

## DUST TORUS DEVELOPMENT AROUND MARS

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Small dust grains are continuously ejected from the surface of Phobos and Deimos by interplanetary particle bombardment. Recent studies (prompted in part by the Phobos 2 plasma and magnetic field measurements) have attempted to describe the expected dust grain halo comprised of these small dust particles [1, 2, 3, 4]. The torus density will be determined by the dust grain production and loss rates and is usually approximated analytically using a simple power law distribution. However, much of the dynamics and structure of the torus must be obtained using detailed orbital dynamics.

The current work models a system consisting of a Mars type planet along with two moons representing Phobos and Deimos in orbit around a Sun type star. The usual gravitational forces are taken into account (including the  $J_2$  component of the Martian gravity) as well as the solar radiation force. Dust grains with radii varying between 100  $\mu\text{m}$  to 5  $\mu\text{m}$  are injected into the system and their orbital trajectories tracked. Several different numerical methods (3rd, 4th & 5th order Runge-Kutta) have been employed in an attempt to optimize CPU time constraints with numerical accuracy. The acceleration to the particle due to gravitational forces (excluding the  $J_2$  component of the Martian gravity for the moment) is given by

$$\ddot{\mathbf{x}}_i = \sum_{\substack{k=1 \\ k \neq i}}^{n-1} Gm_k \left( \frac{\mathbf{x}_k - \mathbf{x}_i}{|\mathbf{x}_k - \mathbf{x}_i|^3} - \frac{\mathbf{x}_k}{|\mathbf{x}_k|^3} \right) - G(m_n + m_i) \frac{\mathbf{x}_i}{|\mathbf{x}_i|^3}$$

where that due to the radiation forces is

$$\ddot{\mathbf{x}} = \left( \frac{GM_s \beta}{r^2} \right) \left[ \left( 1 - \frac{\dot{r}}{c} \right) \hat{\mathbf{u}}_r - \frac{\bar{\mathbf{v}}}{c} \right]$$

where  $\dot{r}$  is the radial velocity,  $\hat{\mathbf{u}}_r$  is the direction to the Sun,  $c$  is the speed of light,  $\beta$  is the ratio of radiation force to gravitational force,  $G$  is the gravitational constant and  $M$  represents the mass of the Sun [5]. Calculations were made with dust particles of varying radii, densities of 3  $\text{g/cm}^3$  and varying  $\beta$  values.

Several interesting results have been obtained and are illustrated below in Figures 1 - 4. Additional results (as well as a detailed analysis) will be presented in a forthcoming publication.

**References:** [1] Juhasz, A. and Horanyi M. (1995) JGR, 100, E2, 3277-3284.

[2] Horanyi, M. et al. (1991) JGR, 96, A7, 11283-11290.

[3] Kholshchevnikov, K.V. et al. (1993) Icarus, 105, 351-362.

[4] Juhasz, A. et al. (1993) JGR, 98, E1, 1205-1211.

[5] Witner, A., (1947), The Analytical Foundations of Celestial Mechanics, Princeton University Press, Princeton, New Jersey.

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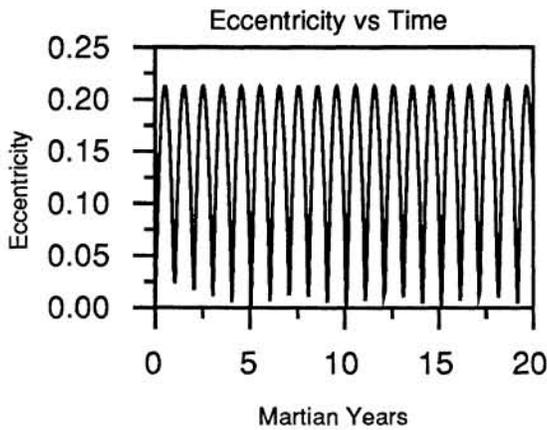


Fig. 1. The eccentricity of a 50  $\mu\text{m}$  particle released along the orbit of Deimos and under the influence of the gravity of Mars and solar radiation pressure. The particle was tracked for 20 Martian years

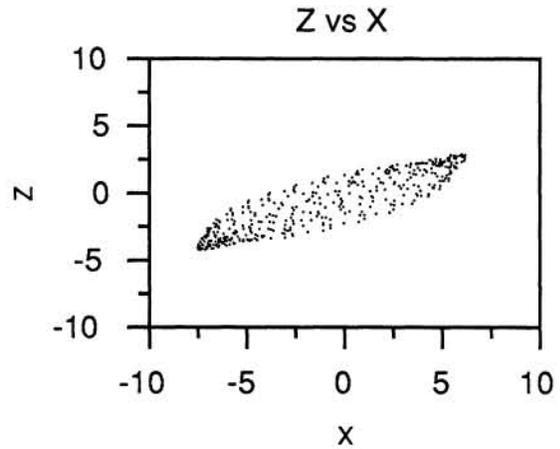


Fig. 2. A position plot of the same particle as in figure 1 in the X-Z plane. Z is the distance above the ecliptic plane defined by the orbit of Mars.

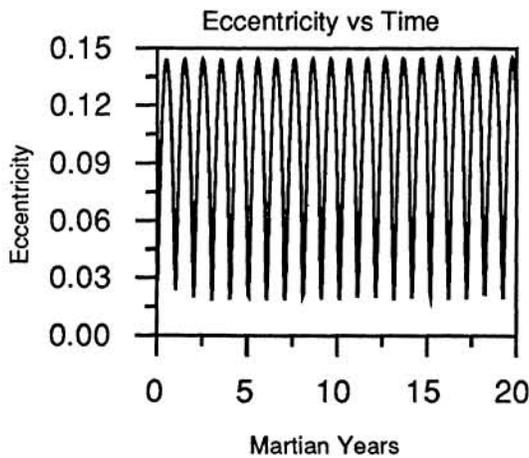


Fig. 3. The eccentricity of a 50  $\mu\text{m}$  particle released from the orbit of Phobos and tracked for 20 Martian years. Only Martian Gravity and solar radiation pressure act on the particle.

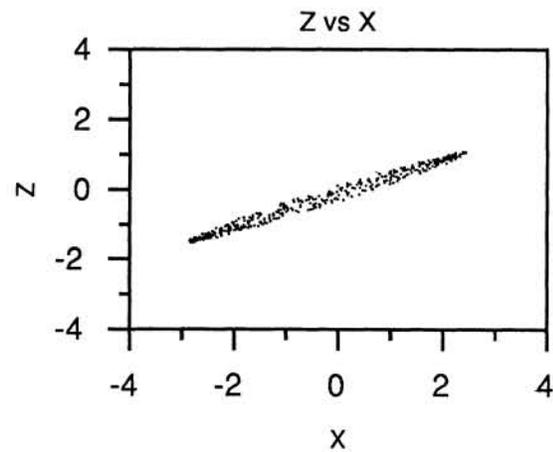


Fig. 4. The particle's cross-section in the X-Z plane. The conditions are the same as in Figure 3.