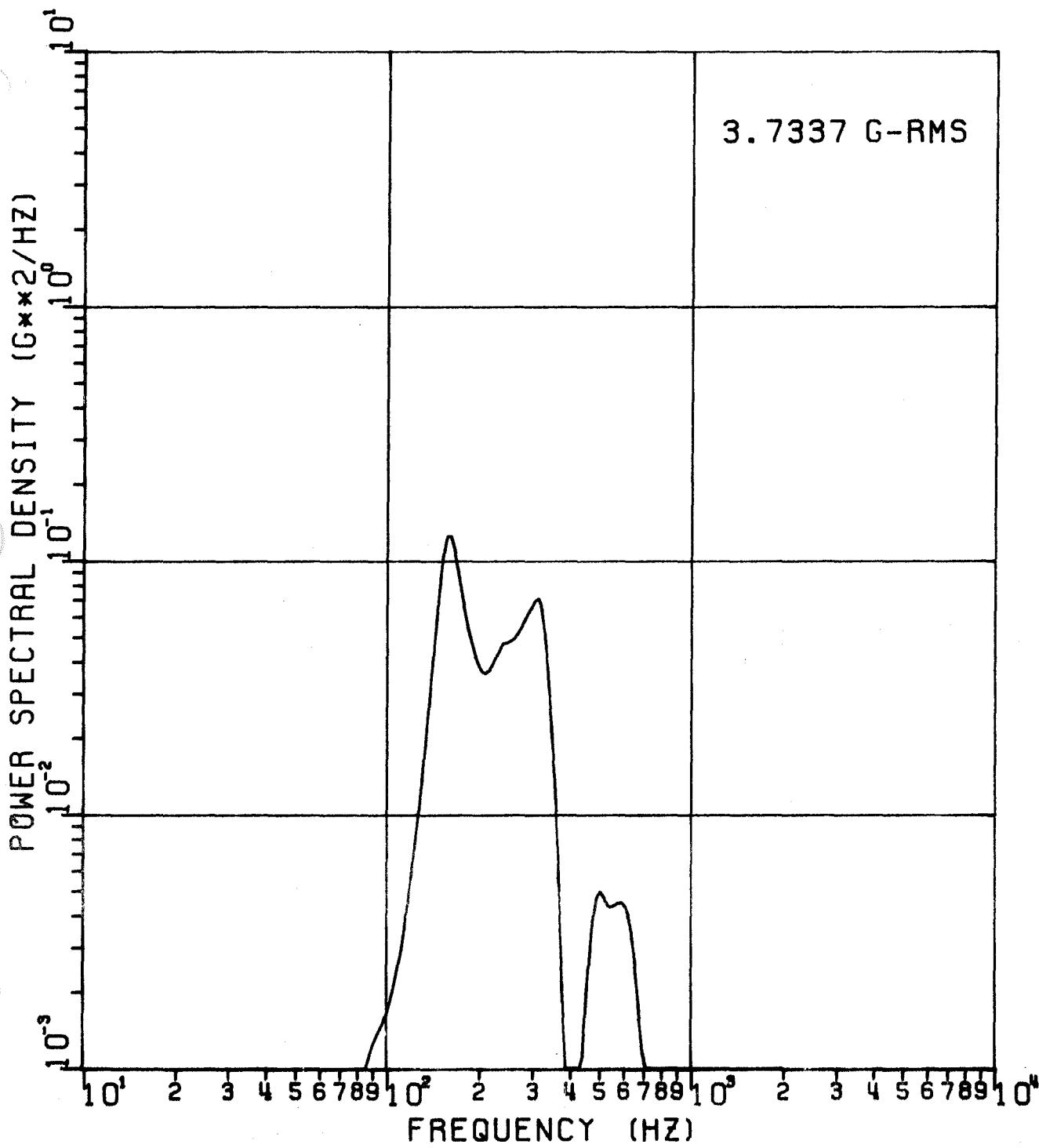
LOCATION 14



1 X AXIS SUBPACK 3 SEP 1970

## FIGURE 17c RANDOM VIBRATION SPECTRUM

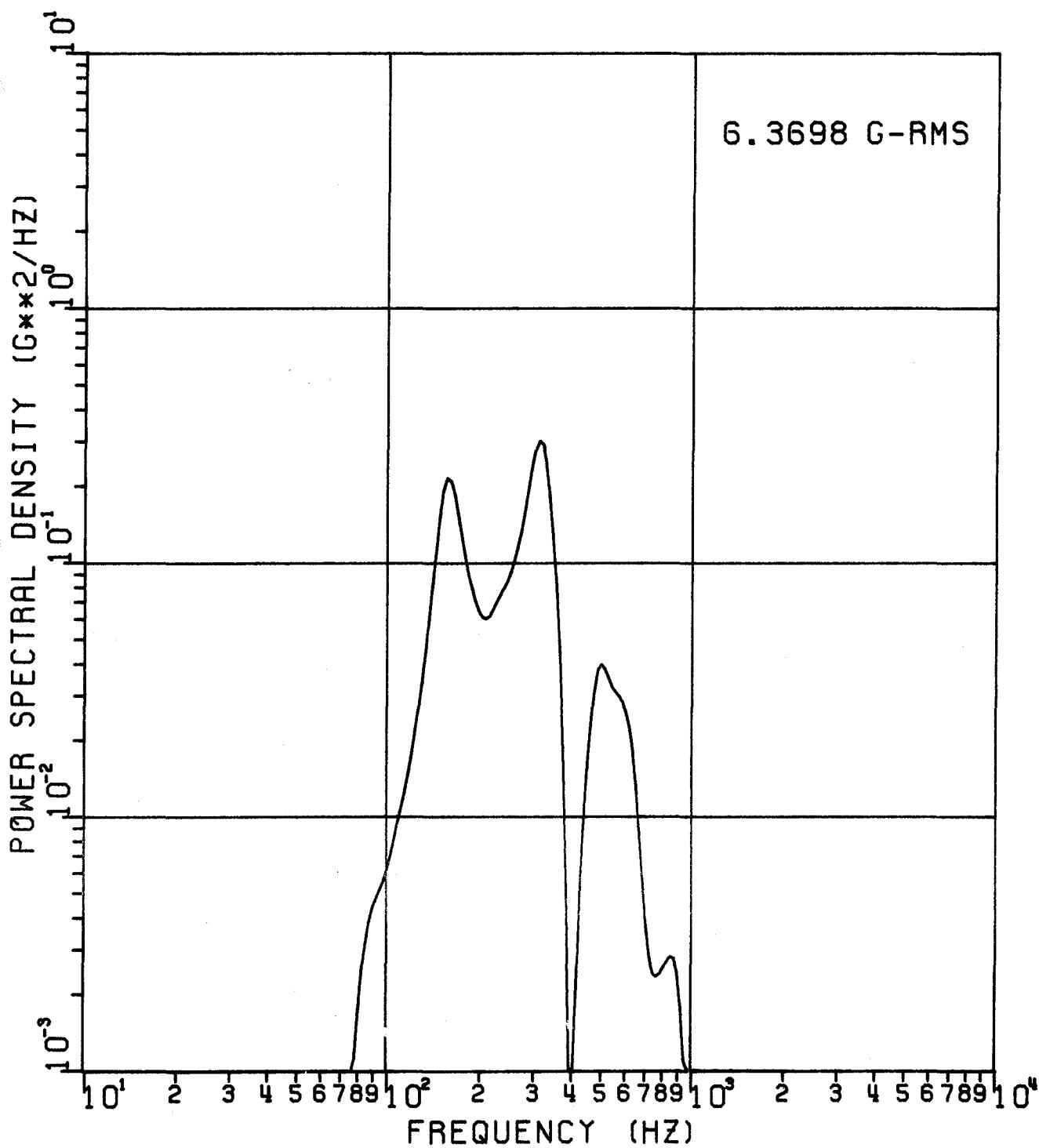
LOCATION 14



1 X AXIS SUBP. 3 SEP 70 NEW LEVELS

## FIGURE 17d RANDOM VIBRATION SPECTRUM

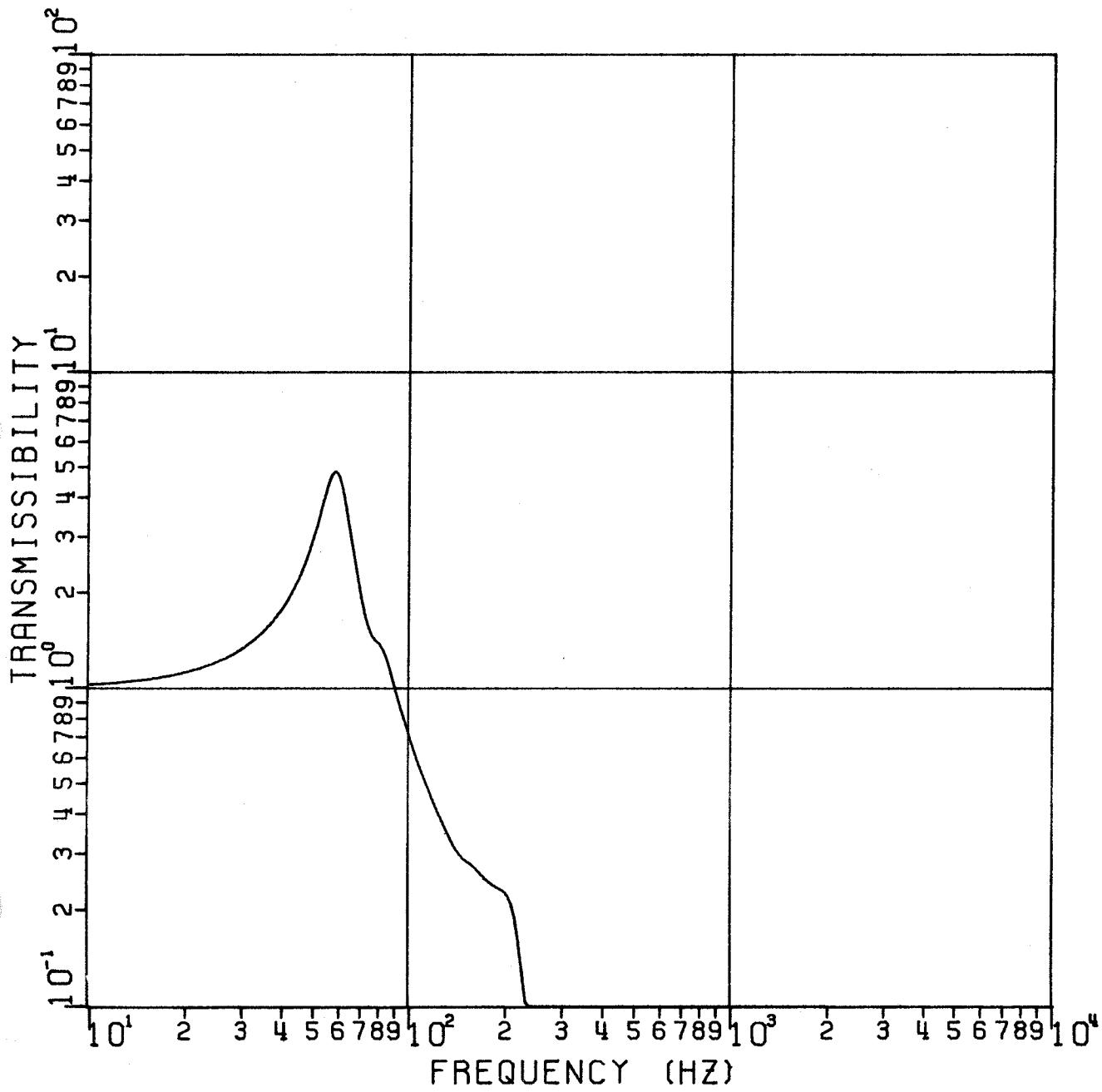
LOCATION 14



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 18 a TRANSMISSIBILITY

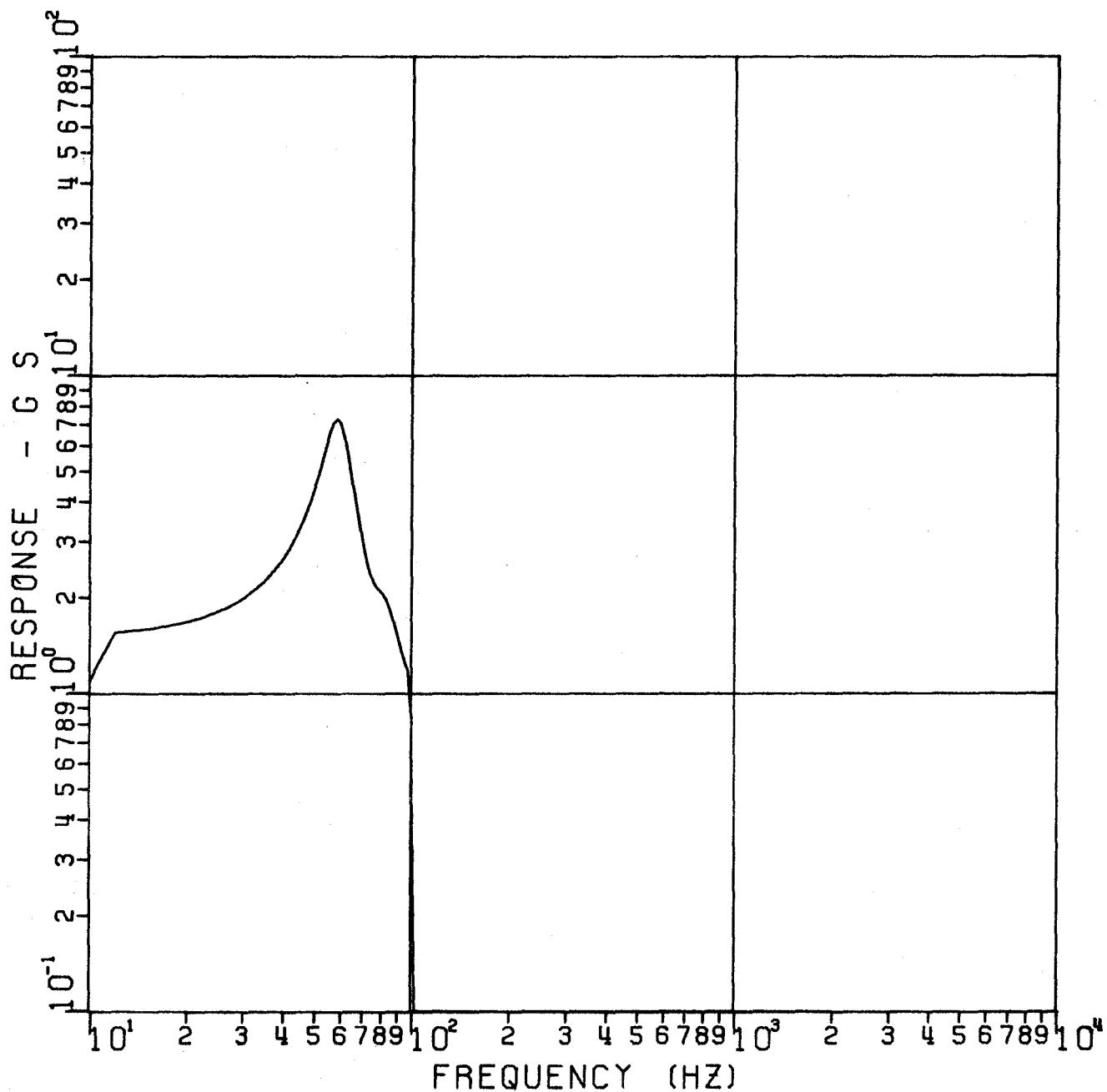
LOCATION 2



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 18b SINE RESPONSE

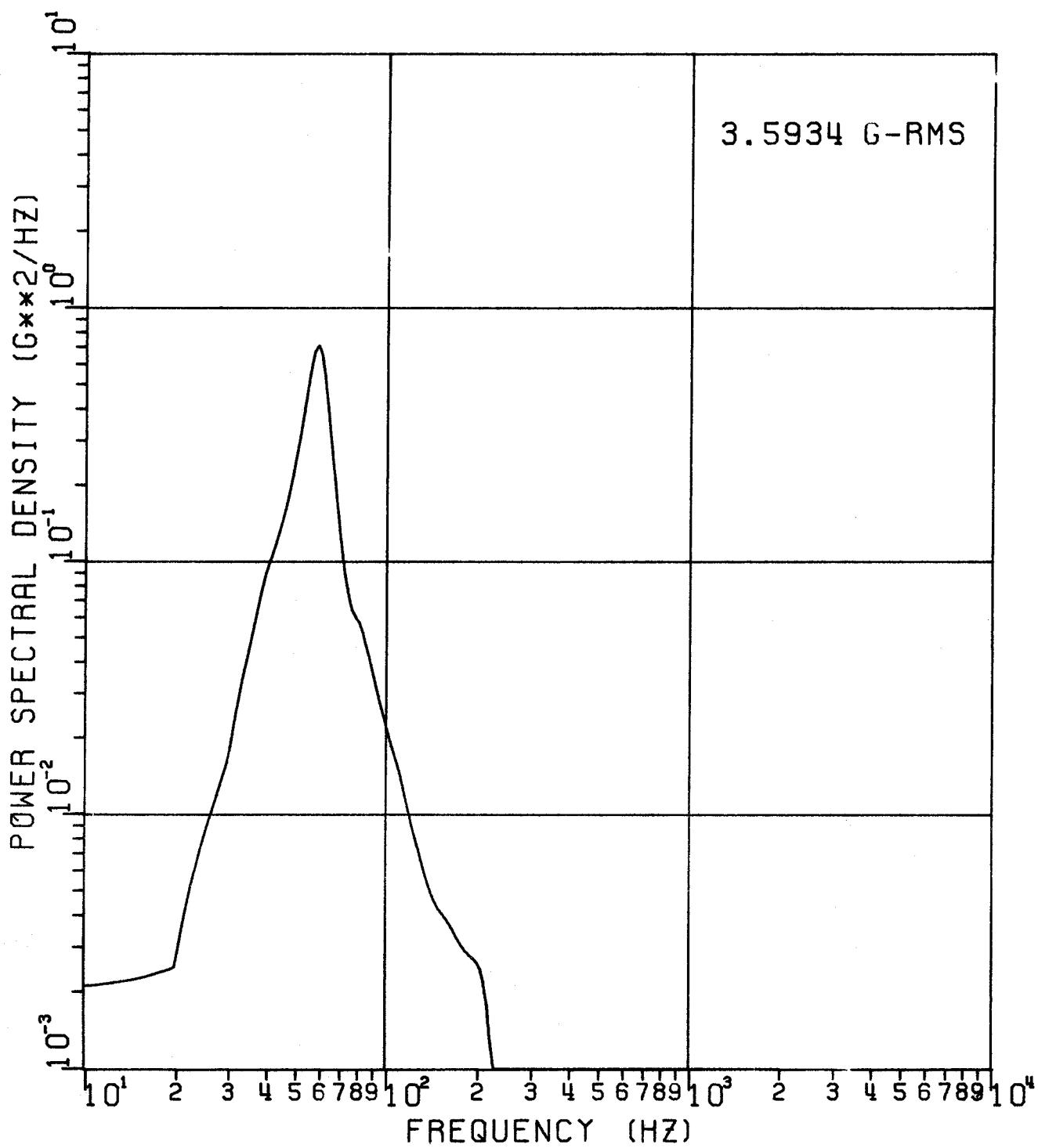
LOCATION 2



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

## FIGURE 18c RANDOM VIBRATION SPECTRUM

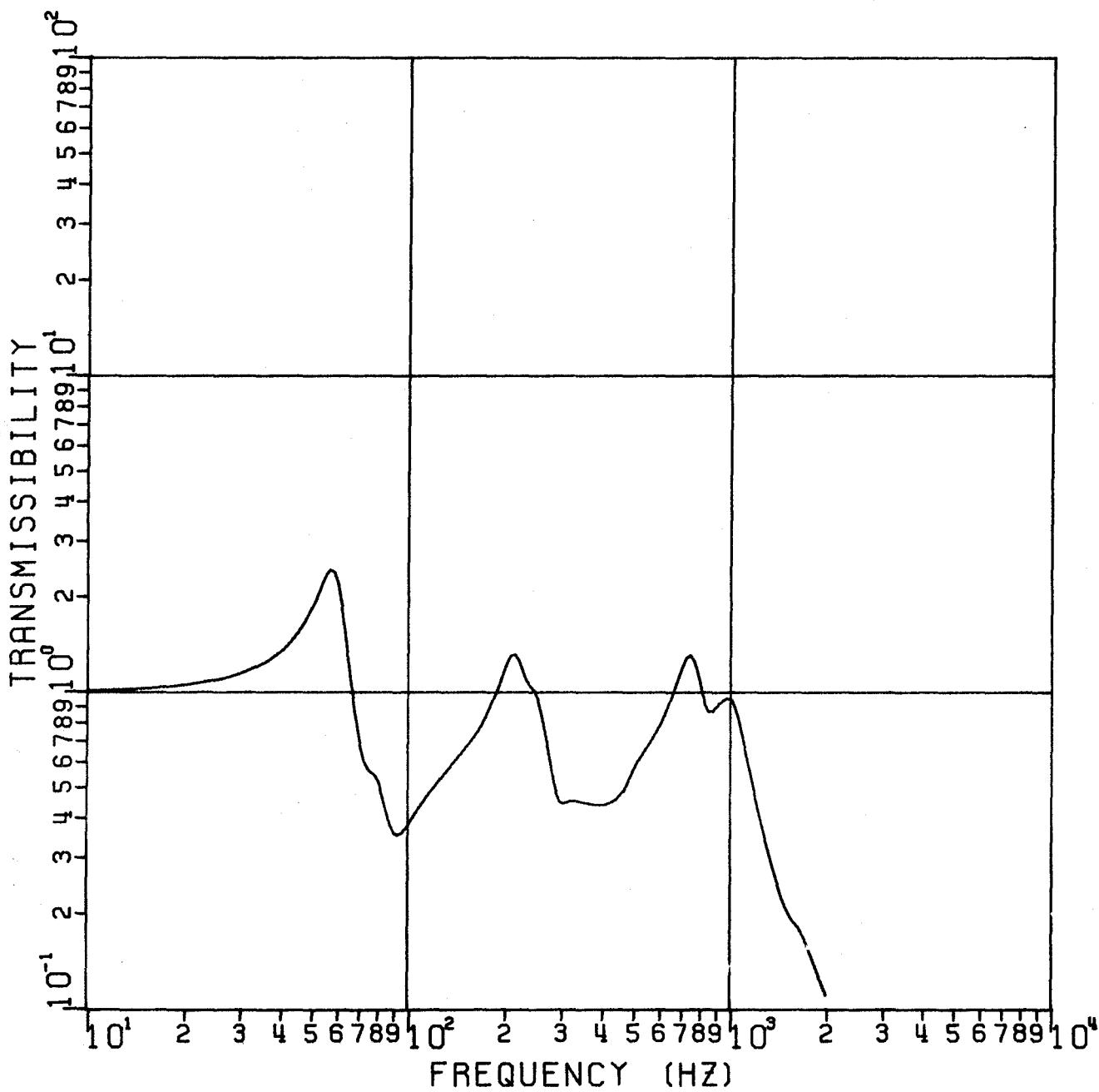
LOCATION 2



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 19a TRANSMISSIBILITY

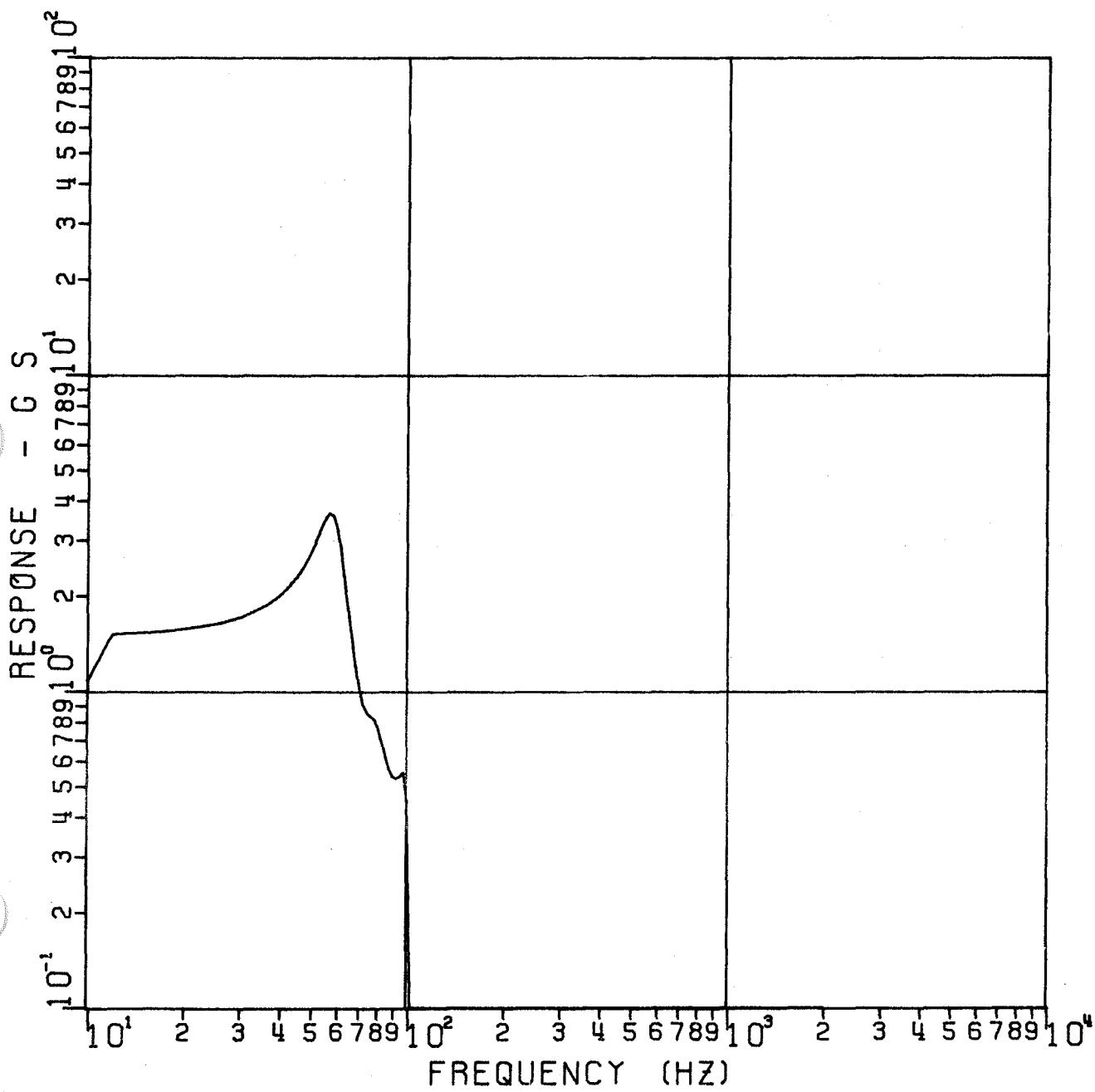
LOCATION 8



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 19 b SINE RESPONSE

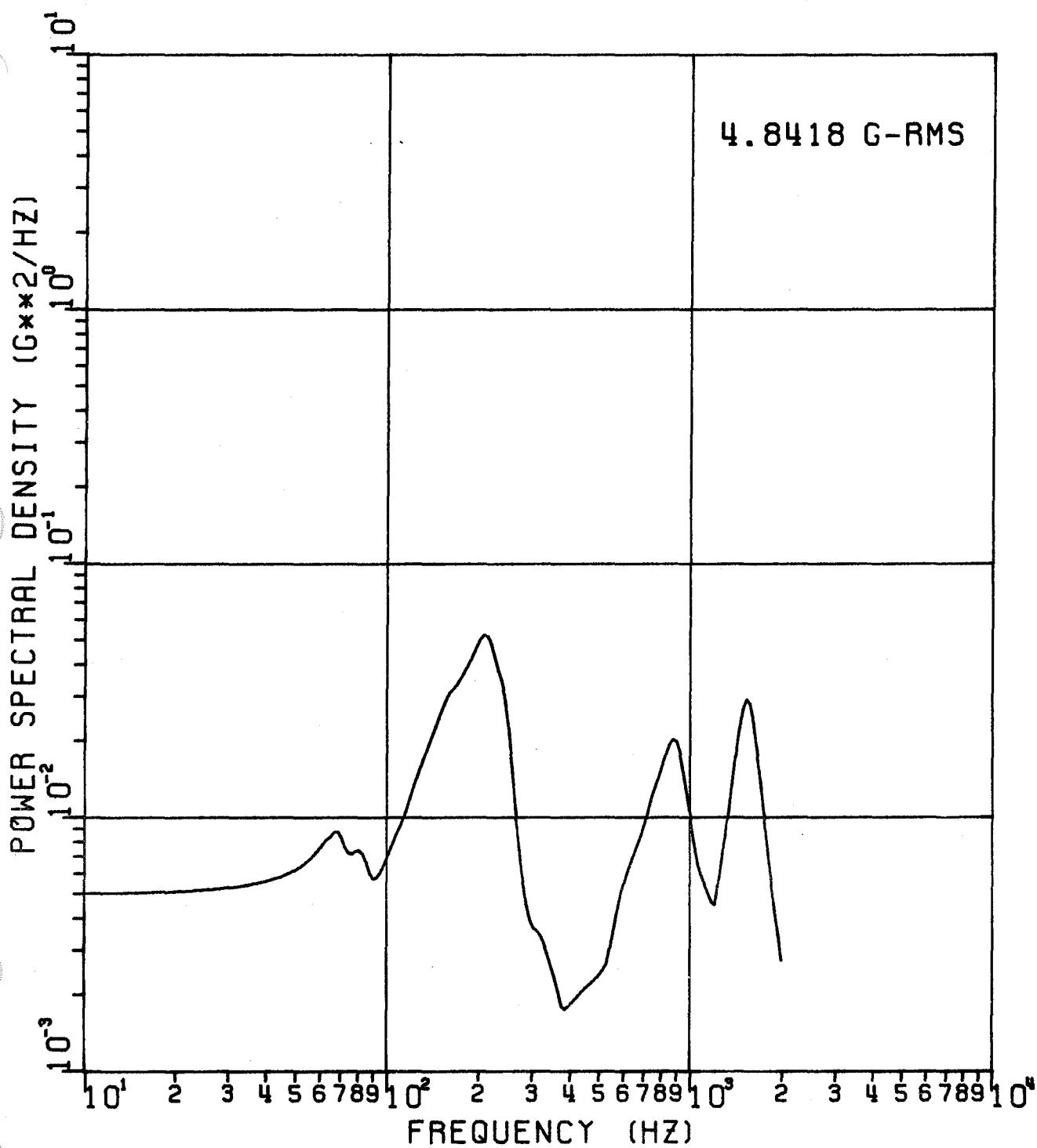
LOCATION 8



1 Y AXIS SUBPACK 3 SEP 1970

## FIGURE 19c RANDOM VIBRATION SPECTRUM

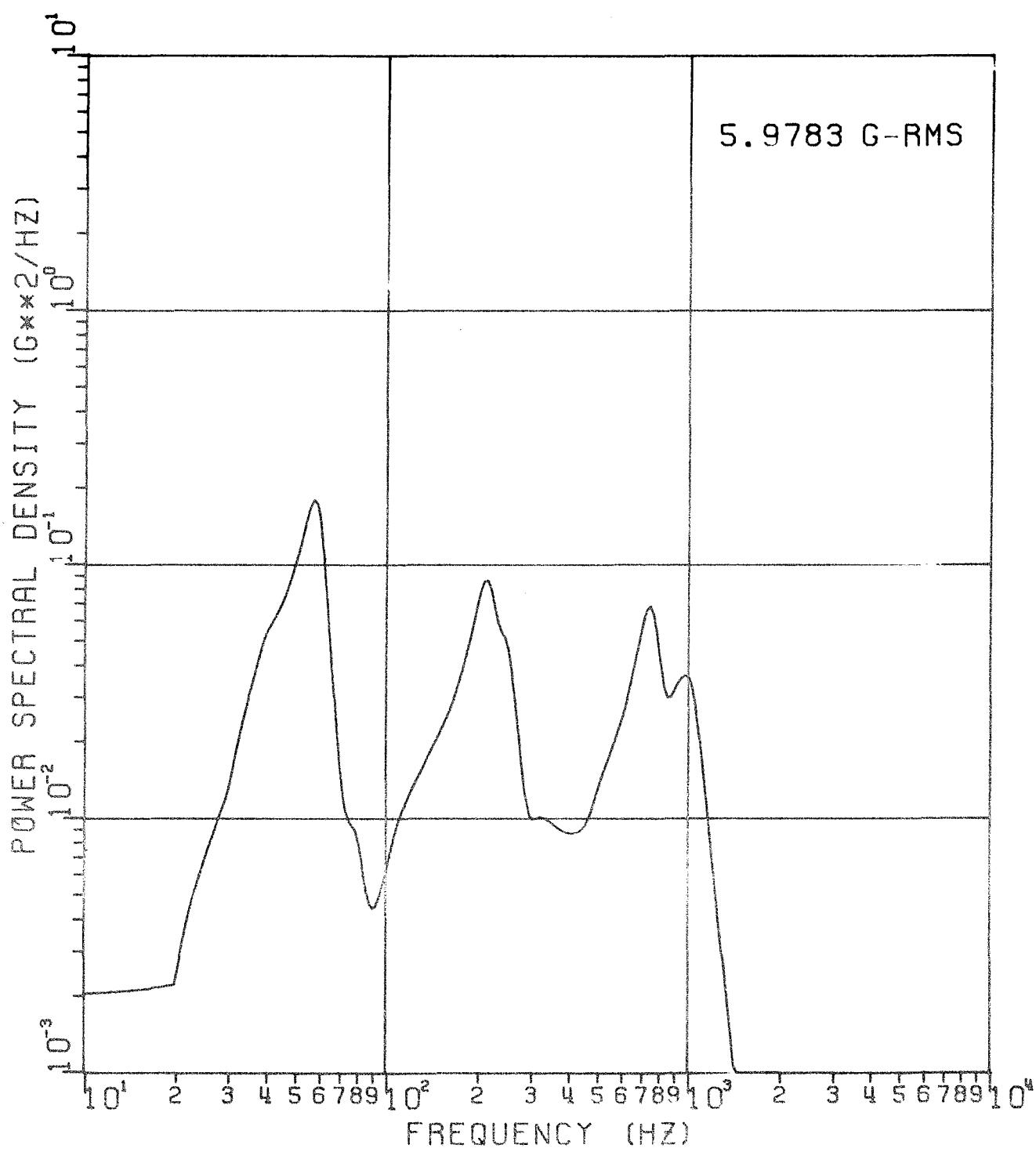
LOCATION 8



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 19d RANDOM VIBRATION SPECTRUM

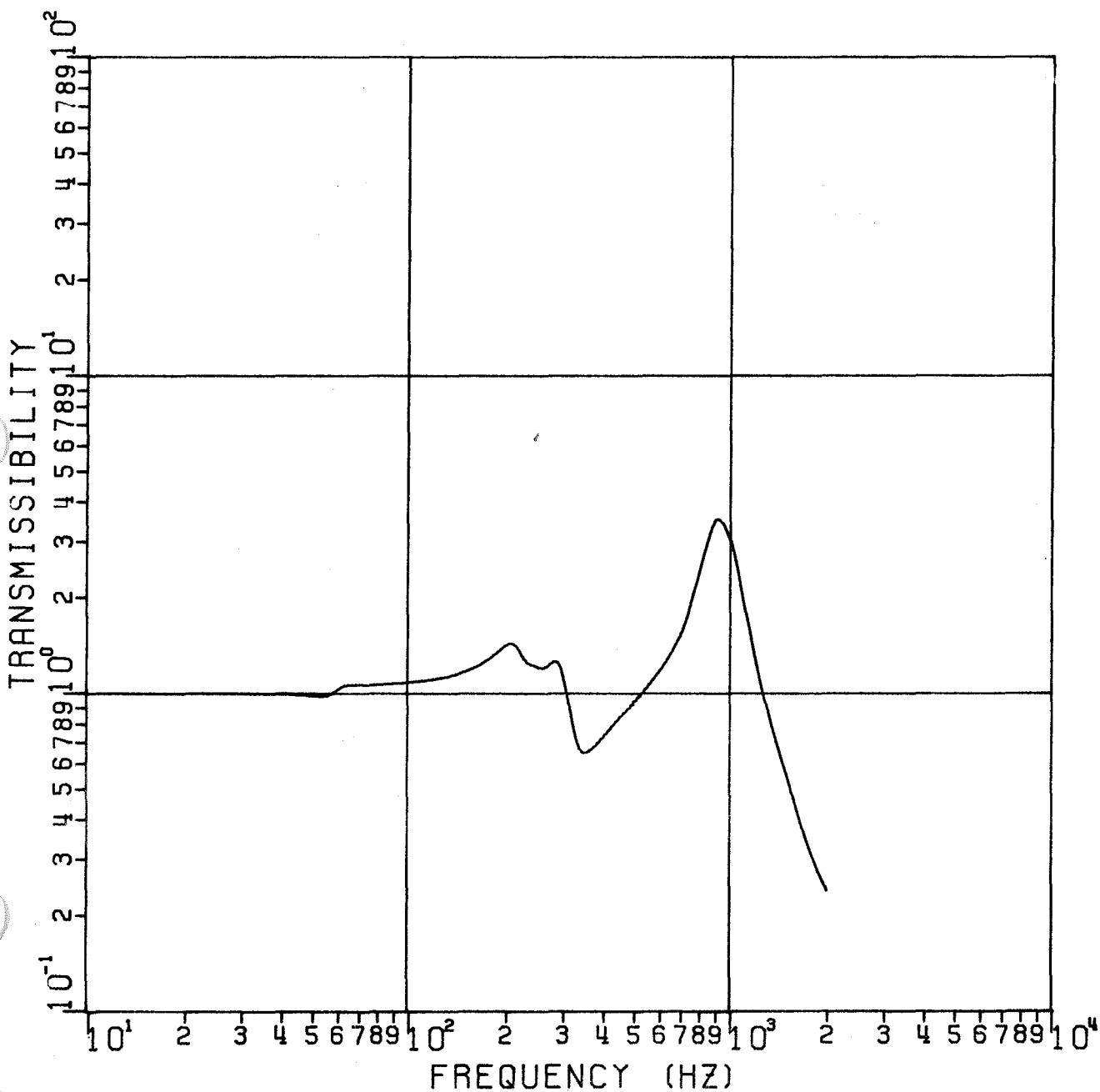
LOCATION 8



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 20a TRANSMISSIBILITY

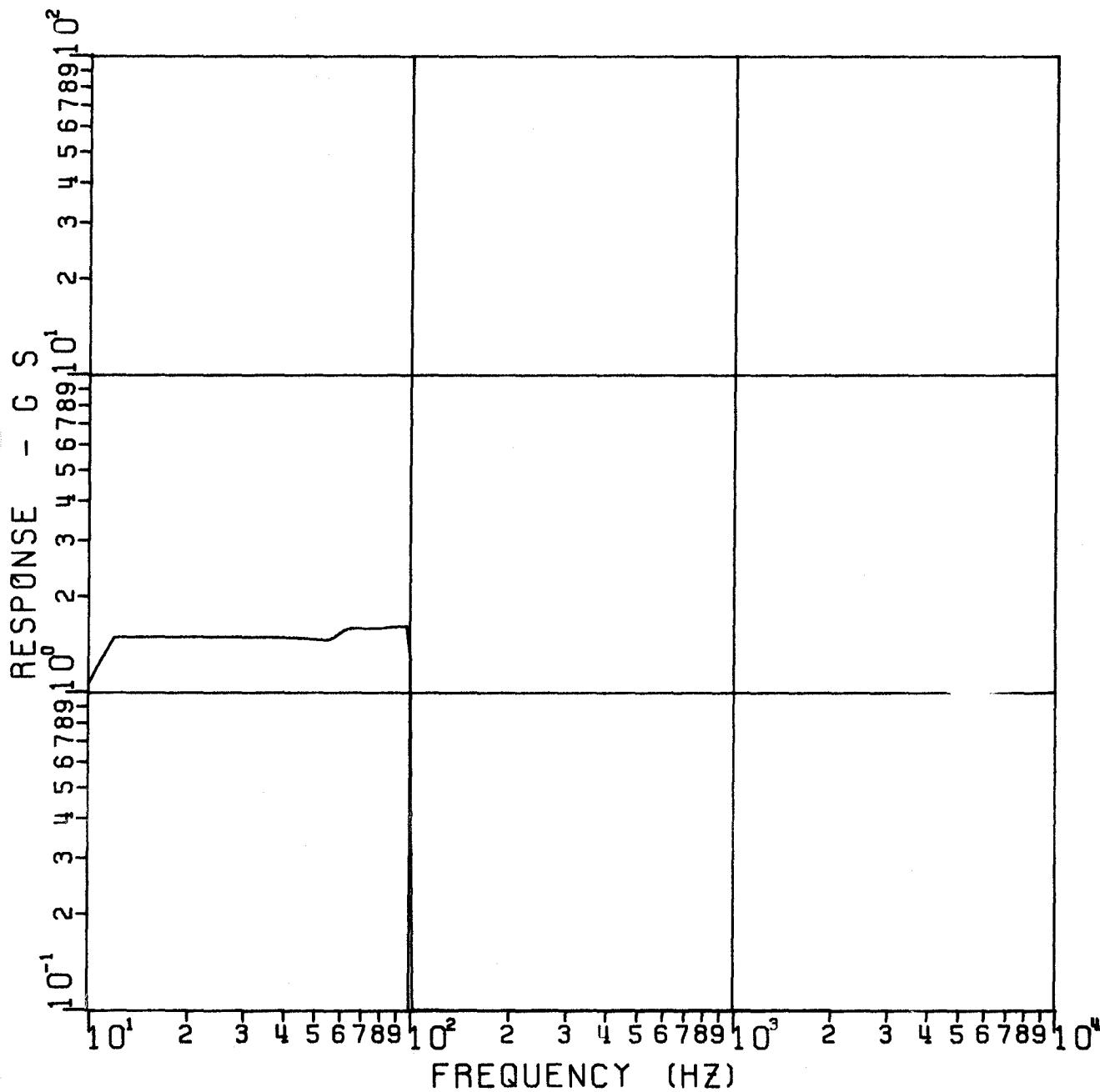
LOCATION 9



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 20b SINE RESPONSE

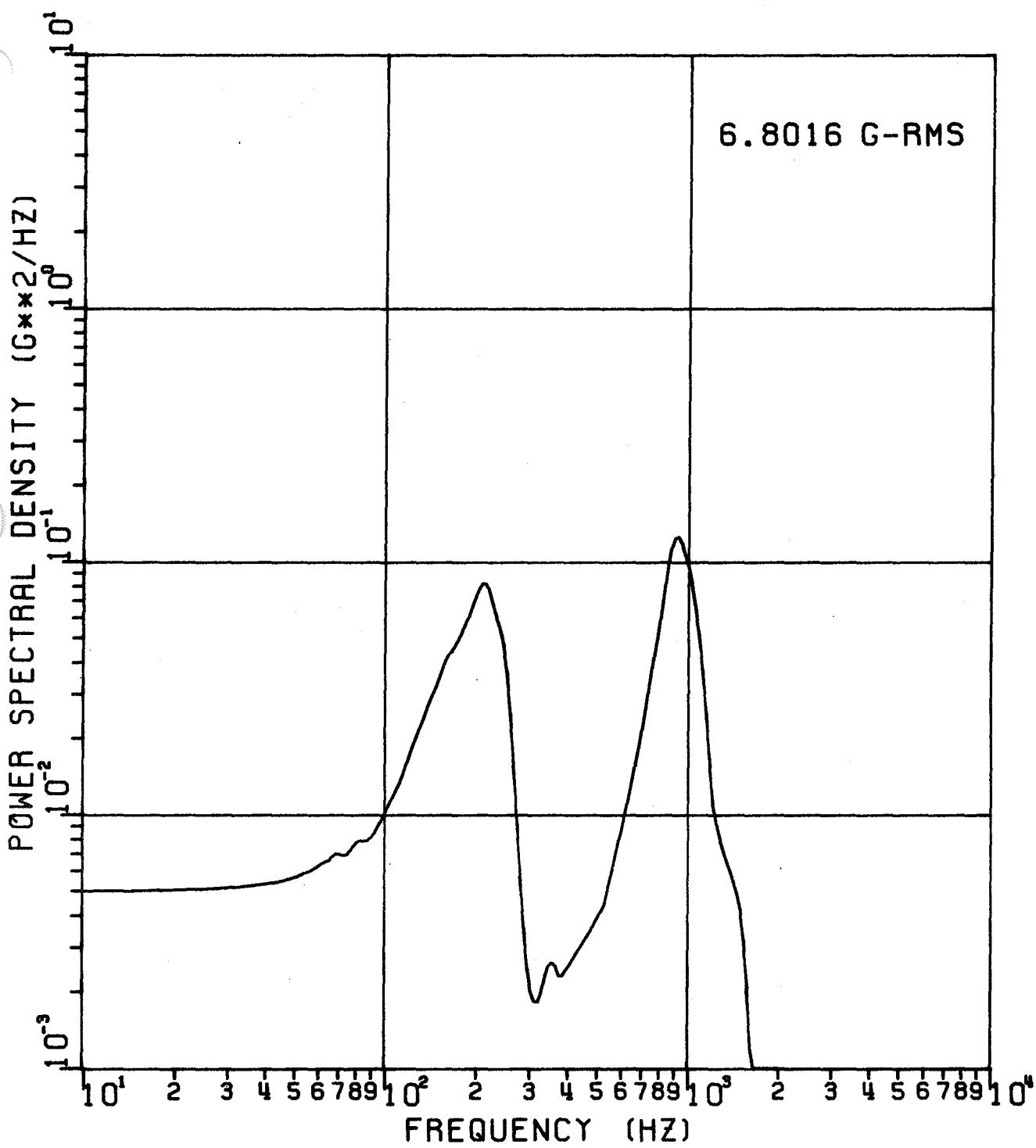
LOCATION 9



1 Y AXIS SUBPACK 3 SEP 1970

FIGURE 20c RANDOM VIBRATION SPECTRUM

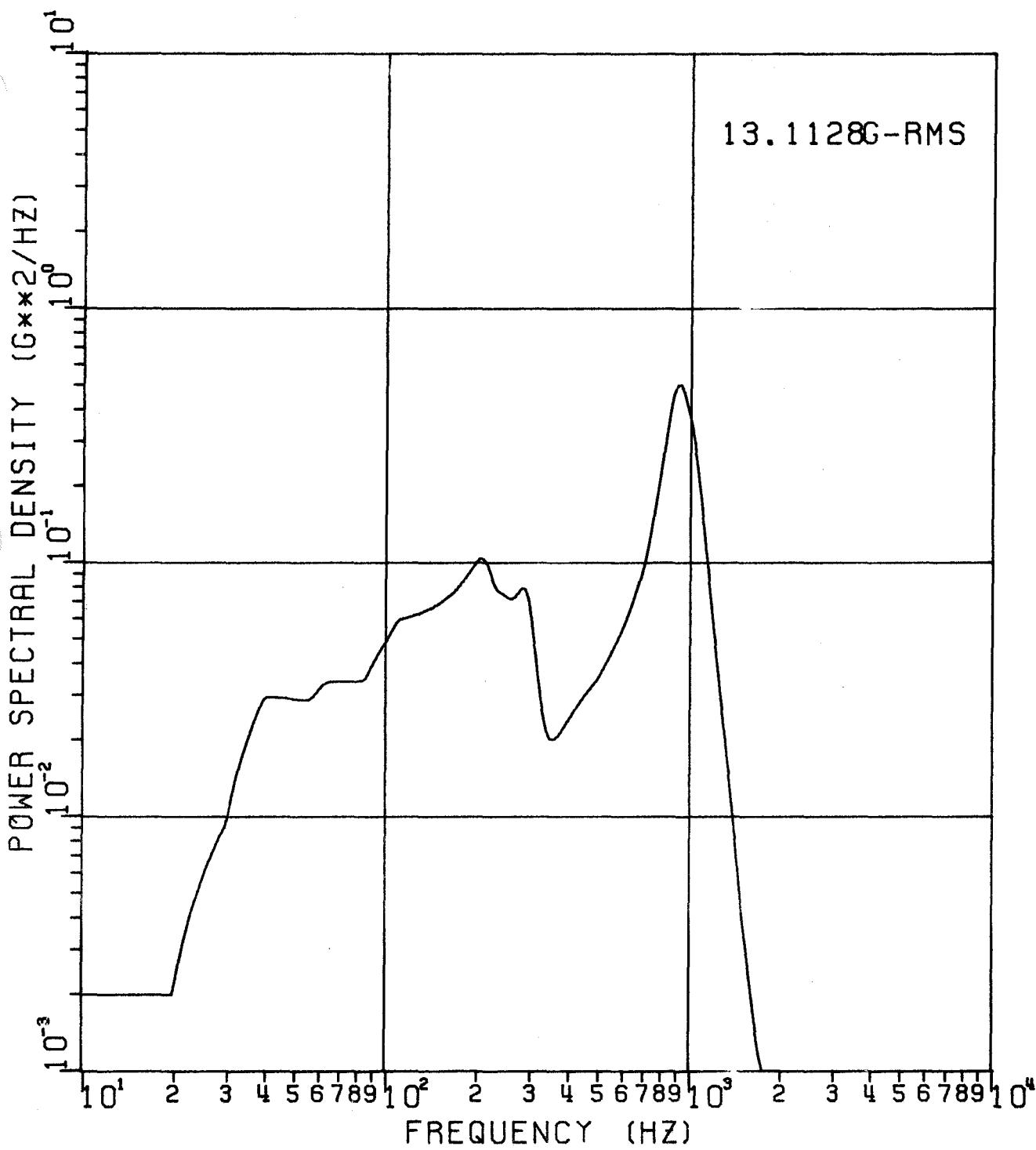
LOCATION 9



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 20d RANDOM VIBRATION SPECTRUM

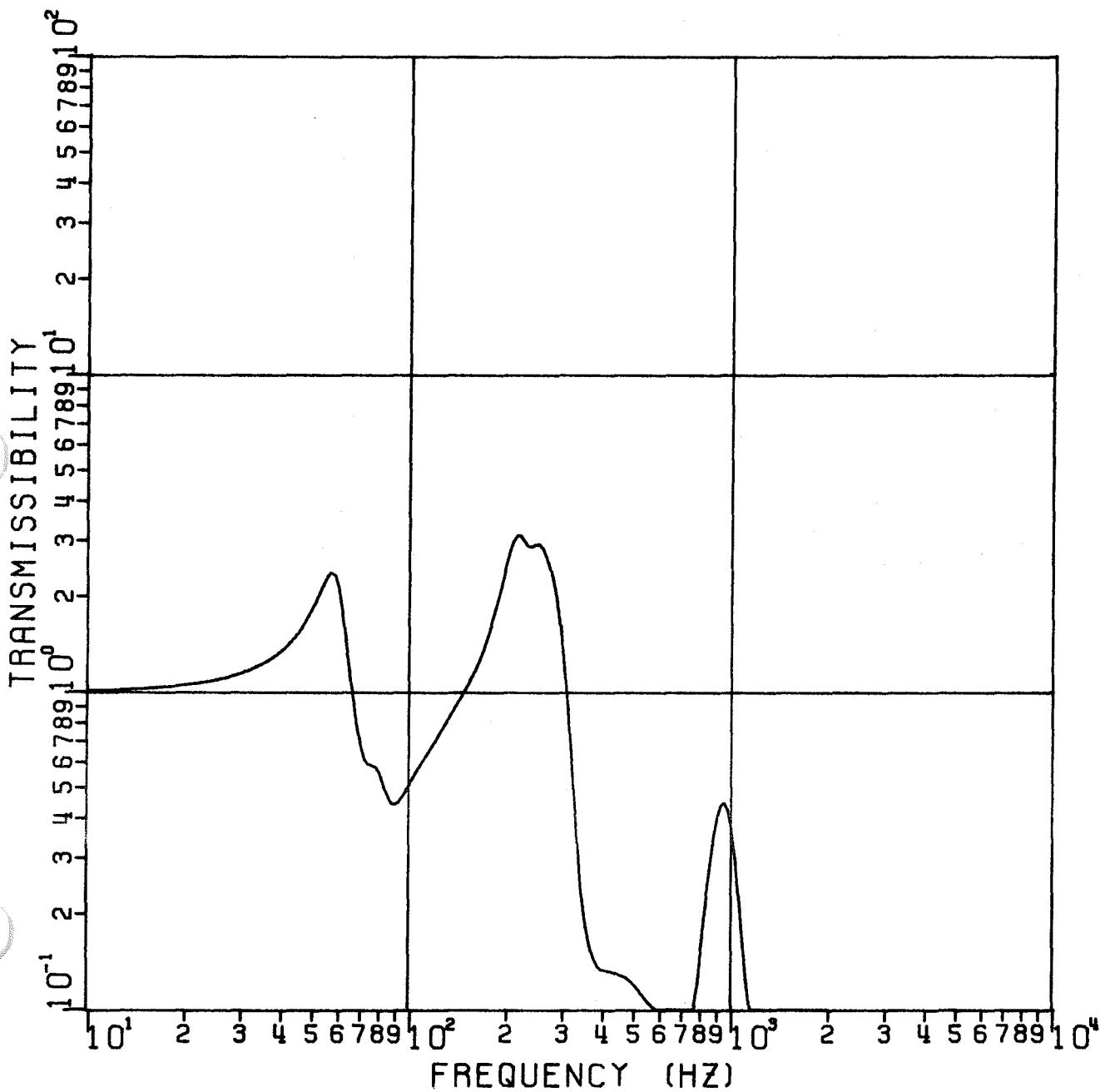
LOCATION 9



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 21a TRANSMISSIBILITY

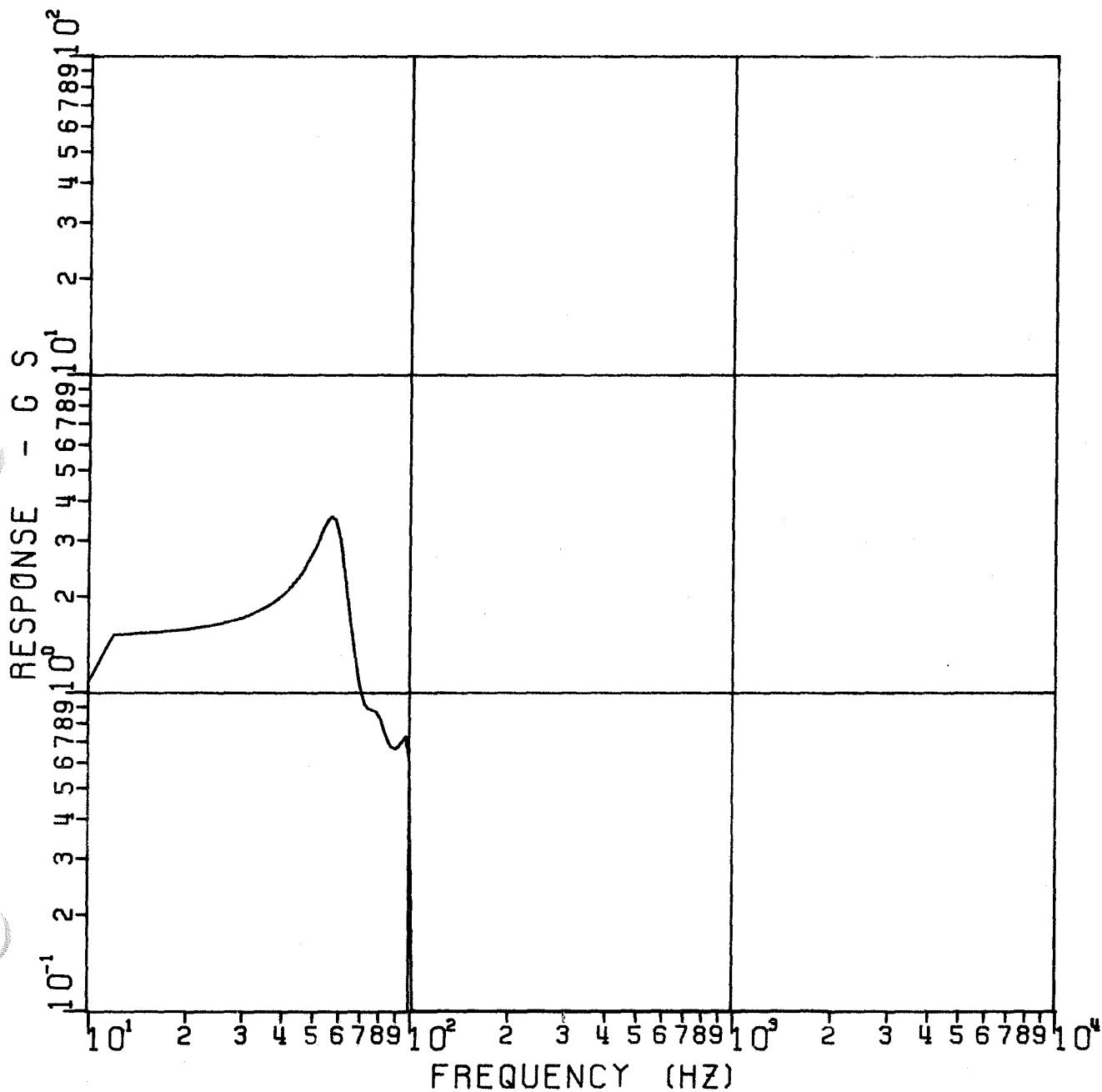
LOCATION 11



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 21b SINE RESPONSE

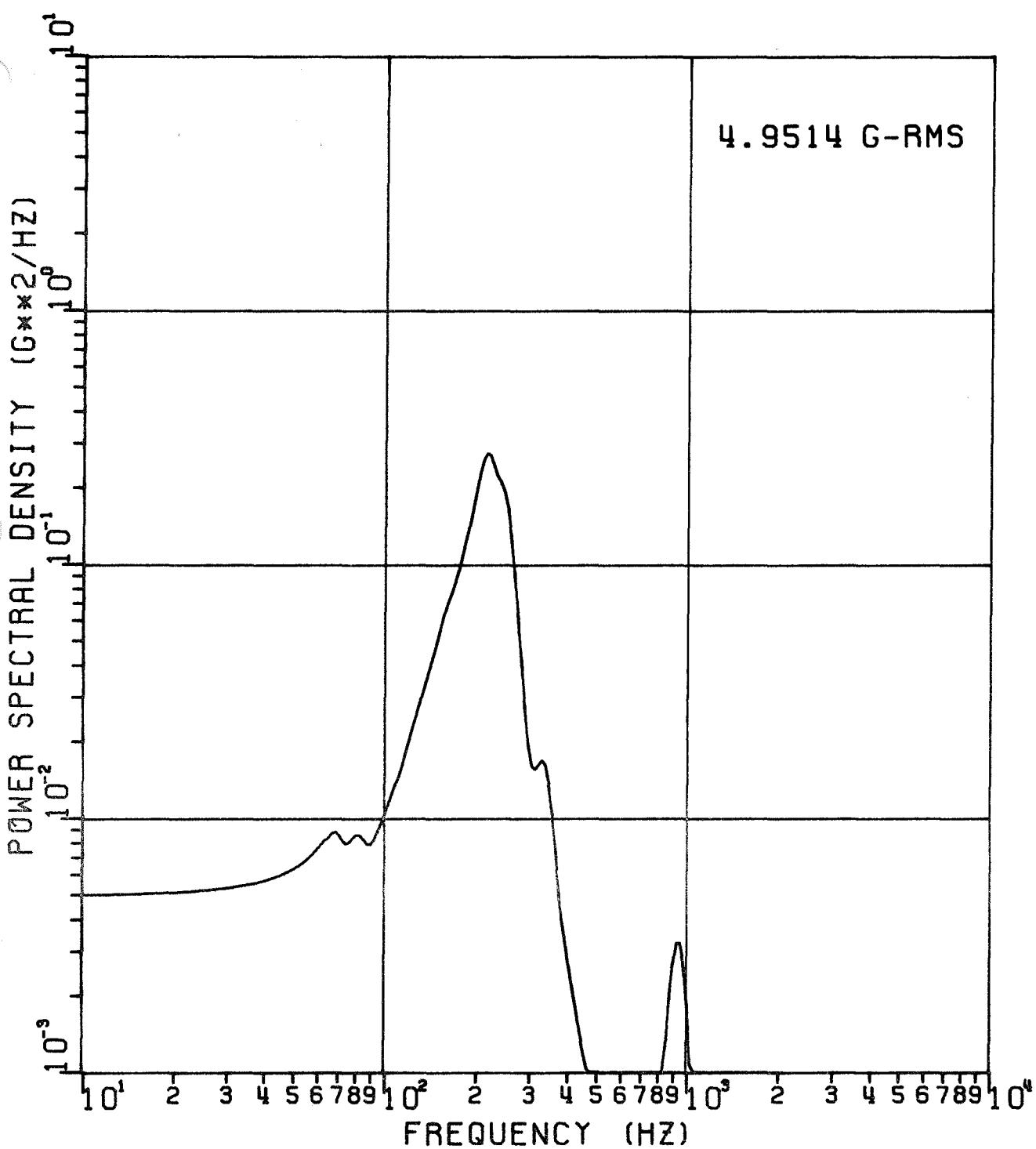
LOCATION 11



1 Y AXIS SUBPACK 3 SEP 1970

## FIGURE 2/c RANDOM VIBRATION SPECTRUM

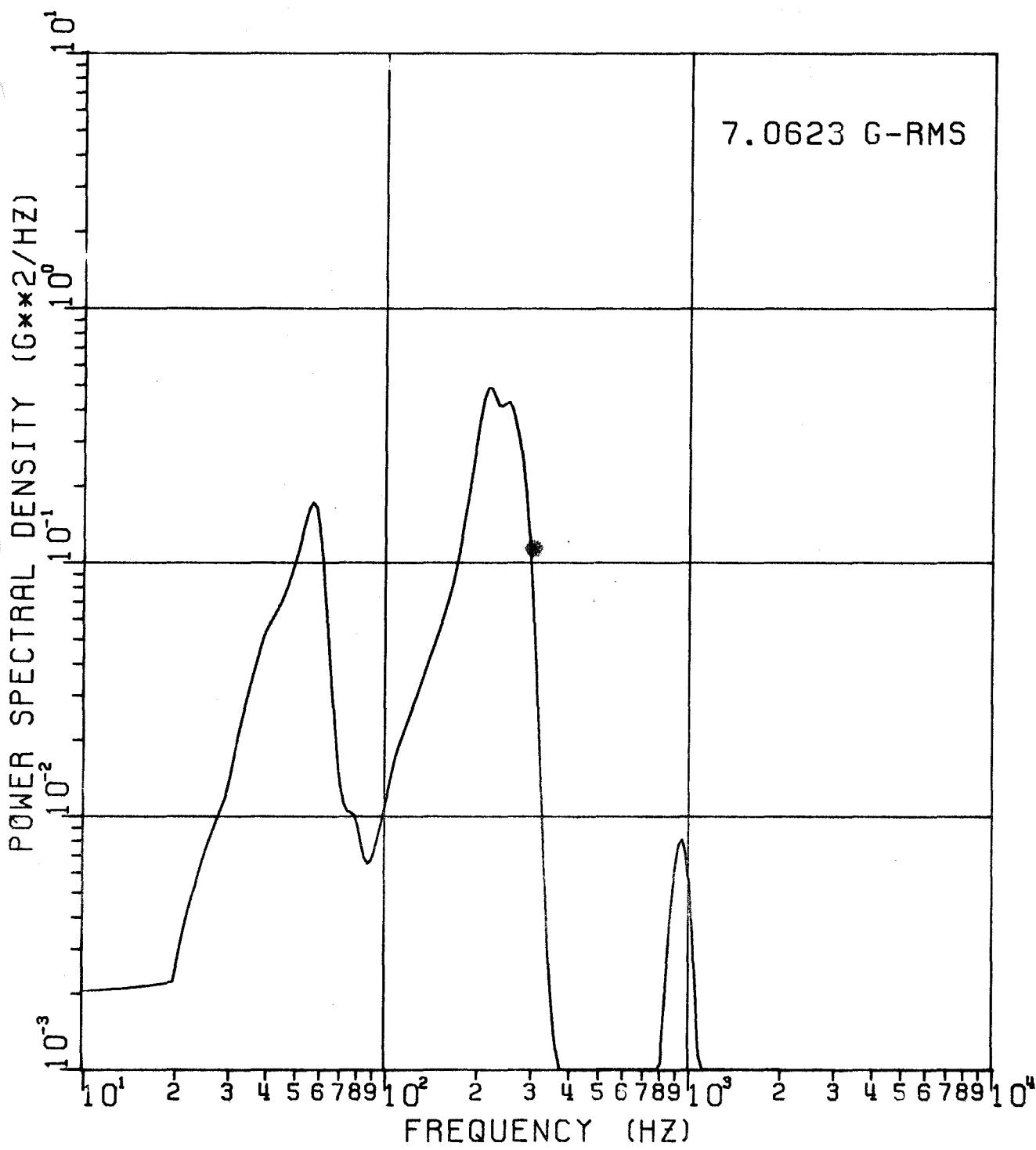
LOCATION 11



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 21d RANDOM VIBRATION SPECTRUM

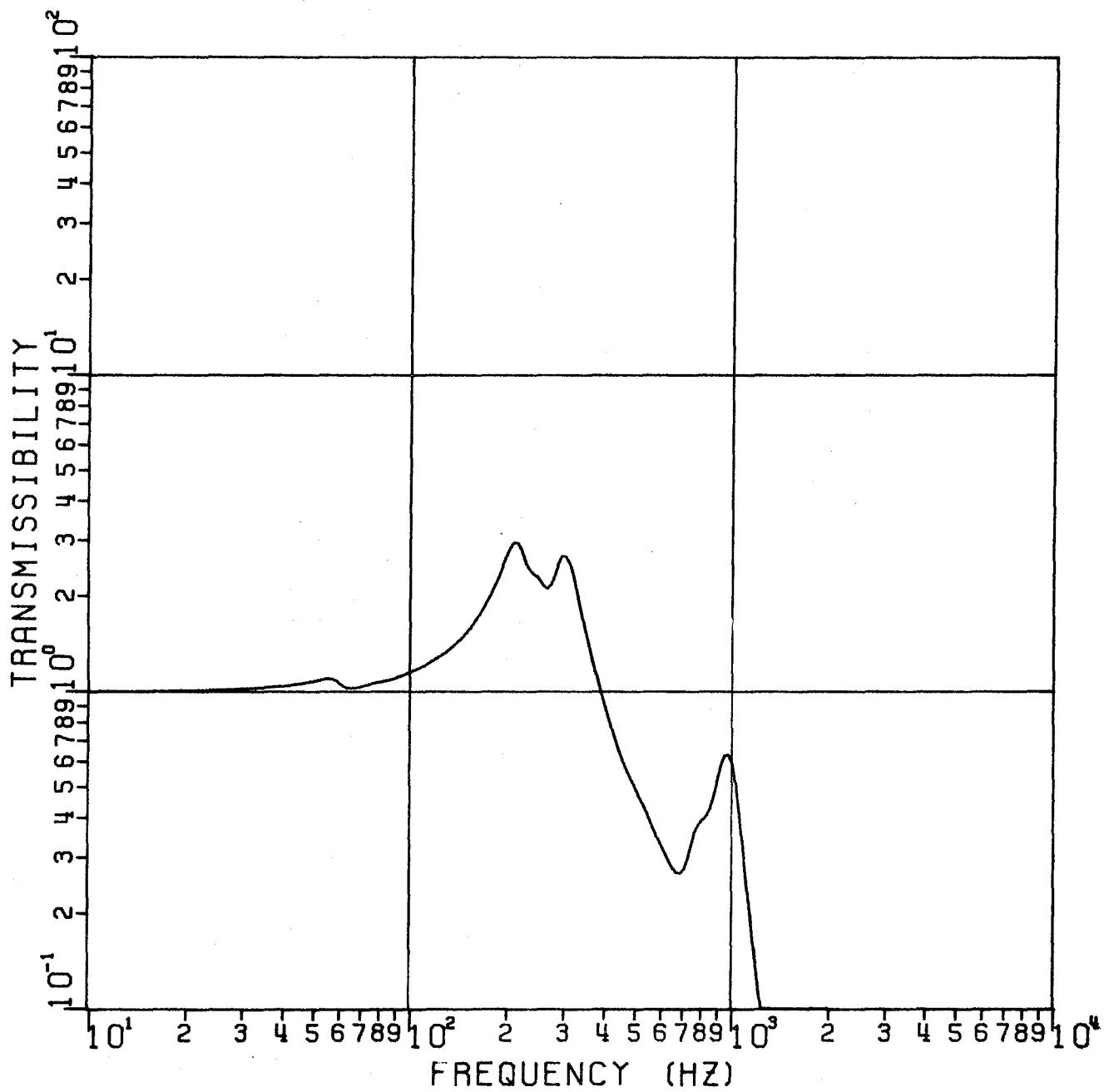
LOCATION 11



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 22 a TRANSMISSIBILITY

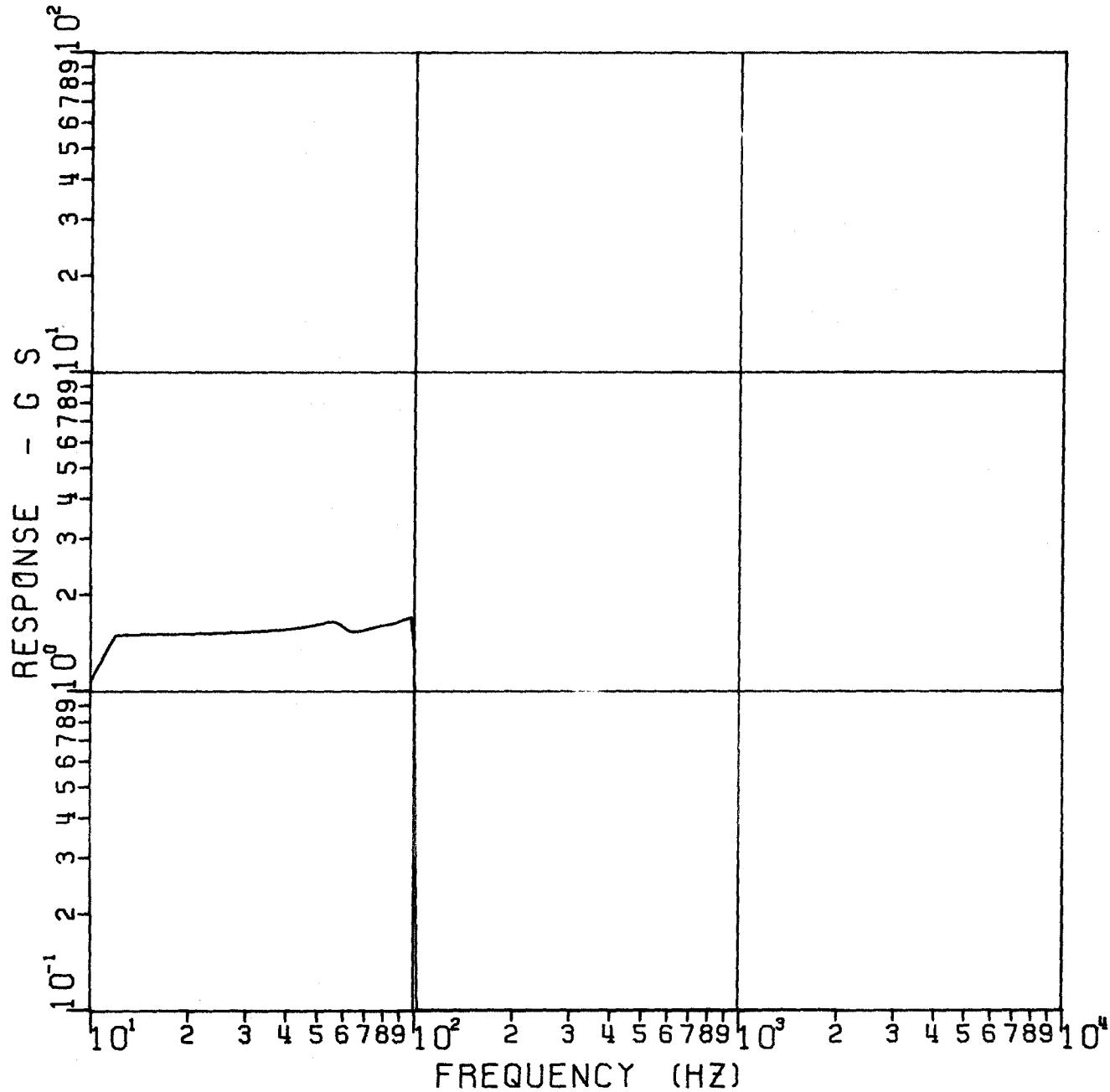
LOCATION 12



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 22 b SINE RESPONSE

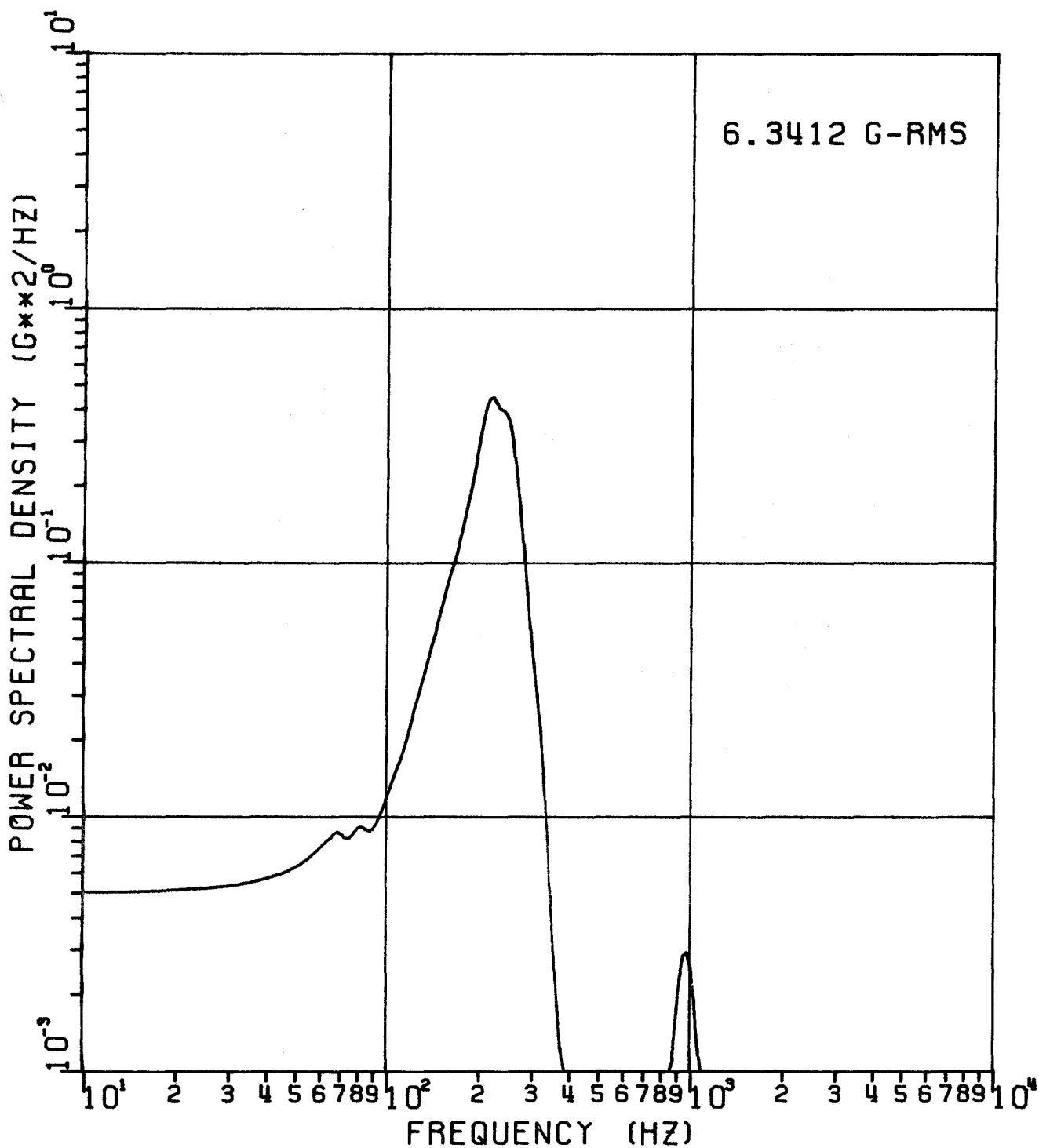
LOCATION 12



1 Y AXIS SUBPACK 3 SEP 1970

## FIGURE 22c RANDOM VIBRATION SPECTRUM

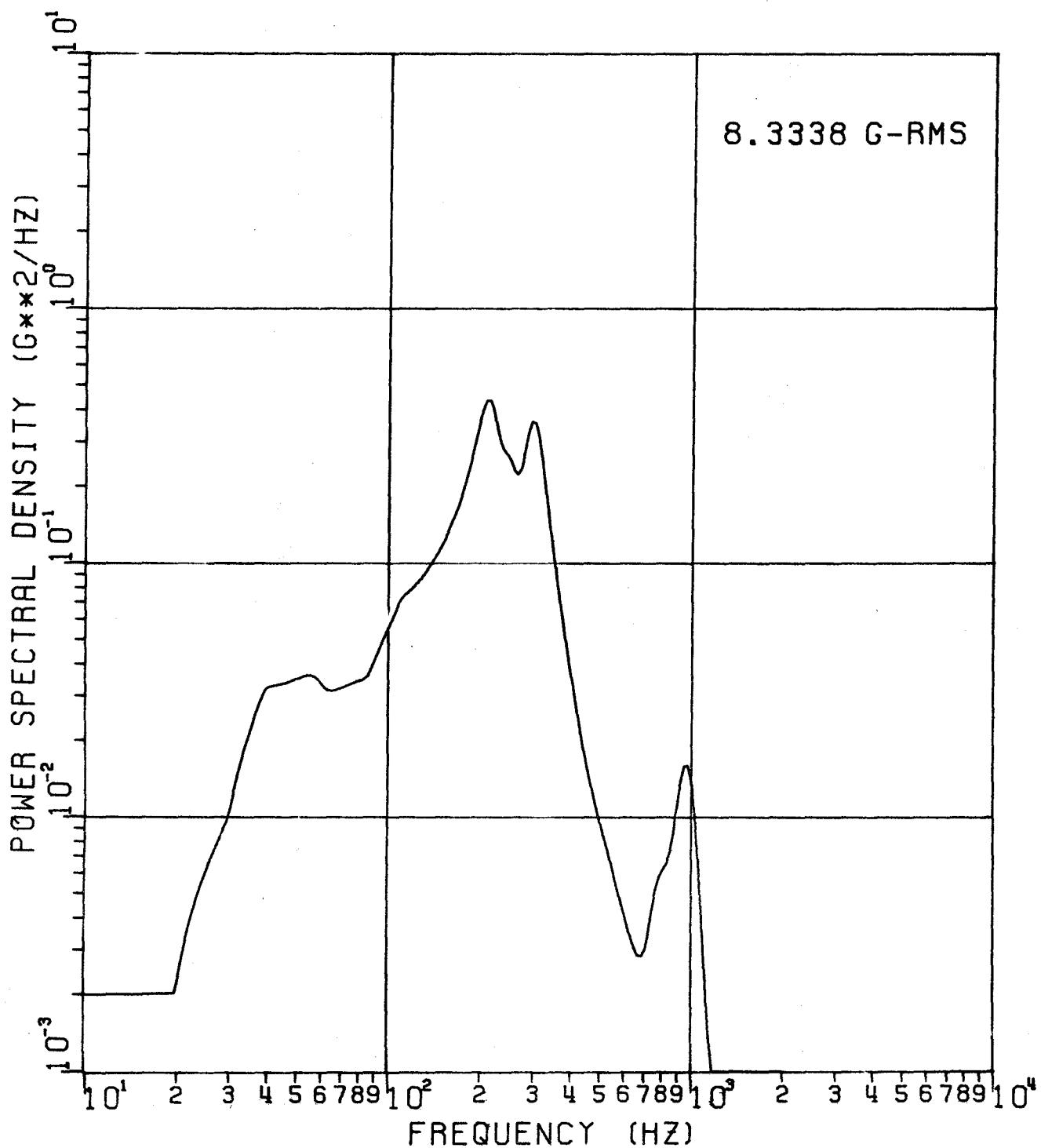
LOCATION 12



1 Y AXIS SUBP.-3 SEP 70 NEW LEVELS

FIGURE 22 d RANDOM VIBRATION SPECTRUM

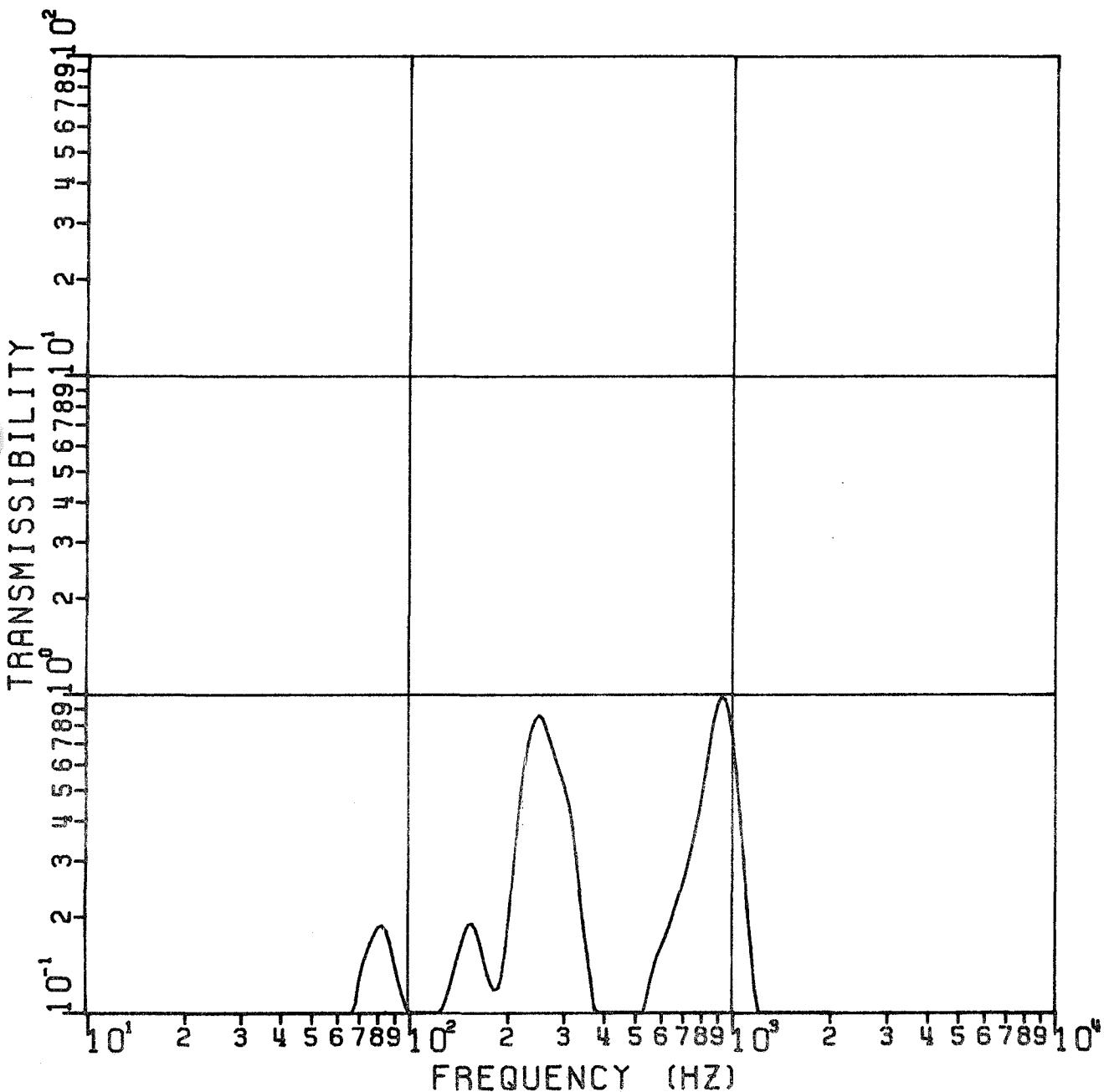
LOCATION 12



1 Y AXIS SUBPACK 3 SEP 1970

FIGURE 23a TRANSMISSIBILITY

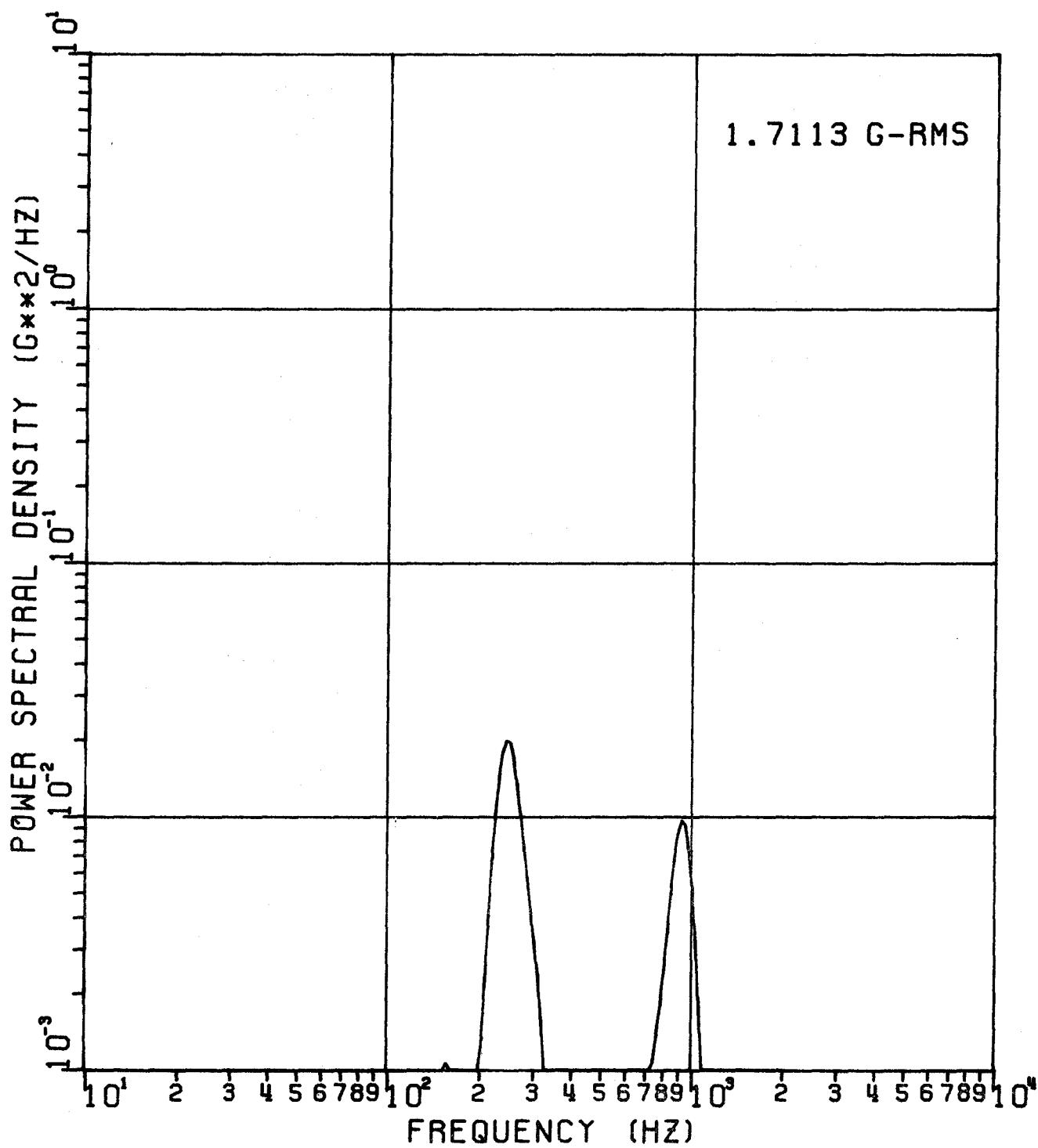
LOCATION 14



1 Y AXIS SUBPACK 3 SEP 1970

## FIGURE 23b RANDOM VIBRATION SPECTRUM

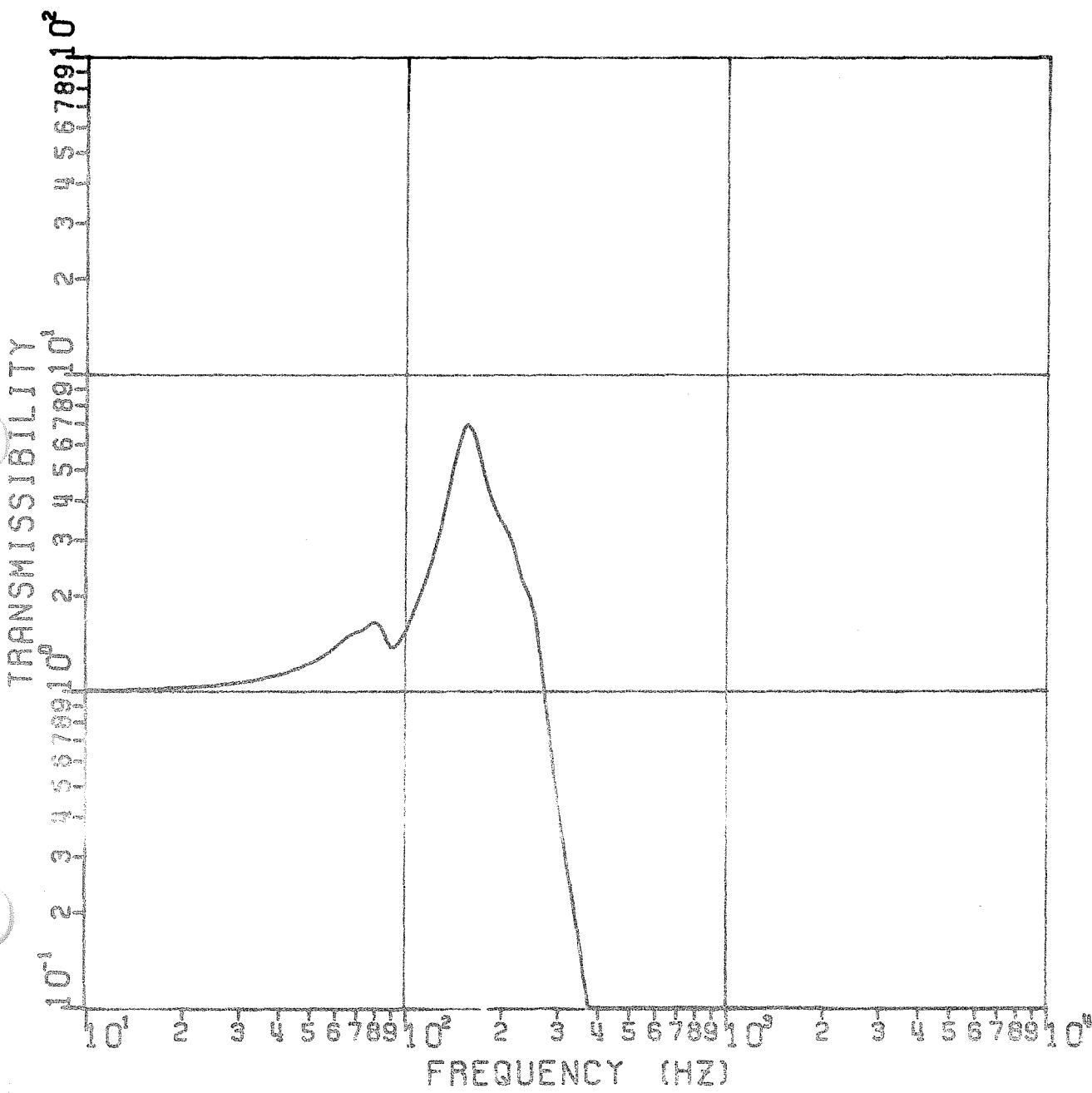
LOCATION 14



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 24a TRANSMISSIBILITY

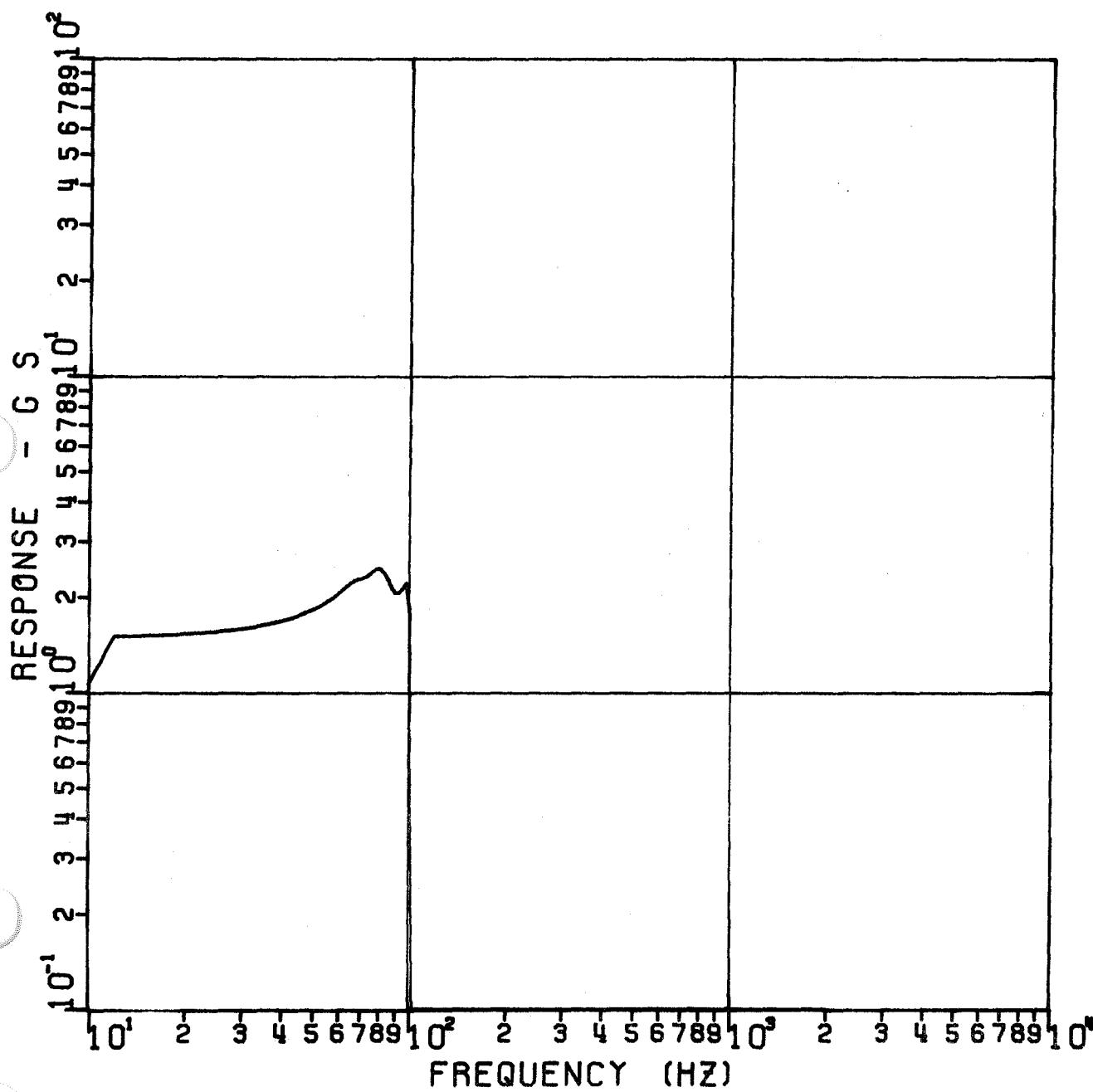
LOCATION 3



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 24b SINE RESPONSE

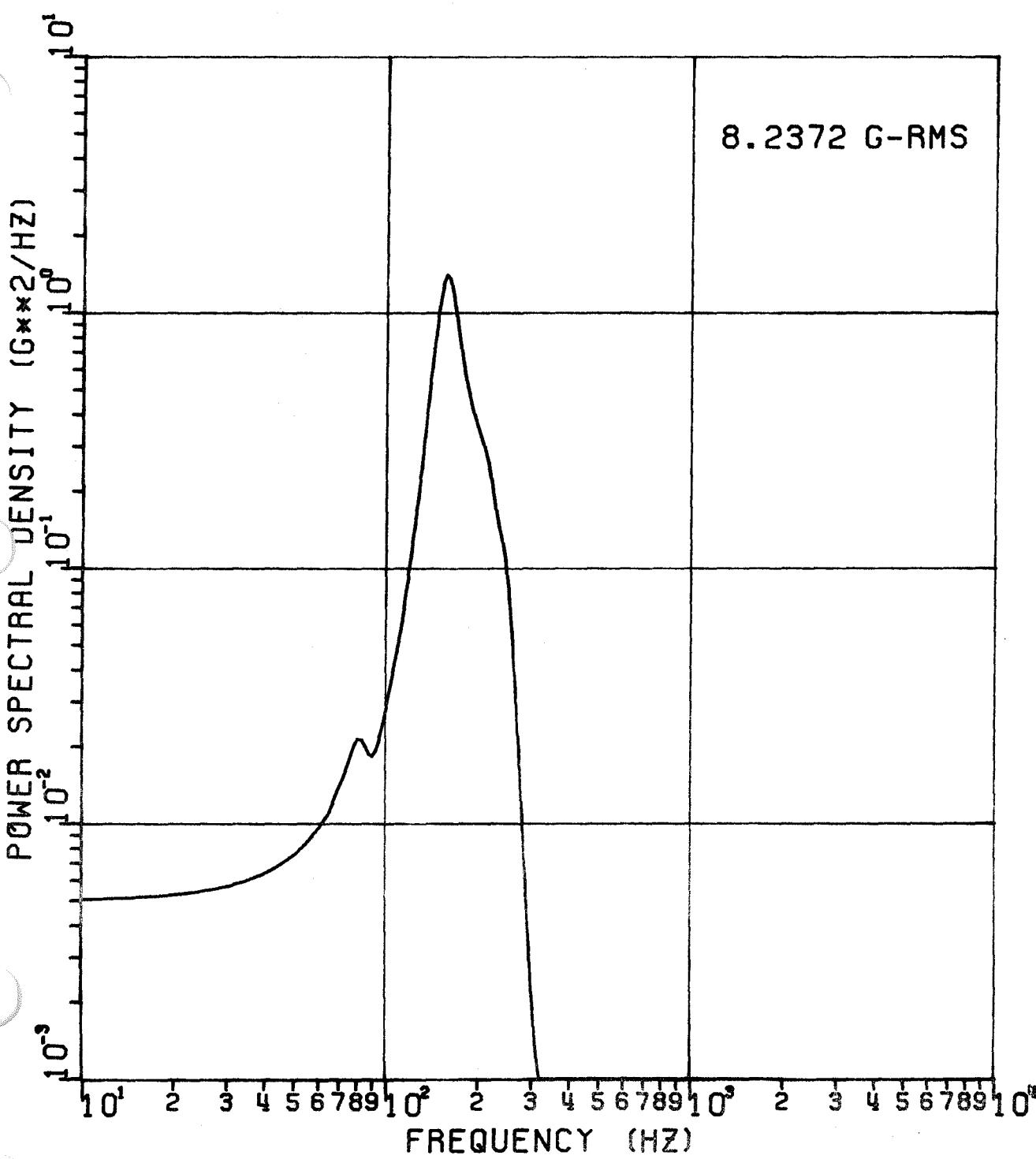
LOCATION 3



1 Z AXIS SUBPACK 3 SEP 1970

## FIGURE 24C RANDOM VIBRATION SPECTRUM

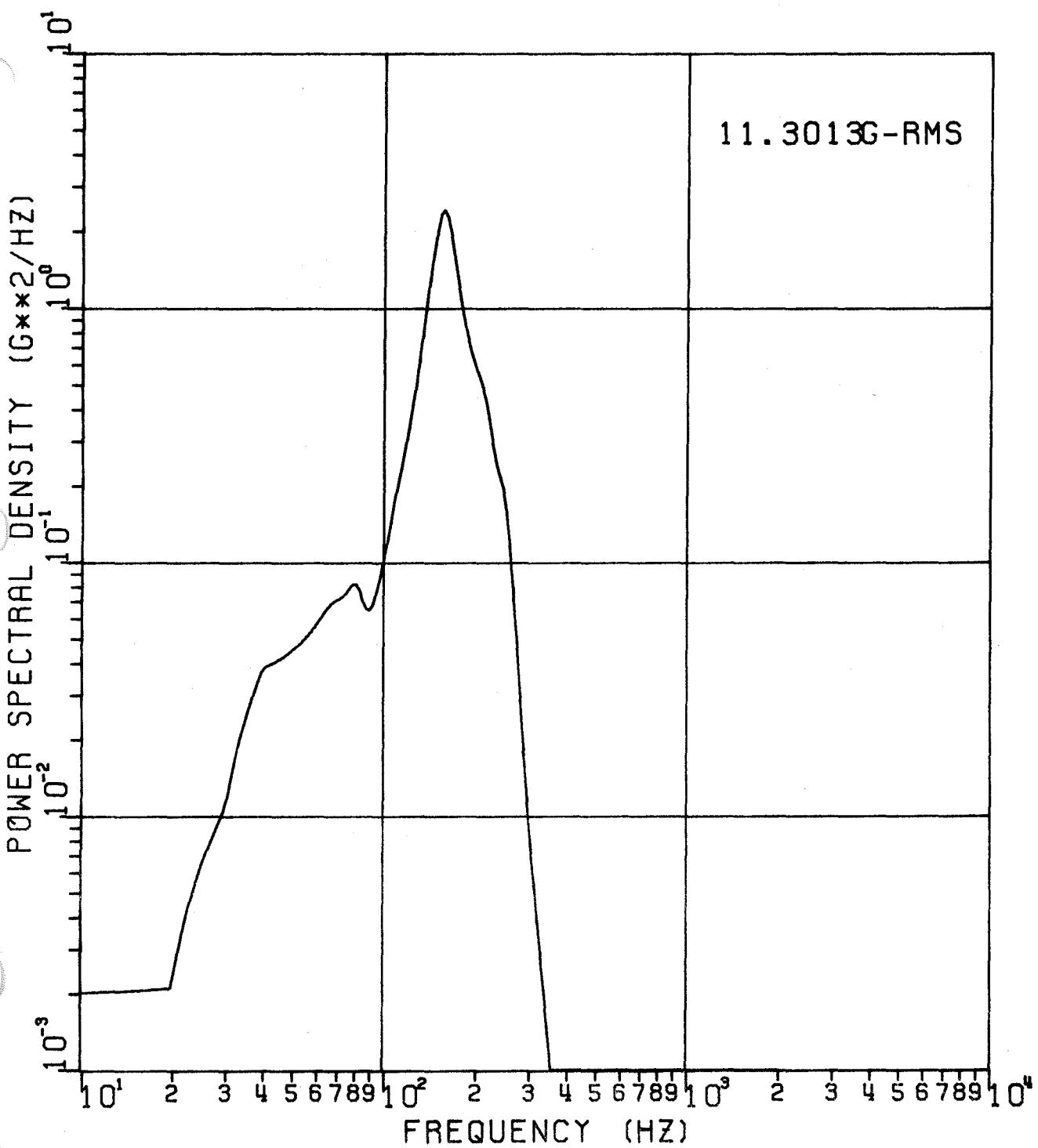
LOCATION 3



1 Z AXIS SUBP. 3 SEP 70 NEW LEVELS

FIGURE 24d RANDOM VIBRATION SPECTRUM

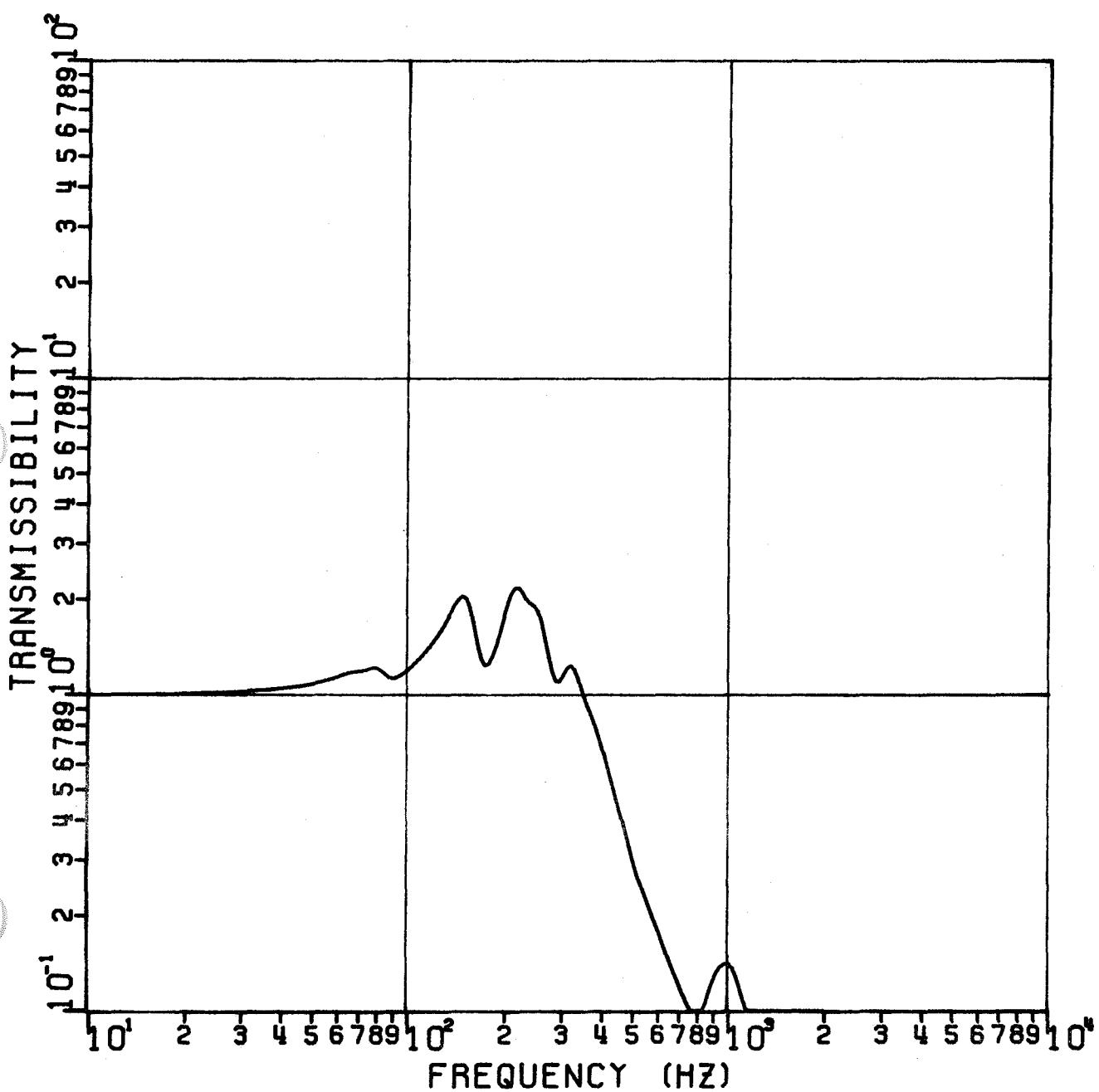
LOCATION 3



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 25a TRANSMISSIBILITY

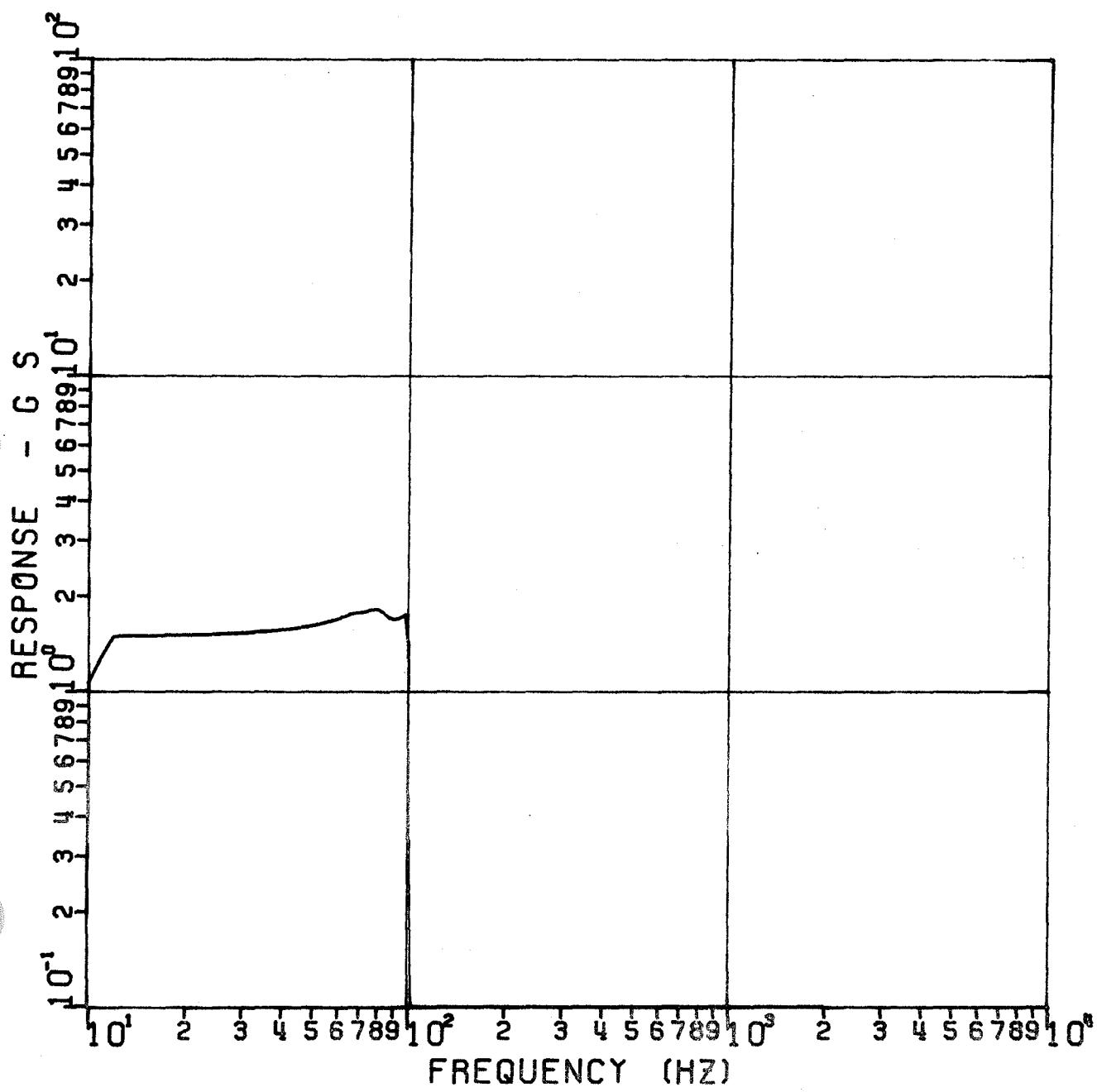
LOCATION 5



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 25b SINE RESPONSE

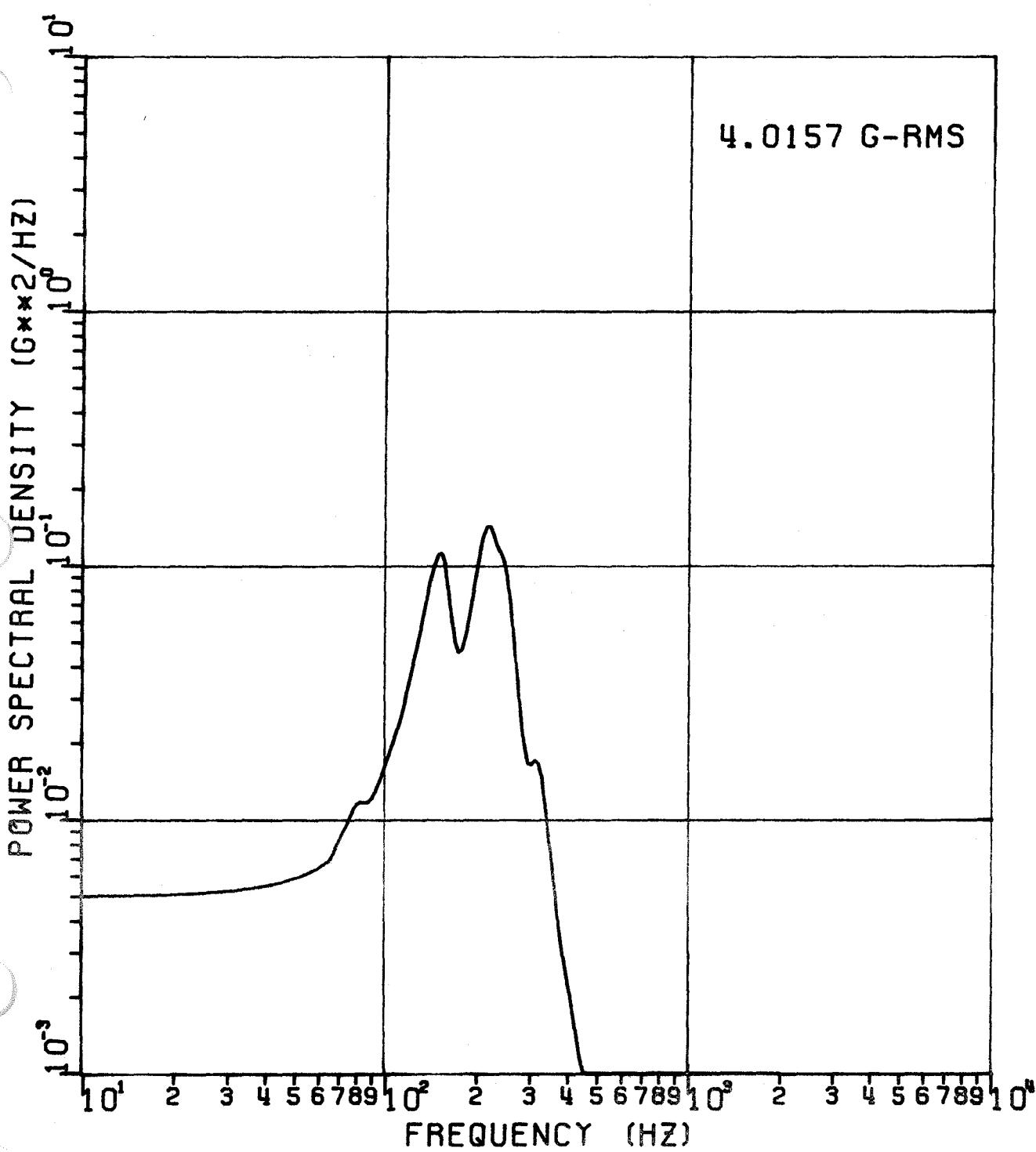
LOCATION 5



1 Z AXIS SUBPACK 3 SEP 1970

## FIGURE 25C RANDOM VIBRATION SPECTRUM

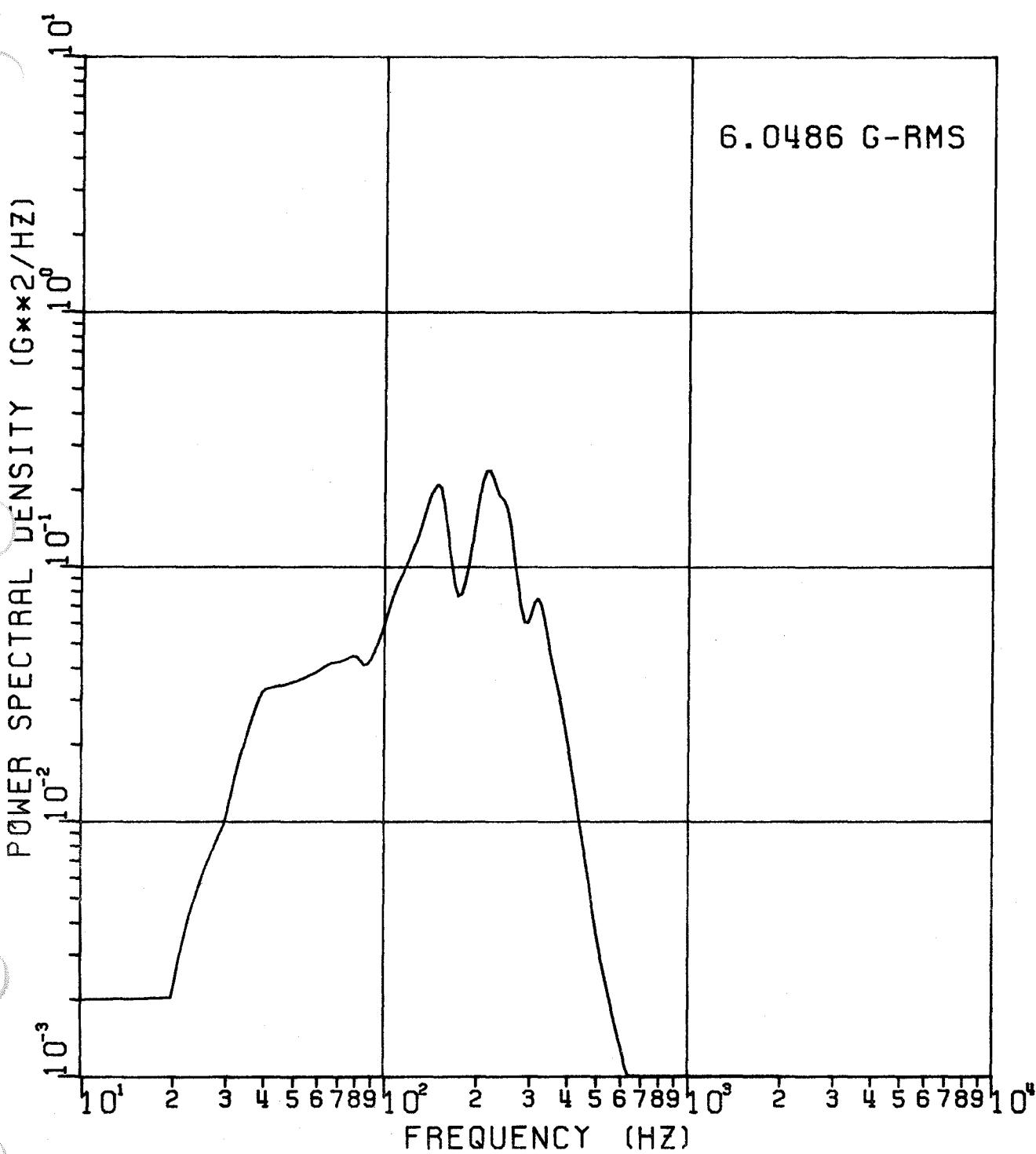
LOCATION 5



1 Z AXIS SUBP. 3 SEP 70 NEW LEVELS

## FIGURE 25d RANDOM VIBRATION SPECTRUM

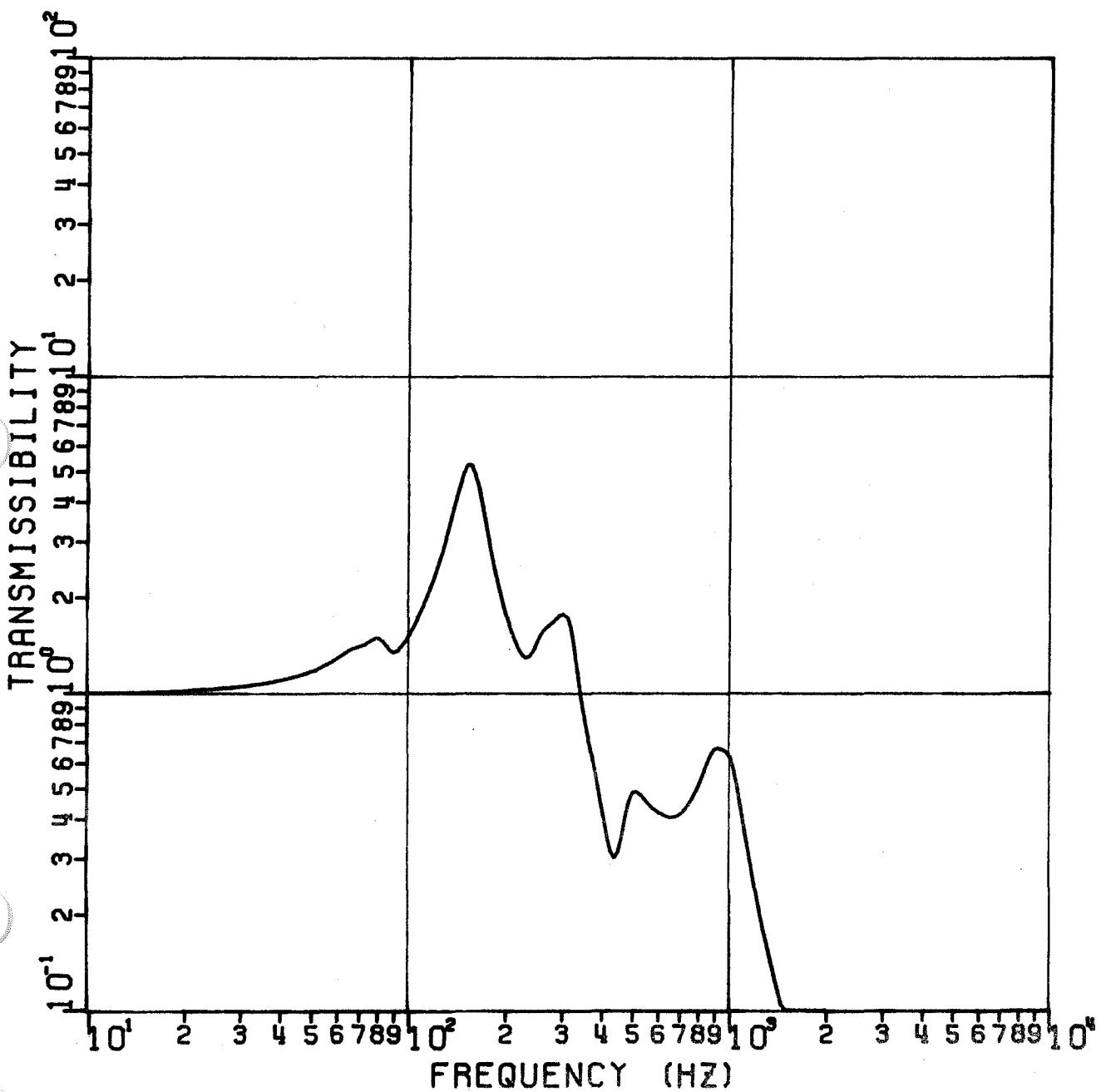
LOCATION 5



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 26a TRANSMISSIBILITY

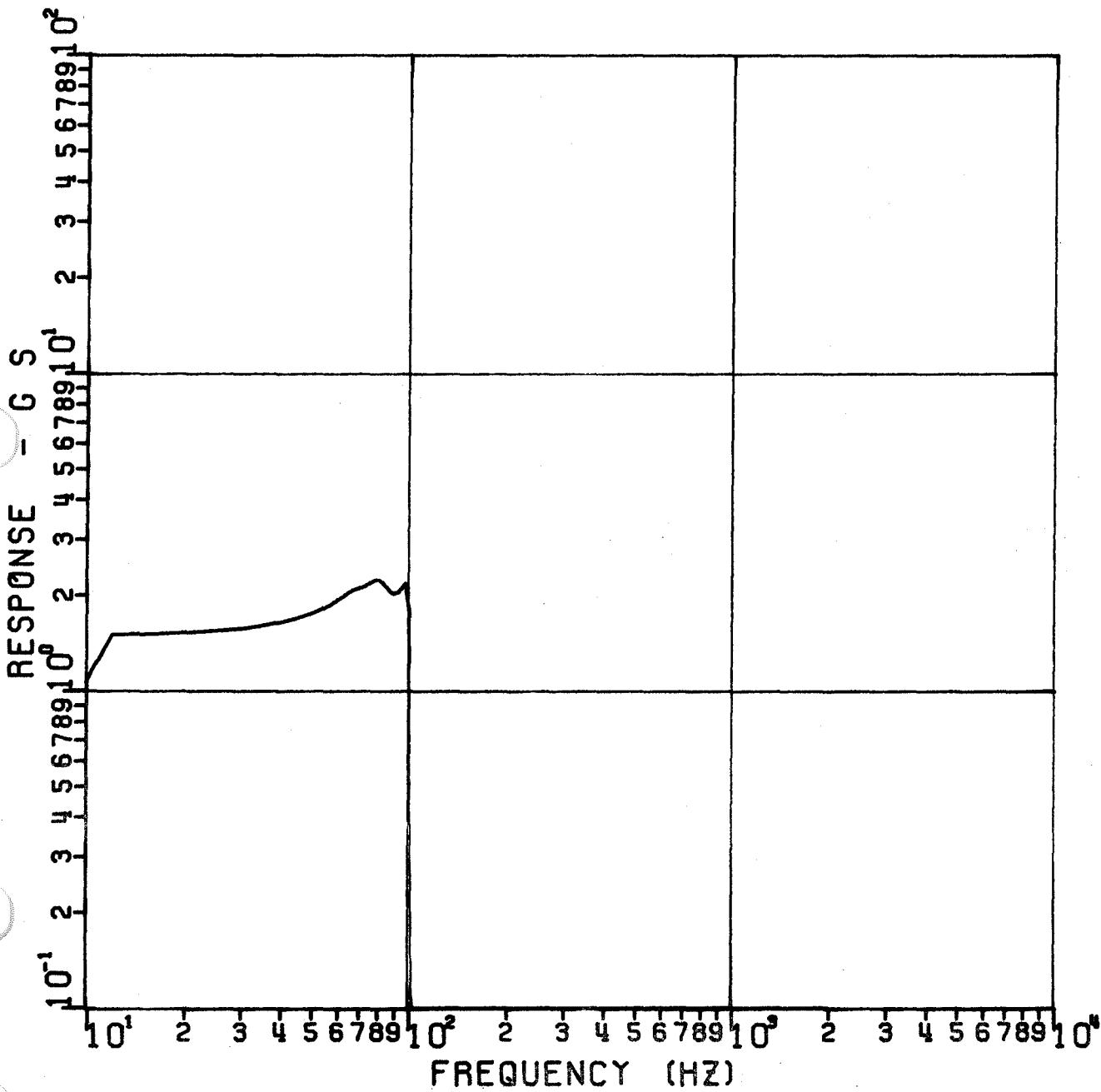
LOCATION 13



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 26 b SINE RESPONSE

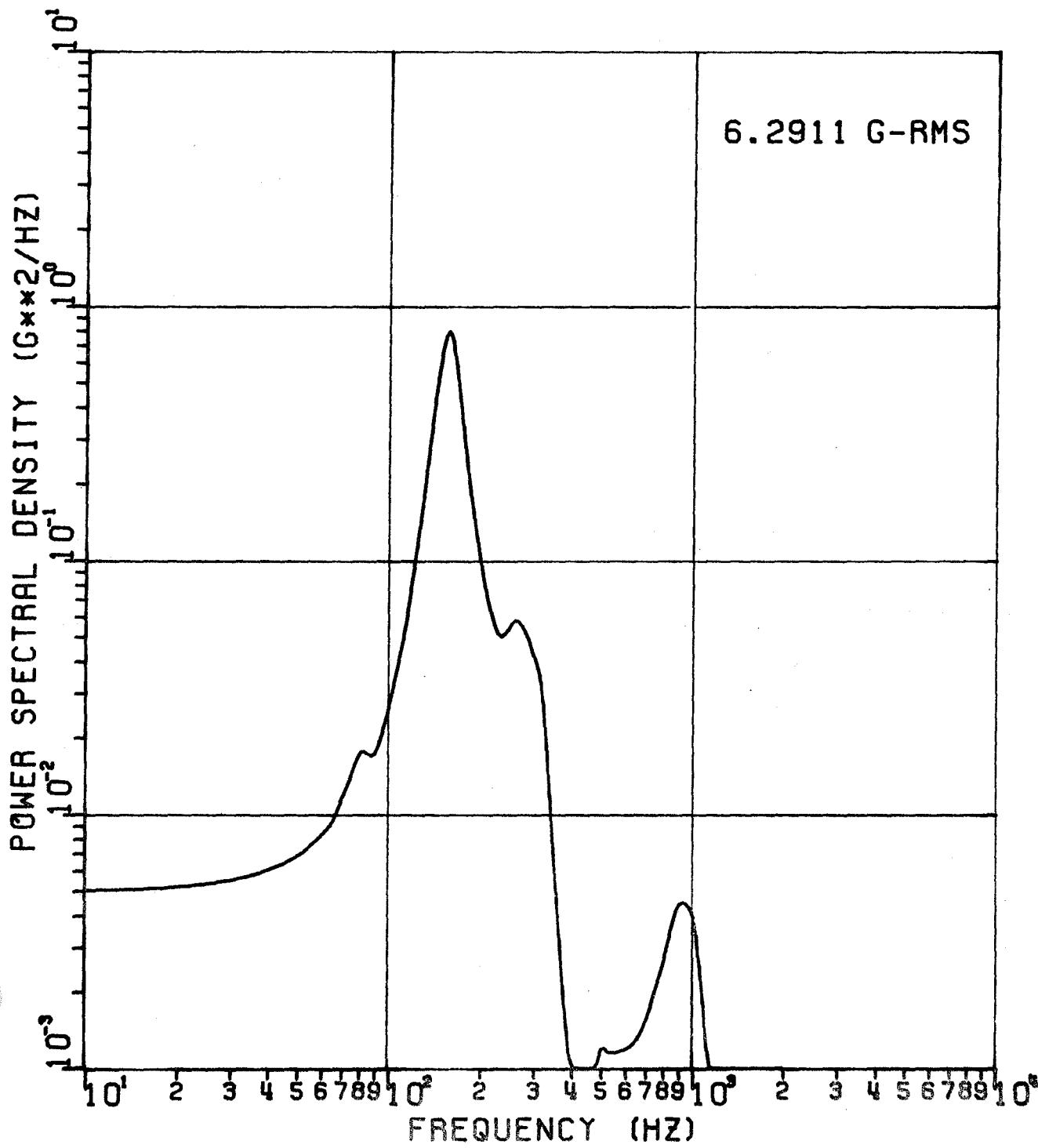
LOCATION 13



1 Z AXIS SUBPACK 3 SEP 1970

## FIGURE 26 C RANDOM VIBRATION SPECTRUM

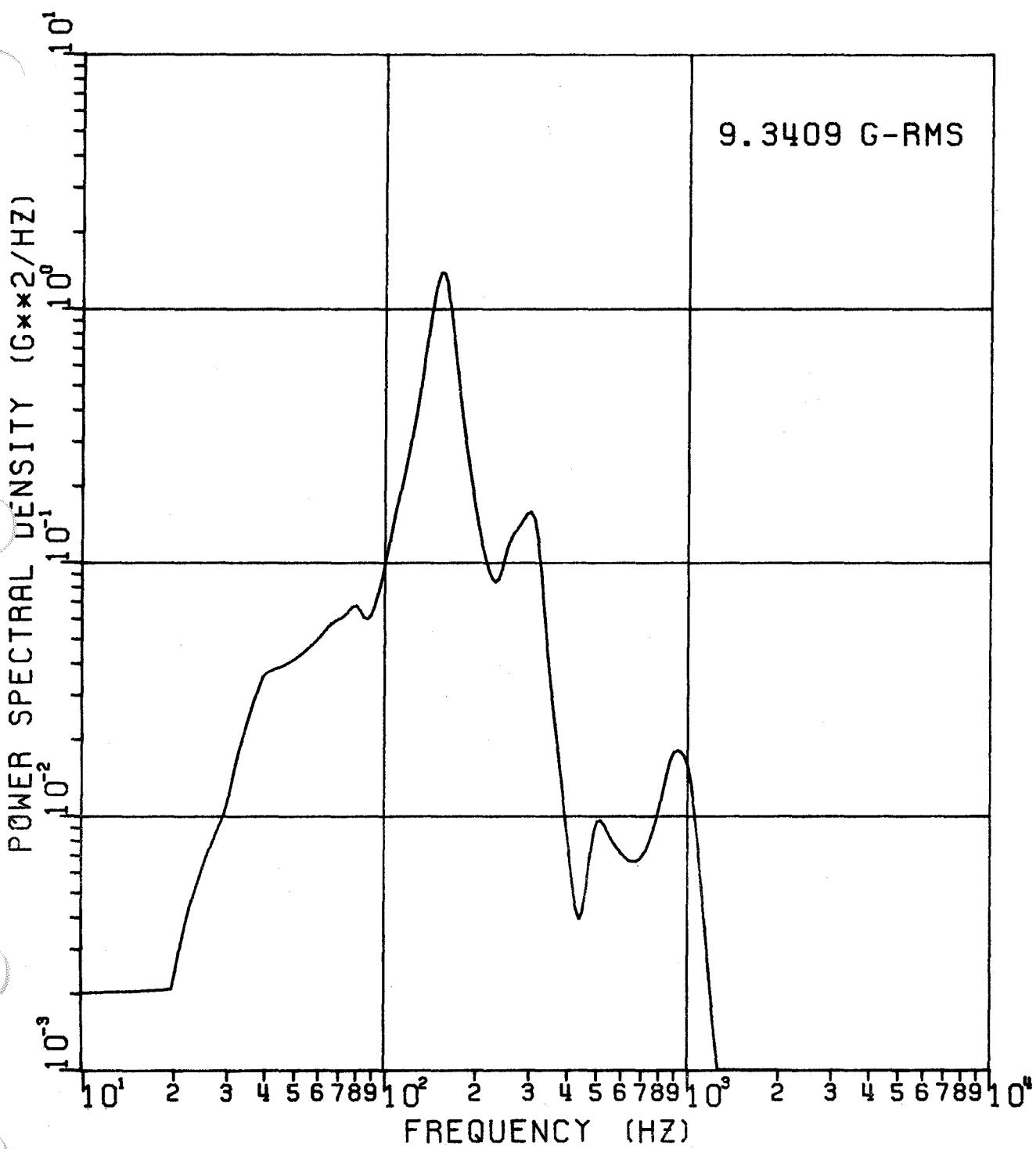
LOCATION 13



1 Z AXIS SUBP. 3 SEP 70 NEW LEVELS

## FIGURE 26d RANDOM VIBRATION SPECTRUM

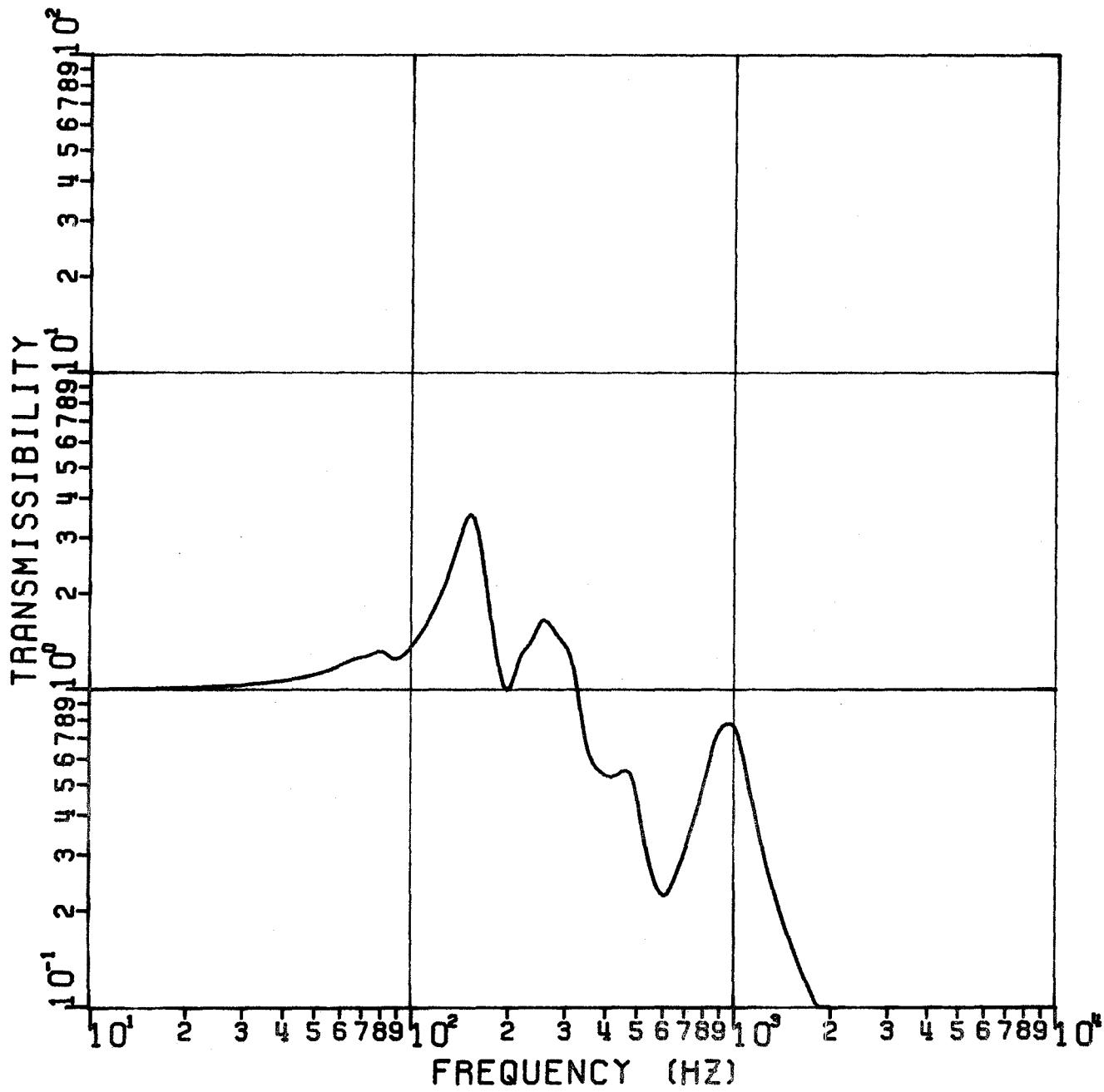
LOCATION 13



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 27a TRANSMISSIBILITY

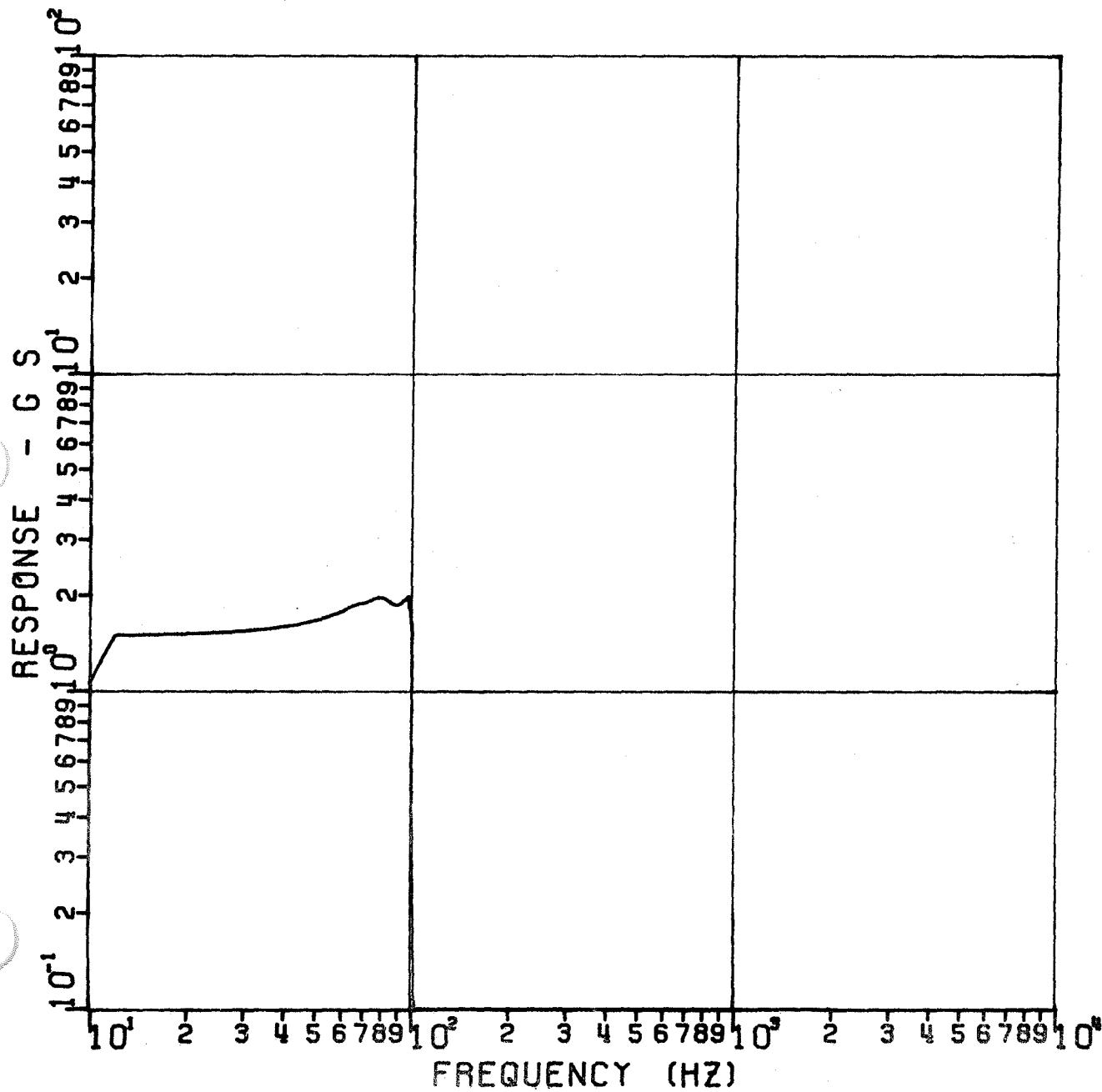
LOCATION 14



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 27b SINE RESPONSE

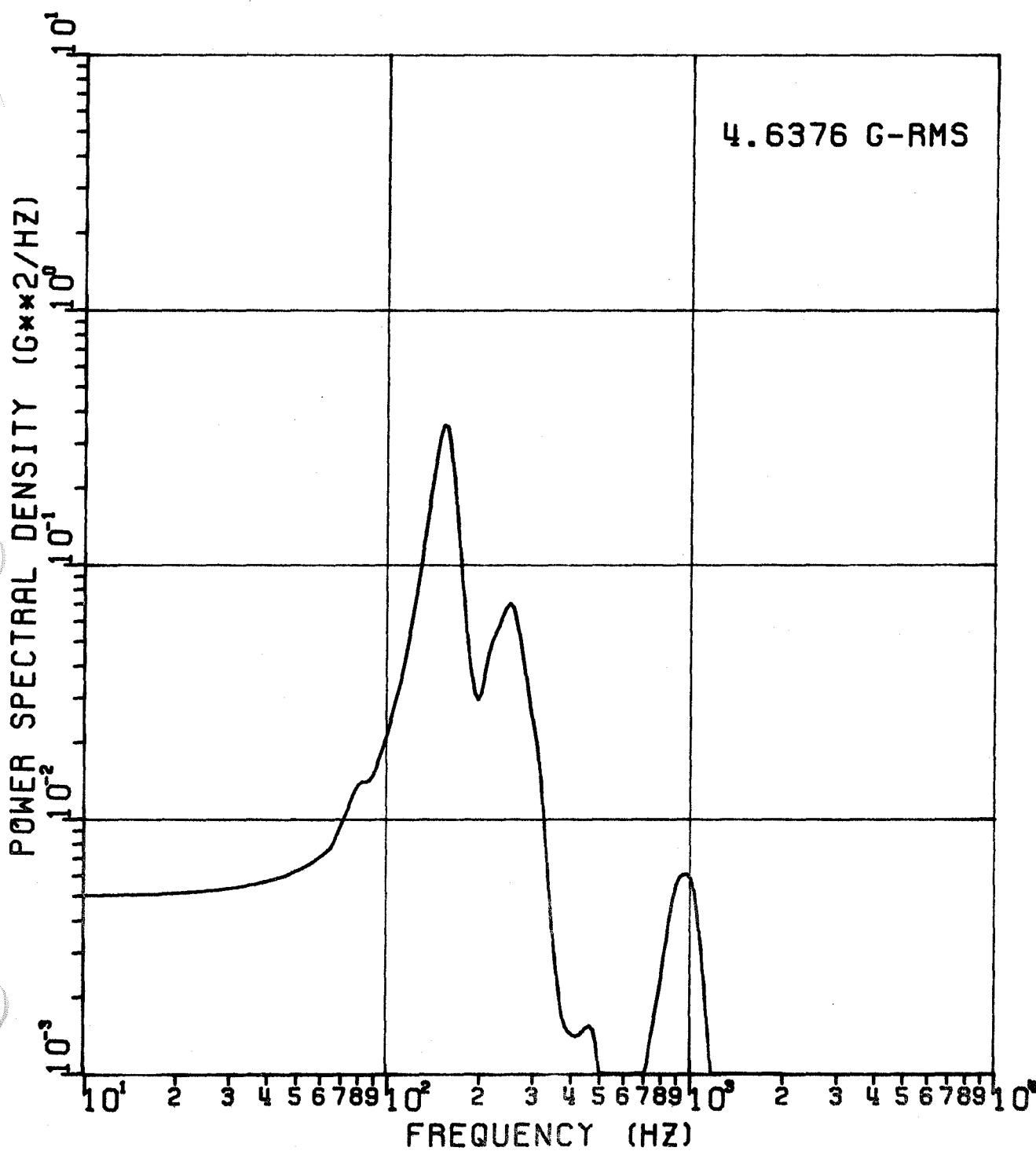
LOCATION 14



1 Z AXIS SUBPACK 3 SEP 1970

## FIGURE 27c RANDOM VIBRATION SPECTRUM

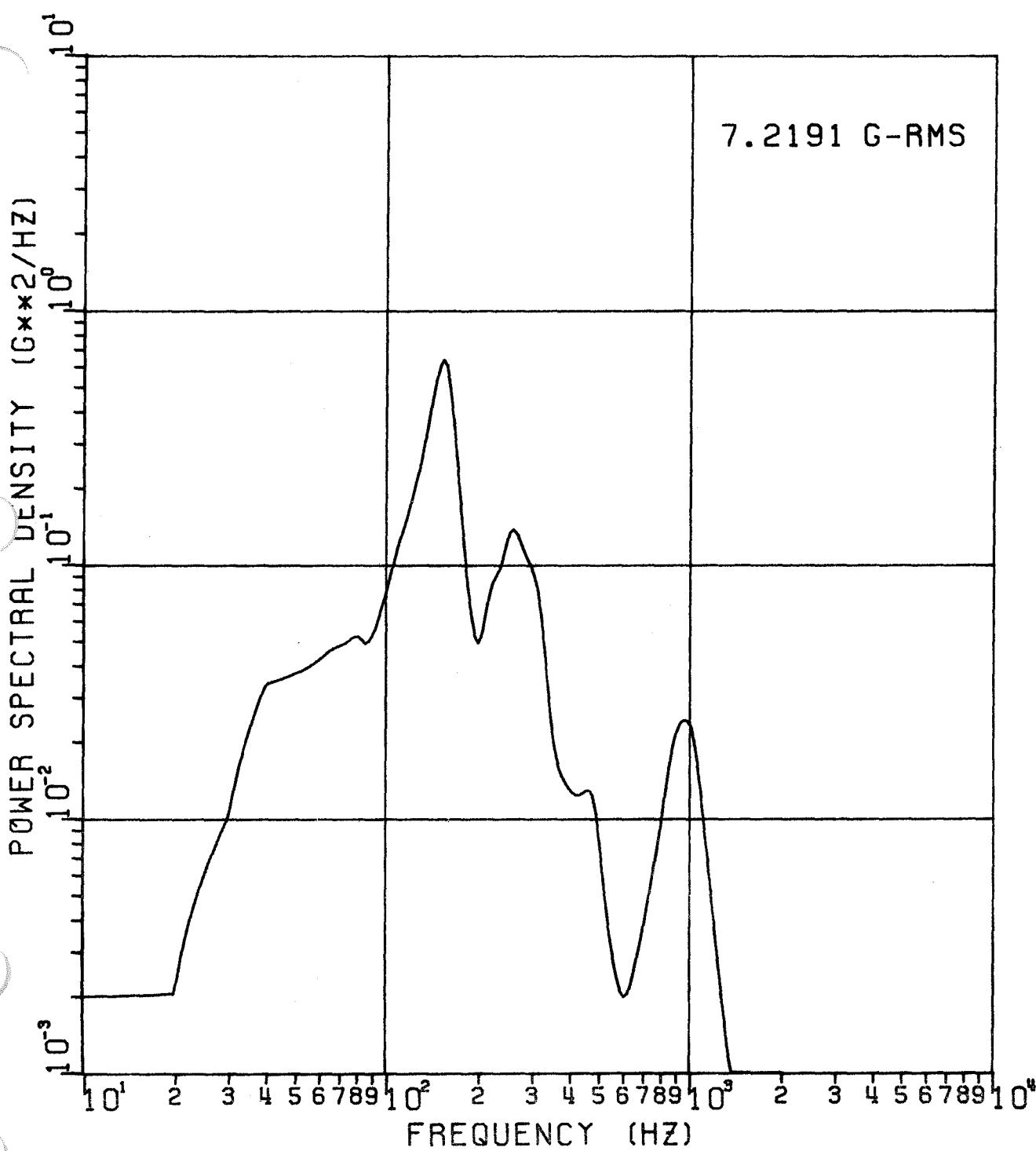
LOCATION 14



1 Z AXIS SUBP. 3 SEP 70 NEW LEVELS

FIGURE 27d RANDOM VIBRATION SPECTRUM

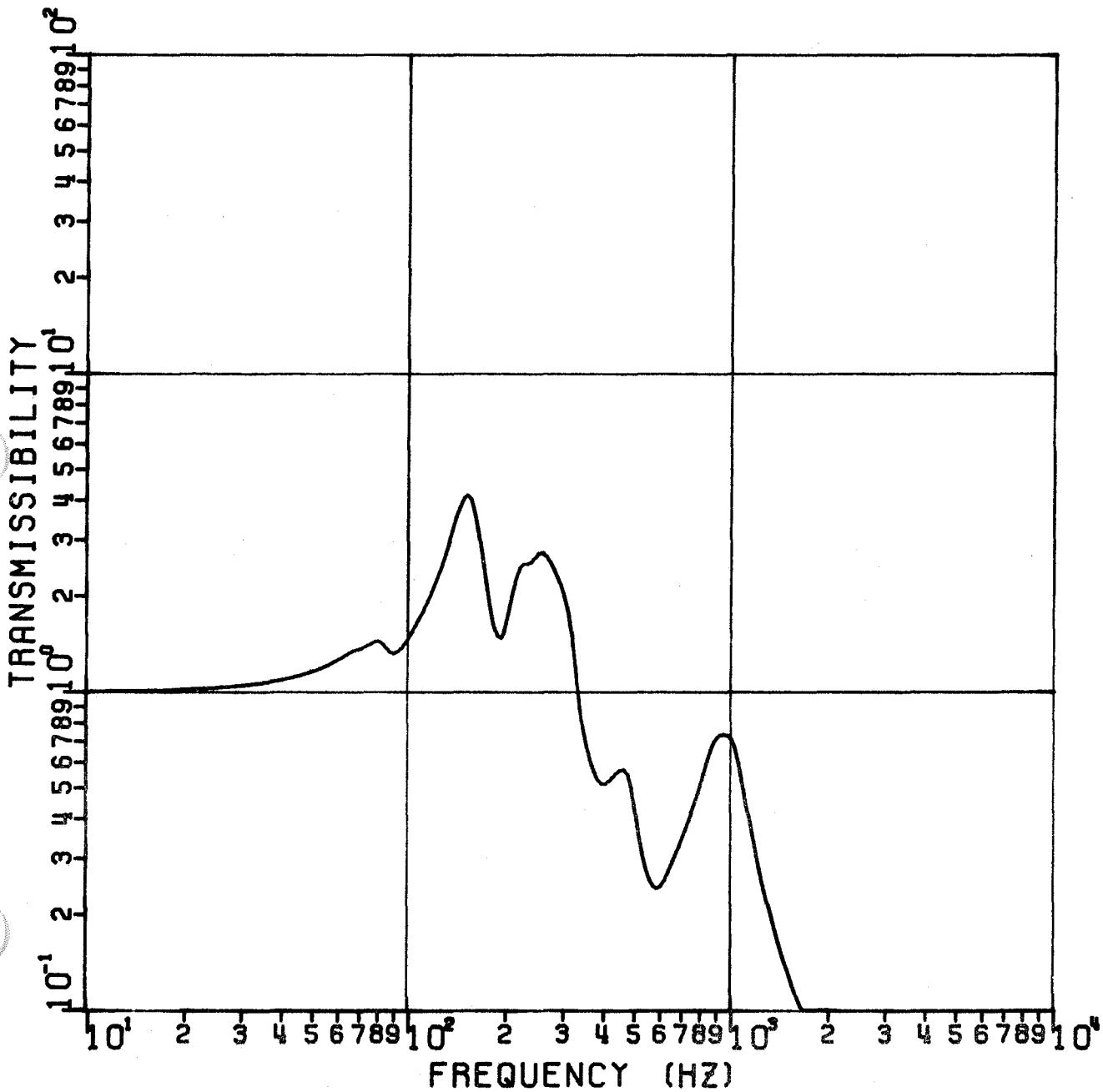
LOCATION 14



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 28a TRANSMISSIBILITY

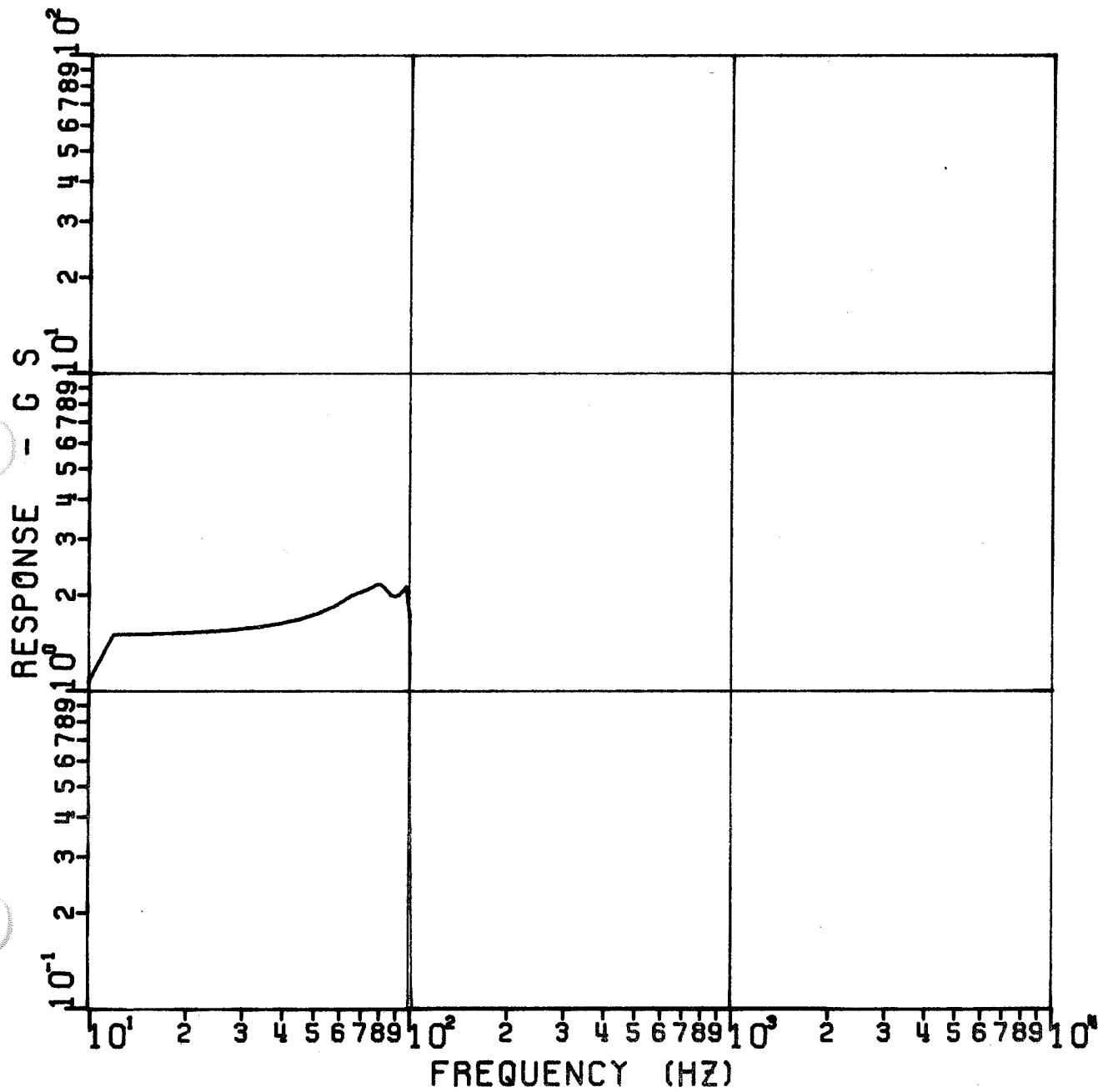
LOCATION 15



1 Z AXIS SUBPACK 3 SEP 1970

FIGURE 28b SINE RESPONSE

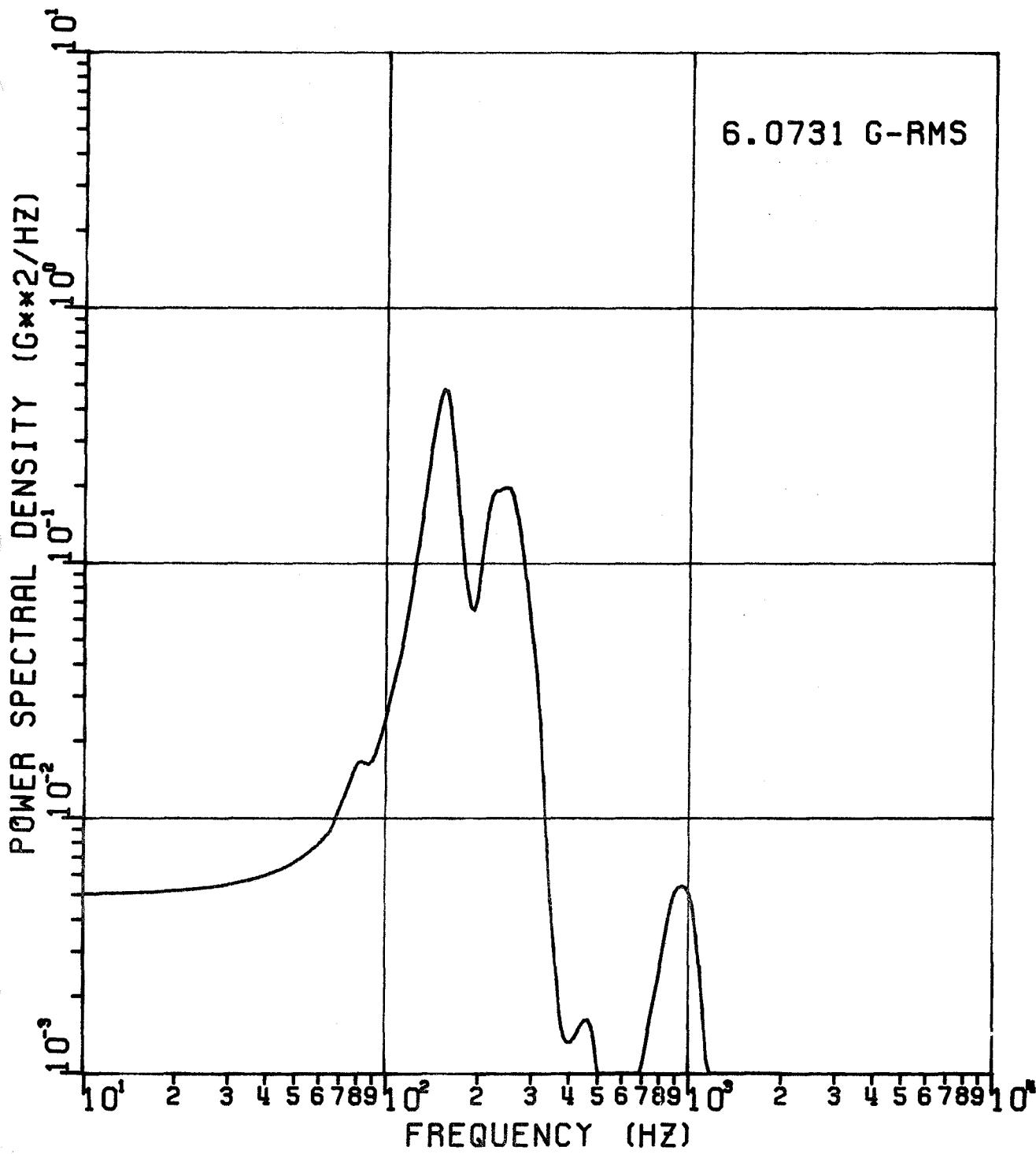
LOCATION 15



1 Z AXIS SUBPACK 3 SEP 1970

## FIGURE 28C RANDOM VIBRATION SPECTRUM

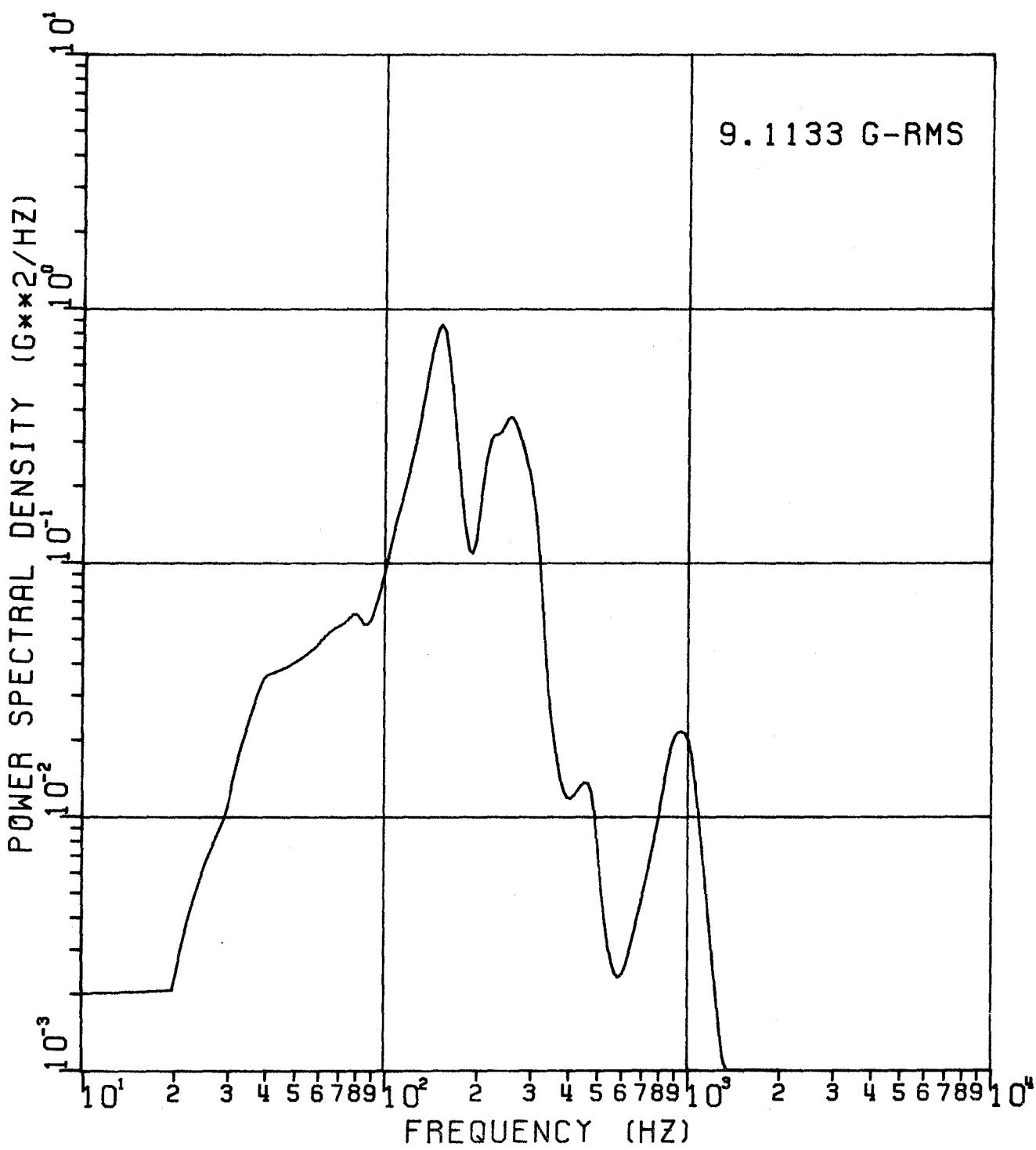
LOCATION 15



1 Z AXIS SUBP. 3 SEP 70 NEW LEVELS

## FIGURE 29 d RANDOM VIBRATION SPECTRUM

LOCATION 15



S 3 LOADS

LEVELS

T 3

## ROOT MEAN SQUARE--COMBINED LOADS

## X-AXIS

## DEFLECTIONS - IN.

	INTERNAL LOADS - LB.
1 C.7054701D-02	0.2319968D 03
2 C.4608755D-02	0.2609940D 02
3 C.2559569D-02	0.2688653D 02
4 C.3122792D-02	0.4449155D 02
5 C.0.1220524D-02	0.2685657D 02
6 C.0.1417060D-02	0.1221506D 03
7 C.7056074D-02	0.8550271D 02
8 C.1493043D-02	0.2609940D 02
9 C.1026659D-02	0.4449155D 02
10 C.2928775D-02	0.8378591D 02
11 C.2728582D-03	0.2685657D 02
12 C.8744010D-03	0.6900272D 02
13 C.1521901D-02	0.2519445D 02
14 C.1985436D-02	0.2551793D 02
15 C.3119573D-02	0.5664197D 02
16 C.0.1183953D-02	0.2524956D 02
17 C.1273187D-02	0.2707783D 02
18 C.1493043D-02	0.2704213D 02
19 C.1026859D-02	0.4602286D 02
20 C.2928775D-02	0.8390648D 02
21 C.2728582D-03	0.2724551D 02

## Y-AXIS

## DEFLECTIONS - IN.

	INTERNAL LOADS - LB.
1 C.1391058D-C2	0.4548761D 02
2 C.9295478D-03	0.10546100 02
3 C.3957980D-02	0.2359141D 02
4 C.2534793D-02	0.2278111D 02
5 C.1519744D-02	0.3095613D 02
6 C.6548C87D-04	0.5644452D 01
7 C.9375525D-02	0.1124881D 03
8 C.5625381D-03	0.10546100 02
9 C.1401983D-02	0.2278111D 02
10 C.3948728D-02	0.1070323D 03
11 C.4627058D-03	0.3095613D 02
12 C.4254323D-03	0.3251171D 02
13 C.7435613D-03	0.1237598D 02
14 C.8314524D-03	0.1000171D 02
15 C.1264849D-02	0.2247157D 02
16 C.60342C2D-03	0.1037646D 02
17 C.5822539D-03	0.1160442D 02
18 C.5625381D-03	0.1067412D 02
19 C.1401983D-02	0.2299541D 02
20 C.3948728D-02	0.107257CD 03
21 C.4627058D-03	0.3491328D 02

## Z-AXIS

## DEFLECTIONS - IN

## INTERNAL LOADS - LB

1 C.4941035D-C2	0.1615719D 03
2 C.8552128D-03	0.5212988D 01
3 C.0.15C7C73D-C2	0.1273879D 02
4 C.1577021D-C2	0.1522011D 02
5 C.0.4483461D-03	0.9778412D 01
6 C.0.1865445D-C3	0.1611462D 02
7 C.0.2992364D-02	0.354264D 02
8 C.0.3586161D-03	0.5212988D 01
9 C.0.4923270D-C3	0.1692591D 02
10 C.1334141D-02	0.35266C8D 02
11 C.0.1207562D-03	0.9778412D 01
12 C.0.1395676D-02	0.1116054D 03
13 C.0.2738530D-02	0.4920356D 02
14 C.0.3834076D-02	0.4700833D 02
15 C.0.6494432D-02	0.1152635D 03
16 C.0.1644290D-02	0.4716092D 02
17 C.0.2170335D-02	0.4698504D 02
18 C.0.3586161D-03	0.5275135D 01
19 C.0.4923270D-03	0.1693752D 02
20 C.0.1334141D-C2	0.3533946D 02
21 C.0.1207562D-03	0.9928922D 01

REFER TO TABLE 1

FOR COORDINATE DEFINITIONS



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## SECTION II STRESS ANALYSIS OF A2/SP-3 FRAME ASSEMBLY

Enclosures: (1) Schematic Layout of A-2/SP-3 Frame Assembly  
(2) Results of Stress Analysis Including In-Plane and Out-of-Plane Loading Conditions

### 1.0 INTRODUCTION

A stress analysis of the subject frame assembly was performed in accordance with the requirements specified in the statement of work for the design of the A-2/SP-3.

The methods of analyses were based on BxA computer programs BSR 2909 and BSR 2910 which are rigid frame analysis and plane grid analysis programs, respectively. In addition to the computer programs, manual analyses of clips, joints, beam columns, etc. were performed.

Stiffness influence coefficients were printed out for use in the formulation of the dynamics analysis performed on the A-2/SP-3.

### 2.0 SUMMARY

The analysis shows that the design satisfies all requirements of structural integrity. Most elements of the structure have relatively low internal stress levels for all conditions of externally applied loads. Hence, cross-sectional geometry of the members was more a function of displacement limits than stress limits. The critical design loads are those acting in the plane of the frame parallel to the X-axis.

### 3.0 RESULTS

Results of the analysis are shown in Enclosure (2). A maximum displacement of 0.04 inches occurs at node 3, and a maximum bending stress of 32,500 psi occurs at node 6 on member 14. Bending stress levels between nodes are all less than the end moment acting on member 14.

The analysis without members 15 and 18 showed excessive displacements of the nodes in the middle section the frame assembly in the X-axis direction. Therefore, in order to limit these displacements members 15 and 18 were added to the structure.

The minimum margin of safety occurs adjacent to node 6 on member 14.

M. S. = 0.06 (combined bending and comp.).



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#### 4.0 DISCUSSION

Design ultimate loads were determined by multiplying the design limit loads by 20 g load factors and then applying safety factors of 1.5. Using this procedure, the following ultimate loads were determined for use in the analysis.

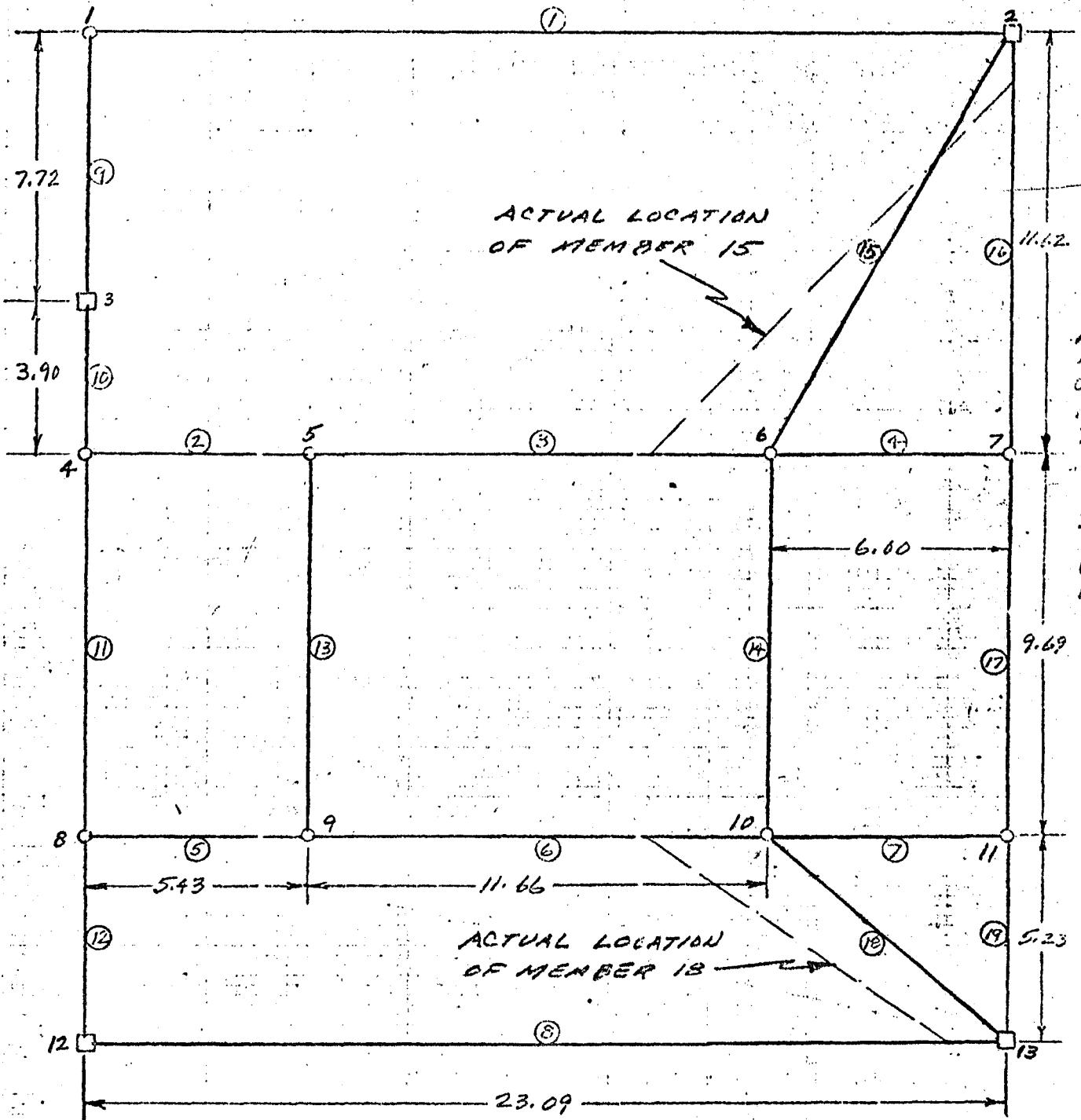
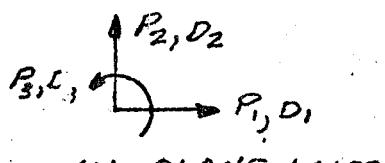
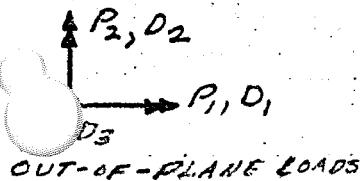
<u>Item</u>	<u>Ult. Load (lb.)</u>
ALSD	700
HFE	200
Probe Box	100

The externally applied loading conditions are defined as follows:

1. Loads applied normal to the frame parallel to the Z-axis.
2. Loads applied in the plane of the frame parallel to the X-axis.
3. Loads applied in the plane of the frame parallel to the Y-axis.

It should be noted in Enclosure (1) that the true locations of elements 15 and 18 are as indicated by the dashed lines. The analysis was performed before these members were added to the drawing. Subsequently, the problem of securing these members to nodal points 2, 6, 10 and 13 became nearly insurmountable. The dashed lines indicate the compromise locations of the members that still insures adequate strength of the frame.

The stiffness characteristics of the assembly in the Y-direction are such as to reduce stress and displacement levels to negligible values. Therefore, results of the analysis for in-plane loading parallel to the Y-axis (cond. 3) are not shown in Enclosure (2).

SCHEMATIC OF A-2/SP-3 FRAMELEGEND

- NODAL POINTS
- FIXED SUPPORT POINTS
- (①) MEMBER NUMBERS

NODAL FORCES & DISPLACEMENTS

LOADING CONDITION NO. 1

MEMBER FORCES AND STRESSES

MEMBER	BENDING MOMENTS		TORSIONAL MOMENT	BENDING STRESSES		TORSIONAL STRESS			
	@ Low Node No.	@ High Node No.	F1	F2	F3	S1	S2	S3	= $F_S Q / I$
1	0.1120	103.1264	-0.0732	.1.2977	1194.9128	-49.7058			
2	1.5273	428.1563	-1.2798	3.6463	2423.8071	-358.3564			
3	-428.0586	184.8459	0.6940	-1665.8428	719.3508	135.0206			
4	160.9023	0.4570	-1.5662	910.8735	2.5873	-438.5317			
5	-0.2227	470.4297	0.4892	-1.2605	2663.1187	136.9625			
6	-470.5012	313.9524	-1.5512	-1831.0134	1221.7844	-262.8748			
7	40.2625	-0.5720	-0.0212	256.0232	-3.6374	-11.4433			
8	0.0	0.0	0.1345	0.0	0.0	91.3261			
9	0.0784	-34.5881	0.1119	0.9081	-400.7681	75.9493			
10	34.6328	2122.8086	-1.2239	78.7109	4824.5525	-455.3398			
11	-2121.4688	1482.3555	0.3001	-4821.5156	3368.9893	111.6573			
12	-1482.3372	-0.1418	0.0688	-17181.4414	-1.6435	46.7340			
13	-1.5731	1.8413	0.0730	-57.8975	54.0292	41.0091			
14	-320.9045	-35.6250	0.0993	-9680.3320	-1045.3364	51.6491			
15	658.2725	453.7236	-154.7204	5473.4414	3772.6484	-106.5751			
16	1107.2903	1273.4785	-0.0165	12630.0273	14755.6289	-11.2851			
17	-1275.3549	32.5037	0.4410	-2897.8516	73.8719	104.0734			
18	-244.5715	-812.1815	258.5760	-2033.5781	-6753.1758	178.1822			
19	-32.5474	-723.7717	-0.1209	-377.1221	-8386.2461	-82.0093			

LOADING CONDITION NO. 1

MAXIMUM BENDING STRESS # 17181.4414

NODAL DISPLACEMENTS

ASSOC. MEMBER NUMBER # 12

NODE	01	02	03
	ROTATION X-AXIS	ROTATION Y-AXIS	Z-AXIS (IN)
10	0.0032	0.0016	0.0251
2	0.0	0.0	0.0
3	0.0034	0.0	0.0
4	0.0026	0.0017	-0.0122
5	0.0004	0.0012	-0.0206
6	0.0017	0.0001	-0.0273
7	-0.0013	0.0004	-0.0290
8	-0.0005	0.0007	-0.0214
9	0.0003	0.0000	-0.0239
10	-0.0023	-0.0013	-0.0162
11	-0.0025	-0.0012	-0.0088
12	-0.0059	0.0	0.0
13	0.0	0.0	0.0

MEMBER FORCES,  
STRESSES, AND  
DISPLACEMENTS  
DUE TO OUT-OF-  
PLANE APPLIED LOADS

NODAL REACTIONS

NODE	R1	R2	R3
2	-1763.2510	61.3965	285.4443
3	0.0	-1.3358	557.6602
12	0.0	-0.6688	283.5530
13	1452.5696	442.3892	277.3789

MEMBER	BENDING MOMENTS			AXIAL FORCE			BENDING STRESSES			AXIAL STRESS			HEAR STRESS	
	@ LOW NODE NO.	@ HIGH NODE NO.	F1	F2	F3	@ LOW NODE NO.	S1	S2	S3	= (F1 + F2) / LA	S12			
1	85.8090	44.8901	-40.6694	5367.8904	2683.0837	-265.8130	38.1285							
2	-52.3295	-10.9975	-35.5078	-2600.7134	-5417.0469	-107.0480	-49.5699							
3	-180.7889	17.2726	-21.5703	-5097.4297	487.0085	-50.5969	-32.8443							
4	-210.9814	-291.4858	784.0117	-10485.5195	-14486.4922	2363.6169	-252.4707							
5	-50.2699	-61.7393	-123.5571	-2499.8455	-3068.3679	-372.4966	-62.2650							
6	-267.6196	-155.8623	-237.4548	-7545.6602	-4394.6094	-557.0134	-85.1263							
7	-246.1082	-304.7764	148.9124	-10921.9570	-13525.5742	612.8081	-377.8359							
8	0.0	0.0	26.7172	0.0	0.0	174.5220	0.0							
9	-89.8191	-224.1591	-5.8337	-5367.9570	-13398.0117	-38.1265	-265.8142							
10	19.6948	-178.2996	-171.7734	428.8354	-3882.3276	-713.9362	-164.0270							
11	230.6023	22.2639	27.9591	5021.0016	-4601.3661	210.0055	124.6076							
12	-172.9628	-97.5171	48.5689	-10338.0039	-5828.6055	317.4434	-338.0193							
13	269.7888	329.3599	-15.6853	8503.2227	9664.3516	-128.0433	521.5972							
14	1107.1187	1010.0449	-829.8032	32485.9961	29637.5781	-6765.7422	1783.5891							
15	-1098.0352	-913.4102	-1090.6597	-9130.0078	-7594.8750	-4077.2324	-574.9436							
16	-155.9194	-157.6640	146.4816	-9319.3164	-9423.5938	957.3962	-176.3524							
17	449.1504	413.4353	-107.2626	9779.0528	9002.2148	-445.8130	369.9839							
18	-608.0762	-606.8569	-1001.7683	-5056.0664	-5045.9297	-3744.9302	-570.6179							
19	-108.6589	-73.8313	-199.0759	-6494.5503	-4412.8864	-1301.1499	-228.0545							

MAXIMUM BENDING STRESS # 32485.9961  
ASSOC. MEMBER NUMBER # 14

MAXIMUM AXIAL STRESS # 6765.7422  
ASSOC. MEMBER NUMBER # 14

MAXIMUM SHEAR STRESS # 1783.5891  
ASSOC. MEMBER NUMBER # 14

#### LOADING CONDITION NO. 1

#### LOCAL DISPLACEMENTS

NODE	D1 X-AXIS (IN)	D2 Y-AXIS (IN)	D3 ROTATION Z-AXIS (RAD)
1	0.0006	-0.0006	0.0060
2	0.0	0.0	0.0
3	0.0416	0.0	0.0
4	0.0386	0.0003	-0.0021
5	0.0385	-0.0111	-0.0030
6	0.0385	-0.0139	0.0013
7	0.0399	-0.0111	-0.0001
8	-0.0016	0.0002	-0.0023
9	-0.0018	-0.0110	-0.0025
10	-0.0024	-0.0073	-0.0000
11	-0.0020	-0.0007	-0.0010
12	-0.0004	0.0	0.0
13	0.0	0.0	0.0

#### LOCAL REACTIONS

NODE	R1	R2	R3
2	-704.7139	-757.8782	-1209.0640
3	0.0	-165.9401	-204.4644
12	0.0	-48.5689	-97.5171
13	-593.2456	572.3616	-680.6877

MEMBER FORCES, STRESSES,  
AND DISPLACEMENTS DUE  
TO IN-PLANE APPLIED LOADS

LOADING CONDITION NO. 2

## MEMBER FORCES AND STRESSES

MEMBER	BENDING MOMENTS @ LON NODE No. 6 HIGH NODE No.			TORSIONAL MOMENT @ LON NODE No. 6 HIGH NODE No.			BENDING STRESSES = $F_u q / I$			TORSIONAL STRESS		
	F1	F2	F3	S1	S2	S3						
1	-0.0454	-41.8050	0.0297	-0.5260	-484.3887		20.1496					
2	0.4216	-246.4121	0.3805	2.3869	-1394.9473		106.5358					
3	246.4302	123.3945	0.5207	959.0134	480.2046		101.3008					
4	232.5273	0.3867	-0.8064	1316.3452	2.1692		-225.8104					
5	0.0291	-171.5852	-0.3624	0.1645	-971.3496		-101.4811					
6	171.5779	357.6299	-0.3104	607.7163	1391.7607		-60.3828					
7	-31.9226	-0.2817	-0.1173	-202.9413	-1.7915		-63.3421					
8	0.0	0.0	-0.0473	0.0	0.0		-32.0976					
9	-0.0310	14.0225	-0.0453	-0.3593	162.4764		-30.7880					
10	-14.0234	-994.4453	-0.4013	-31.8714	-2260.1025		-149.2925					
11	994.0508	-492.8716	0.0198	2259.2061	-1120.1624		7.3554					
12	493.2295	0.0469	0.0501	214.5044	0.131		34.4151					
13	-0.1403	-0.0522	0.0120	-4.1165	-1.5308		6.2344					
14	-204.9781	-86.0607	0.0484	-6014.6357	-2548.7353		25.4557					
15	359.3694	346.5762	-221.5371	2988.1062	2861.7324		-152.8600					
16	755.5932	868.6079	-0.0665	8759.5938	10064.4453		-45.1619					
17	-809.4231	32.4050	0.3152	-1975.9612	73.6500		117.2711					
18	-188.6124	-260.0195	279.3777	-1568.2654	-2162.0259		192.4420					
19	-32.5376	-504.8206	0.0351	-377.0083	-5849.2891		23.8036					

LOADING CONDITION NO. 1

MAXIMUM BENDING STRESS # 10064.4453 LOCAL DISPLACEMENTS  
ASSOC. MEMBER NUMBER # 16

MAXIMUM TORSIONAL STRESS #	ASSOC. MEMBER NUMBER #	NODE	C1	D2	D3
			ROTATION X-AXIS	ROTATION Y-AXIS	Z-AXIS (IN.)
225.8104	4	1	-0.0013	-C.0007	-C.0102
		2	0.0	C.0	0.0
		3	-0.0014	C.0	0.0
		4	-0.0010	C.0006	0.0049
		5	-0.0003	C.0009	0.0012
		6	C.0007	C.0011	-0.0118
		7	-0.0009	0.0015	-0.0198
		8	C.0003	C.0005	0.0077
		9	-0.0003	C.0007	0.0045
		10	-0.0010	C.0004	-0.0039
		11	-0.0017	C.0003	-0.0061
		12	C.0021	C.0	0.0
		13	0.0	C.0	C.0

## NUCLEAR REACTIONS

NODE	R1	R2	R3
2	-1176.9185	9.7723	195.6043
3	0.0	-C.3559	-200.3906
12	0.0	-C.0507	-94.5169
13	886.2275	12.3998	159.1100