



Aerospace
Systems Division

ALHT Support Pin Design Analysis

NO.

ATM-794

REV. NO.

PAGE 1 OF 2

DATE 13 August 1968

ALHT SUPPORT PIN
DESIGN ANALYSIS

A redesign of the ALHT support pin has been accomplished. The strength of the pin has been effectively increased by approximately 60%, which will preclude failure of the pin in future tests.

Prepared by:

B. King
B. King

Prepared by:

E. Loverich
E. Loverich

Approved by:

M. Katz
M. Katz



Aerospace
Systems Division

ALHT Support Pin Design Analysis

NO. ATM-794 REV. NO.
PAGE 2 OF 2
DATE 13 August 1968

During the design limit test of the ALSEP Subpack II qualification model one of the ALHT support pins (Part No. 2333306) failed. Specifically, the failure occurred during the z-axis sine vibration test, per test procedure TP 233438.

The cause of the pin failure is not readily discernible. The subject pin is part of a structural indeterminate system which does not lend itself to a straight forward analysis. However, since pins of identical design had previously passed a complete vibration test series, during Proto model testing it had to be concluded that even a nominal increase in pin strength would suffice. The material of the pin was changed per CRD 55377 from titaluim with an ultimate yield strength (Ftu) of 160,00 psi, to 4340 steel with a Ftu of 260,00psi.

Appendix I presents the detail stress analysis performed on this system. The principal difference between this analysis and the previous analysis performed, is in the assumption of the amount of load carried by the rear diagonal braces. From the actual design of the ALHT it becomes apparent that little load is carried by the diagonal braces, particularly during the initial deflections of the carrier. Consequently, in the current analysis it has been assumed that the total load is carried by the spherical pins. This latter assumption then being the only significant difference in the two analyses.

As shown on page 7 of Appendix I the calculated Margin of Safety (M. S.) for the titanium pin is negative 0.09. The M. S. for the steel pin is positive 0.43, as shown on page 8 of the Appendix. The M. S. of the current design is sufficiently large that a qualification test is not warrented. This contention is further supported by the test performed on the titanium pins used on the Prototype and Qualification Models. In the former the tests were successful, in the latter one of the pins failed, which corroborates the marginal condition predicated analytically in the Appendix.

APPENDIX 1

PREPARED BY ERL
 CHECKED BY _____
 REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace
Systems Division

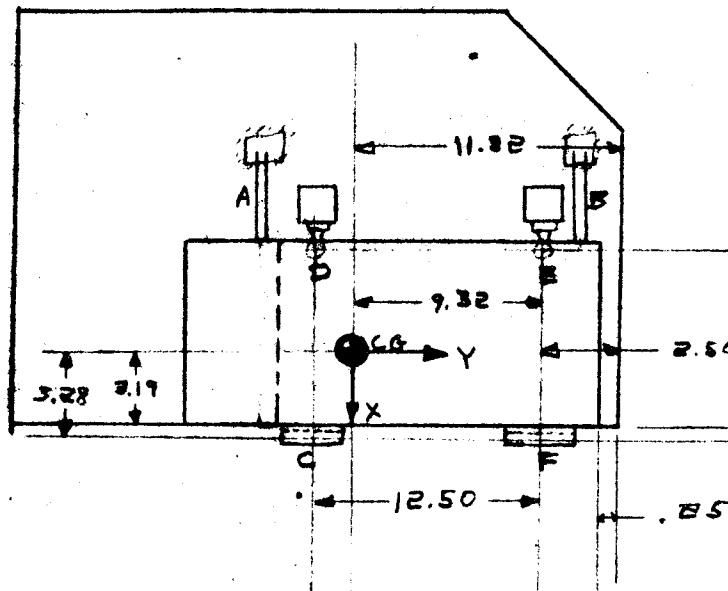
DATE 8/2/68 PAGE 1
 REPORT No. _____
 MODEL _____

ALIVE SPHERICAL PIN ANALYSIS

MATERIAL = A131 4340

F_U = 260F_{TY} = 217

$$\frac{260}{1.5} < \frac{217}{1.15}$$

ASSUME:

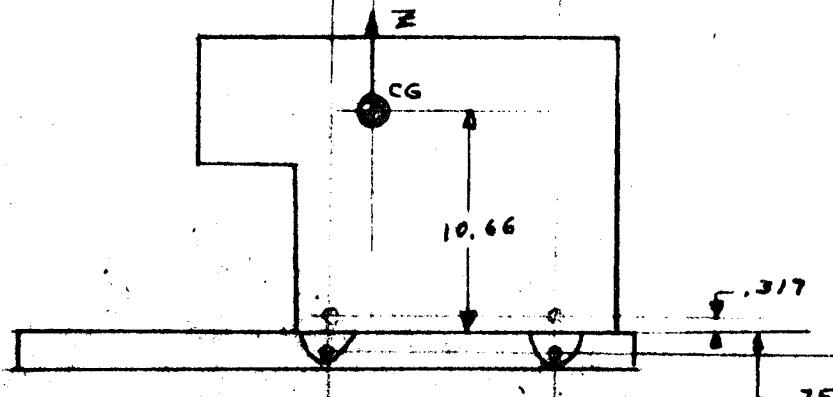
- 1) WT AT C.G. = 18.8 LB
- 2) TIE RODS A AND B SUPPORT NO LOAD SINCE IT IS POSSIBLE THAT A PIN COULD RECEIVE FULL LOAD INDEPENDENTLY OF ROD.
- 3) ULTIMATE ANALYSIS IS CRITICAL.
S.F. = 1.50
- 4) σ LOADING = 200

$$7.256 - 1.375 = 5.841$$

$$.025 + .180/2 = .085$$

LOAD AT C.G.:

$$L = (1.50 \times 20 \times 18.8) \\ = 564.0 \text{ LB}$$

FOR L ACTING IN X-DIRECTION

ASSUME NO AXIAL LOAD CARRIED.

$$M_{Ax} = \frac{9.32}{12.50} M_u, \quad M_u = 10.66 \text{ (Lx)}$$

$$L_D = \frac{M_{Ax}}{5.97 + .01} = \frac{M_{Ax}}{5.97} = \frac{9.32}{12.50} \cdot M_u \cdot \frac{1}{5.97} \\ = \frac{9.32}{12.50} \cdot \frac{10.66}{5.97} L_x$$

$$L_D = 1.33 L_x$$

PREPARED BY EBL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace Systems Division

DATE 8/8/65 PAGE 2
REPORT No. _____
MODEL _____

ALHT SPHERICAL PIN ANALYSIS

FOR L ACTING IN Y-DIRECTION

HORIZONTAL LOAD (Y) :

$$L_{DE} = \frac{3.28}{5.97} L_y$$

$$L_{Dy} = L_{DE}/2 = \frac{3.28}{5.97} \cdot \frac{1}{2} L$$

VERTICAL LOAD (Z) :

$$M_{DE} = \frac{3.28}{5.97} M_y, \quad M_y = 10.66 L_y$$

$$L_{Dz} = M_{DE}/10.50 = \frac{1}{10.50} \left(\frac{3.28}{5.97} \right) M_y$$

$$= \frac{10.66}{10.50} \left(\frac{3.28}{5.97} \right) L$$

$$L_{Dy} = .274 L$$

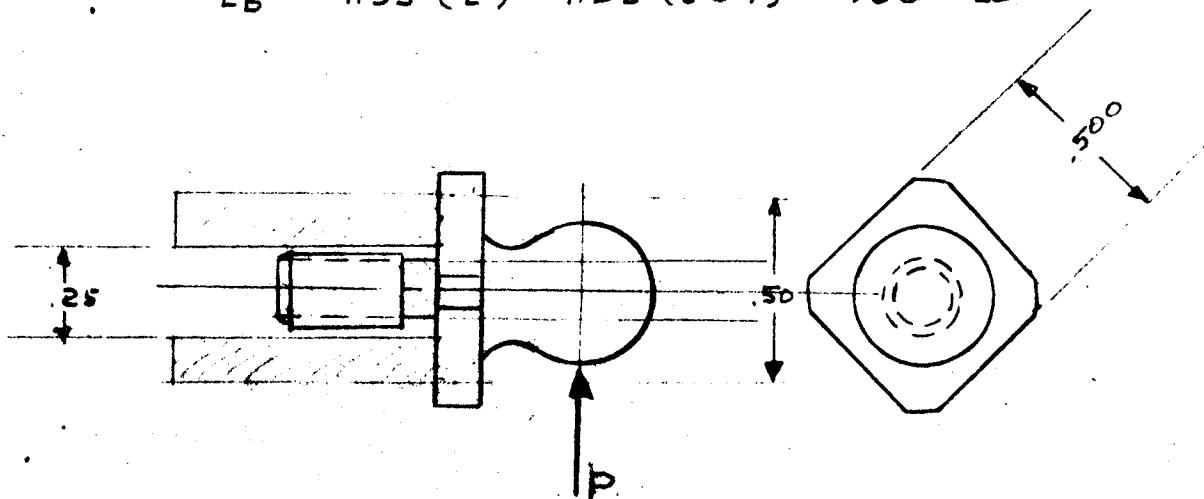
$$L_{Dz} = .468 L \quad L_{(TOT)} = L \sqrt{.274^2 + .468^2} < 1.33 L$$

FOR L ACTING IN Z-DIRECTION

IT IS OBVIOUS THAT L_0 OR L_E WILL NOT BE GREATER THAN L_D FOR L_x OR L_y .

HENCE, L ACTING IN X-DIRECTION IS CRITICAL.
AND WORST PIN LOADING IS

$$L_D = 1.33 (L) = 1.33 (564) = 750 \text{ LB}$$



CONSIDERING A 10% POSSIBLE LOCATION ERROR, OF CG,
CHANGE 9.32 TO 10% (12.50) + 9.32 = 10.57

THEN,

$$P = \frac{10.57}{9.32} (L_D) = 850 \text{ LB.}$$

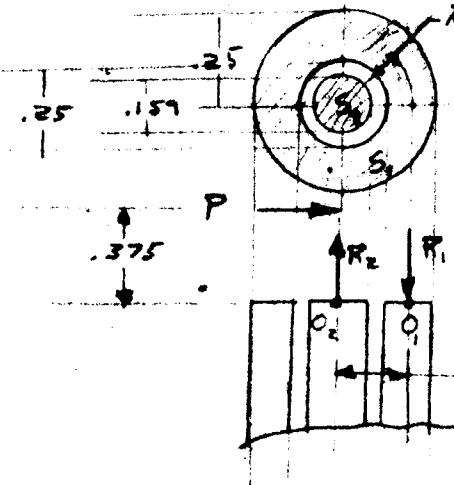
PREPARED BY EGL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace Systems Division

DATE 8/2/68 PAGE 3
REPORT No. _____
MODEL _____

AL HI SPHERICAL PIN ANALYSIS

AREA OVER WHICH MOMENT ACTS:



$$x = (.50 - .25)(\frac{2}{3})(\frac{1}{2}) = .083$$

ASSUME THAT PIN TIPS ABOUT POINT O_1 . THEN, ASSUMING NO PRELOAD, THE FORCE INDUCED AT O_1 AND O_2 IS

$$R_2 = -R_1 = \frac{.375}{.208}(P)$$

$$= 1.8P = 1.8(85) = 153 \text{ LB.}$$

$$= .083 + .125 = .208$$

PRELOADED SYSTEM W/O EXTERNAL LOAD P:

TORQUE = $\frac{80}{.20} \text{ IN-LB}$ FACTOR FOR TORQUE VARIATION SAFETY FACTOR
 $R_o = (1.80)(1.50)(560) = 1010 \text{ LB.}$ ASSUMING $K = .20$ FROM "MACH. DESIGN"

IN THE CALCULATION OF THE EFFECTIVENESS OF PRELOAD, CONSIDER

$$(1) A_1 = \frac{2}{3} S_1, E_1 = 10.3 (10^6)$$

$$A_2 = \frac{(\pi \times .159)^2}{4}, E_2 = 30.0 (10^6)$$

(2) RESULTANT OF PRESSURE RESISTED AREA ($\frac{2}{3} S_1$) ACTS AT O_2 .

THEN, THE RESULTANT LOAD ACTING ON S_2 BECOMES

$$F = \frac{k_1 R_2}{k_1 + k_2} + R_o \quad (\text{FROM M.E. DESIGN, SHIGLEY, p. 243})$$

WHERE,

$$k_1 = \frac{A_1 E_1}{L} = \frac{10^6}{L} \left(\frac{\pi}{3} \right) \left[\frac{\pi (0.50)^2}{4} - \frac{\pi (0.25)^2}{4} \right] (10.3) \\ = 1.01 (10^6/L)$$

$$k_2 = \frac{A_2 E_2}{L} = \frac{10^6}{L} \left(\frac{\pi}{4} (0.159)^2 (30.0) \right) \\ = .594 (10^6/L)$$

ASSUMING THAT BOLT HEAD IS RIGID.

$$F = \frac{(1.01)(1530)}{1.604} + 1010 \\ = 567 + 1010 \\ = 1577 \text{ LB.}$$

PREPARED BY EBL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace
Systems Division

DATE 8/16/68 PAGE 4
REPORT NO. _____
MODEL _____

ALHT SPHERICAL PIN ANALYSIS

HENCE, THE WORST LOADING CONDITION PROVIDES A TENSION LOAD OF 1577 LB. IN THE PIN SHANK. EXCLUDING STRESS CONCENTRATION, THE MAX. STRESS IS FOUND BY,

$$M = .567 (.208) = 11.8 \text{ IN-LB.}$$

$$\begin{aligned} I_{xx} &= I_o + \frac{\pi (159)^2}{4} (.208)^2 \\ &= \frac{\pi}{4} \left[\left(\frac{159}{2} \right)^4 + (.159)^2 (.208)^2 \right] \\ &= \frac{\pi}{4} (10^{-4}) (11.35) \\ &= 8.92 (10^{-4}) \end{aligned}$$

$$c = .208 + \frac{159}{2} = .288$$

$$\sigma_t = \frac{MC}{I} + \frac{P}{A} = \frac{(378)(.288)(10^4)}{8.92} + \frac{1010(4)}{\pi (.159)^2} = 38,100 + 50,800 = \underline{\underline{88,900 \text{ PSI}}}$$

CHECKING FOR SHEAR STRESS:

$$N = P = \frac{567}{159} + \frac{1010}{(\pi)(.159)} = 378 + 562 = 940$$

FROM M.E. H/B, $F_c = .61$ FOR ALUMINUM ON MILD STEEL,

$$\begin{aligned} \text{THE } F_{t,pic.} &= (61)(940) \\ &= \underline{\underline{573 \text{ LB.}}} \end{aligned}$$

$\frac{810}{573}$
 $\underline{\underline{277}}$

SHEAR FORCE $F_s = P = 850$

$$\text{AVERAGE } T_s = \frac{(850 - 573)4}{\pi (.159)^2} = \frac{(4)(277)(10^4)}{\pi (.159)^2} = 1.40 (10^7)$$

$$= 14,000 \text{ PSI.}$$

SINCE, FATIGUE IS CRITICAL IN THIS PROBLEM,

SINCE T_s IS ZERO ON SURFACE WHERE FATIGUE IS CRITICAL, AND SINCE THE BOLT IS STRONG ENOUGH IN STATIC SHEAR, SHEAR STRESS WILL THEREFORE BE NEGLECTED.

PREPARED BY EEL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace Systems Division

DATE 8/2/62 PAGE 5
REPORT NO. _____
MODEL _____

ALHT SPHERICAL PIV ANALYSIS

FATIGUE ANALYSIS

$$S_e = k_a k_b k_c k_d k_e k_f S_e'$$

S_e = CORRECTED ENDURANCE LIMIT (PSI)

S_e' = ENDURANCE LIMIT (PSI)

k_a = SURFACE FACTOR

k_b = SIZE "

k_c = RELIABILITY "

k_d = TEMP. " (0 ≤ T ≤ 120°)

k_e = MOD. FACTOR FOR STRESS CONCENTRATED

k_f = MISC. - EFFECTS FACTOR

LOADING REMOVING THE SAFETY FACTOR OF 1.50 AND ASSUMING A DYNAMIC LOADING DUE TO E8 THE FLUCTUATING STRESS BECOMES (SEE OT PG. 4),

C. T. $\left[\frac{6.0}{20} (38.1) + 50.8 \right] \frac{1}{1.50}$ OR 0 TO 41,500 PSI
AND A STEADY STATE STRESS OF

$$\frac{P}{A} = \frac{\frac{1010}{1.50} (4)}{\pi d^2} = \frac{858}{d^2} = \frac{(8.58 \times 10^{-2})}{(1.57)^2 (10^{-4})} = 3.395 (10^4)$$

$$= 34,000 \text{ PSI.}$$

HENCE,

$$\sigma_s = 34,000$$

$$\sigma_r = 41,500$$

$$\sigma_a = \frac{\sigma_r}{2} = \frac{41,500}{2} = 20,250$$

$$\sigma_m = 34,000 + 20,250$$

$$= 54,250$$

$$\frac{\sigma_a}{\sigma_m} = \frac{20,250}{54,250} = .374$$

PREPARED BY EKL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace Systems Division

DATE 8-5-8 PAGE 6
REPORT No. _____
MODEL _____

ALHT SPHERICAL PIN ANALYSIS

FOR 4340 STEEL, $S_{UT} = 260 \text{ ksi}$.

$$S_e' = 97,000 \text{ psi} \quad \text{FOR 4340} \quad S_{UT} = 260 \text{ ksi.}$$

$k_a = 1.00$ FOR PLATING (NO SCRATCHES)

$k_b = 1.05$ FOR AXIAL LOADS.

$k_c = 1 - .08 D$, FOR A SURVIVAL RATE OF 97%
 $D = 2.3$

$$= 1 - .18$$

$$= .82$$

$k_d = 1.00$ (ASSUMED)

$$k_e = \frac{1}{k_f} \quad k_f = 1 + \gamma (k_x - 1)$$

γ = NOTCH SENSITIVITY

$$\gamma = .01$$

$$\gamma = .90$$

k_x (PETROSON p. 68),

$$D = .375$$

$$d = .157$$

$$k_x = 2.20$$

$$D/d = 2.36$$

$$k_f = 1 + .90 (2.20 - 1)$$

$$\frac{r}{d} = \frac{.01}{.157} = .063$$

$$= 1 + 1.08$$

$$= 2.08$$

$$1/k_f = .481$$

$$k_e = .481$$

$k_g = .65$ (PLATING)

$$S_e = (97)(1.0)(1.0)(.82)(.481)(.65) = .256 (97) \\ = 24,850 \text{ psi}$$

FOR Ti 6AL-4V ($160 \text{ ksi} = S_{UT}$)

$$S_e = K S_e' = (.256)(80,000) \\ = 20,500 \text{ psi}$$

$$S_e' = (50)(S_{UT}) = \frac{1}{2}(160) \\ = 80 \text{ ksi}$$

PREPARED BY JBL
CHECKED BY _____
REVISED BY _____

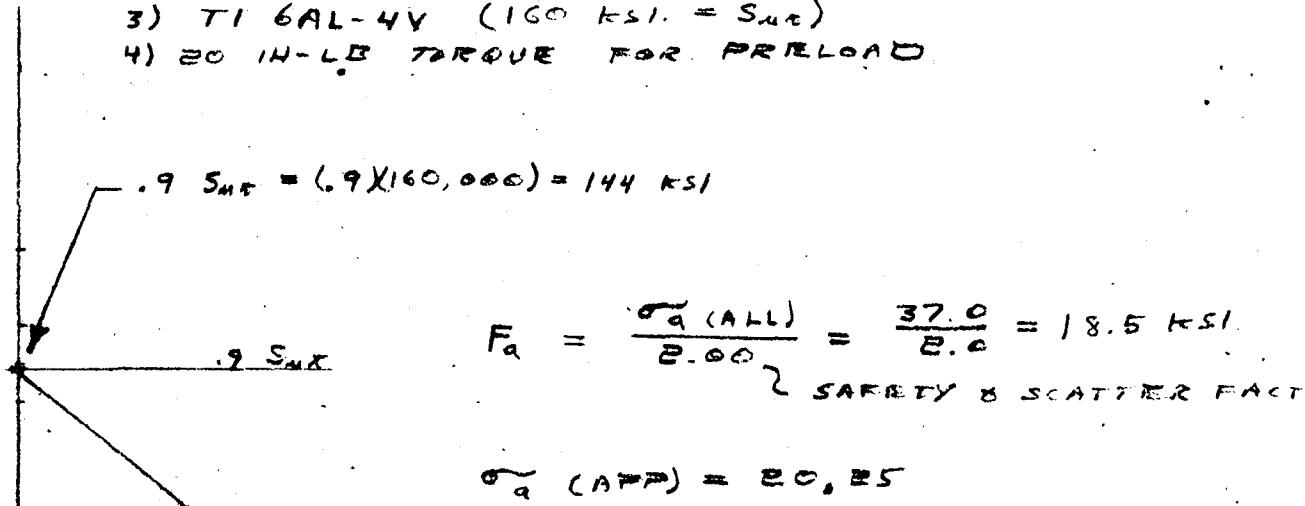
ENGINEERING REPORT
Bendix Aerospace Systems Division

DATE 8-5-8 PAGE 7
REPORT No. _____
MODEL _____

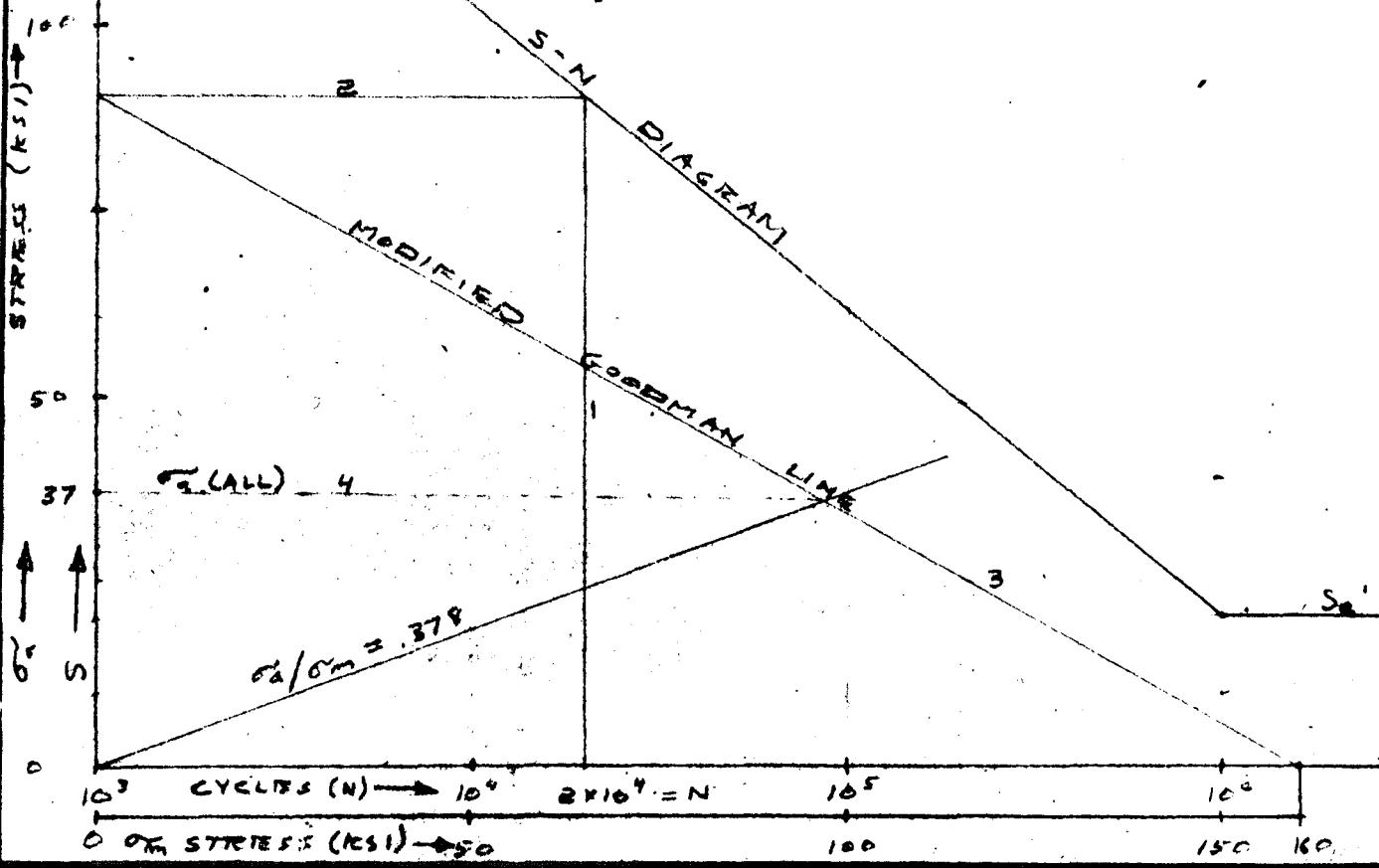
ALHT. SPHERICAL PIN ANALYSIS

FATIGUE ANALYSIS USING:

- 1) 67 DYNAMIC LOAD AT 2×10^4 CYCLES
- 2) SCATTER & SAFETY FACTOR OF 2.00
- 3) TI 6AL-4V (160 ksi. = S_{UT})
- 4) 20 IN-LB TORQUE FOR PRELOAD



$$M.S. = \frac{18.5}{20.25} - 1 = -.09$$



PREPARED BY FBL
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
Bendix Aerospace
Systems Division

DATE 8-5-88 PAGE 3
REPORT No. _____
MODEL _____

ALHT SPHERICAL PIN ANALYSIS

EATIGUE ANALYSIS USING:

- 1) G & DYNAMIC LOAD AT 2×10^4 CYCLES
- 2) 20 IN-LB TORQUE FOR PRELOAD
- 3) SAFETY & SCATTER FACTOR OF 2.0
- 4) 4340 STEEL ($260 \text{ ksi} = S_{UT}$)

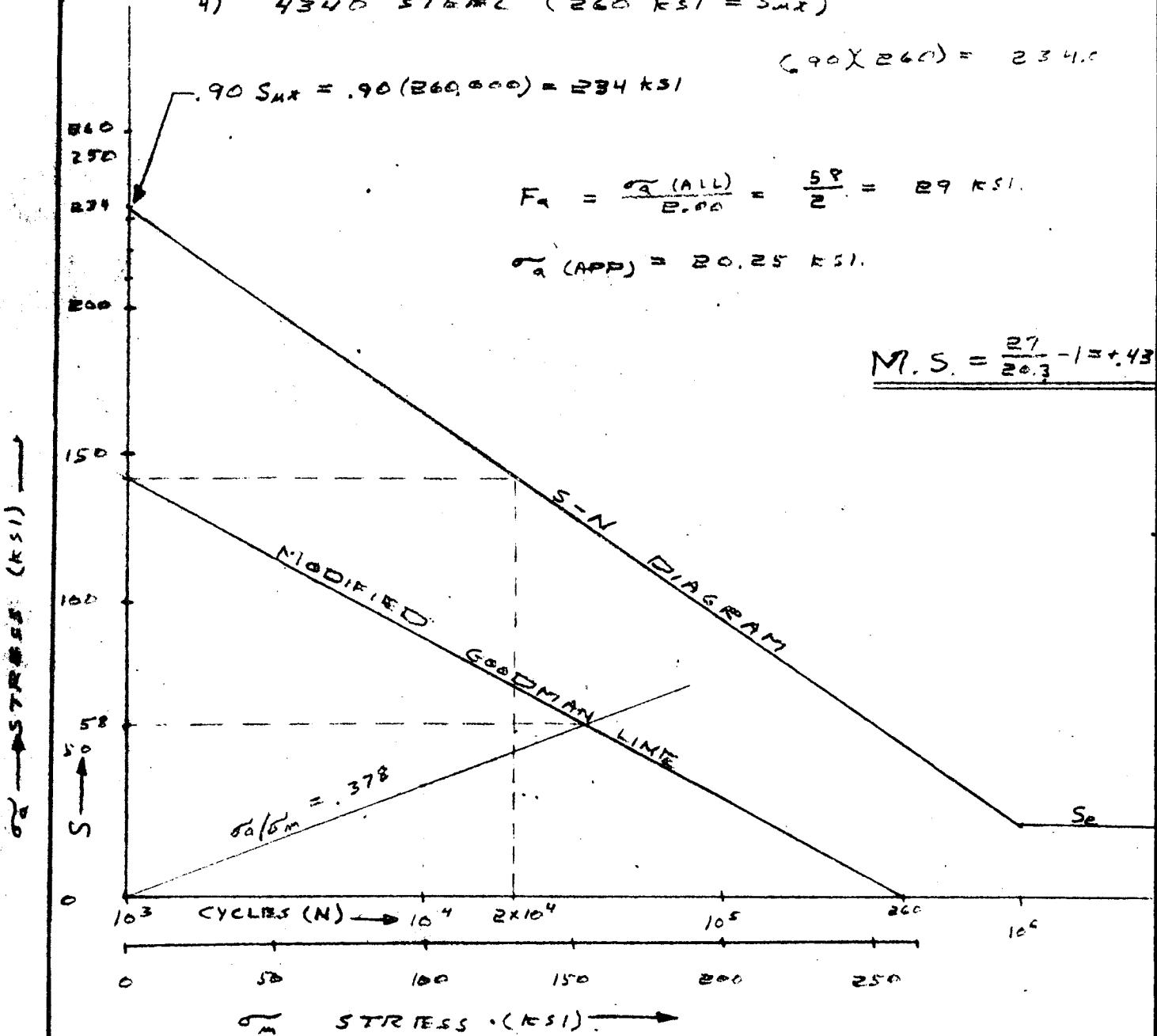
$$(.90 \times 260) = 234.0$$

$$.90 S_{UT} = .90 (260,000) = 234 \text{ ksi}$$

$$F_a = \frac{\sigma_a (\text{ALL})}{E_{\text{UT}}} = \frac{58}{2} = 29 \text{ ksi.}$$

$$\sigma_a (\text{APP}) = 20.25 \text{ ksi.}$$

$$M.S. = \frac{27}{20.3} - 1 = +.43$$



PREPARED BY EBI
CHECKED BY _____
REVISED BY _____

ENGINEERING REPORT
 Bendix Aerospace
Systems Division

DATE 8-5-8 PAGE 9
REPORT No. _____
MODEL _____

ALHT SPHERICAL PIN ANALYSIS

CONCLUSIONS

IT IS THE OPINION OF THE AUTHOR THAT THE TITANIUM PIN IS INADEQUATE AND SHOULD BE USED ONLY IN THE CASE OF FAIL-SAFE VERIFICATION BY TESTING. THE STEEL PIN, ON THE OTHERHAND, WILL BE ADEQUATE PROVIDED ALL OF THE PREVIOUS ASSUMPTIONS ARE MET BY THE MANUFACTURER. TESTING IS RECOMMENDED IF REASONABLY CONVENIENT BUT IS NOT CONSIDERED TO BE OF ABSOLUTE NECESSITY FOR THE FAIL-SAFE VERIFICATION OF THE STEEL PIN.