

# gravitational signatures of atmospheric mass transport by thermal tides on Venus

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## Sun raises two types of tides on Venus

- gravitational tide
  - larger amplitude
  - attracts mass
  - yields positive anomaly near sub-solar point
- thermal tide
  - smaller amplitude
  - heats sub-solar point
  - gas expands and moves away
  - yields negative anomaly near sub-solar point

An important, but currently unanswered, question concerning Venus atmospheric dynamics, is the following:

what is the depth profile of  
***radiative energy absorption***  
within the atmosphere?

We believe that future orbital missions, which enable gravitational monitoring of mass transport by the thermal tide, will resolve this issue

Venus has a slow, retrograde rotation.

The spin period is  $-2\pi/\Omega = 243.025 \text{ days}$

The orbit period is  $2\pi/n = 224.701 \text{ days}$

The mean solar day represents the beat  
between these input periods

$\omega = n - \Omega = 3.083 \text{ deg/day}$  so that

The sub-solar point moves East, at that rate,  
and circulates with a period of

$$2\pi/\omega = 116.752 \text{ days}$$

## Present study examines gravitational signature of thermal tide

### Approach

- use GCM to simulate atmospheric dynamics
- examine surface pressure variations over one solar day
- remove Venus-fixed average (mainly due to topography)
- back-rotate and average Sun-fixed pattern (mean thermal tide)
- examine residuals
- compute gravitational signature of thermal tide

### Conclusions

- thermal tide gravitational signature is
  - too small to have been seen previously (Magellan)
  - large enough to be easily seen by likely future missions

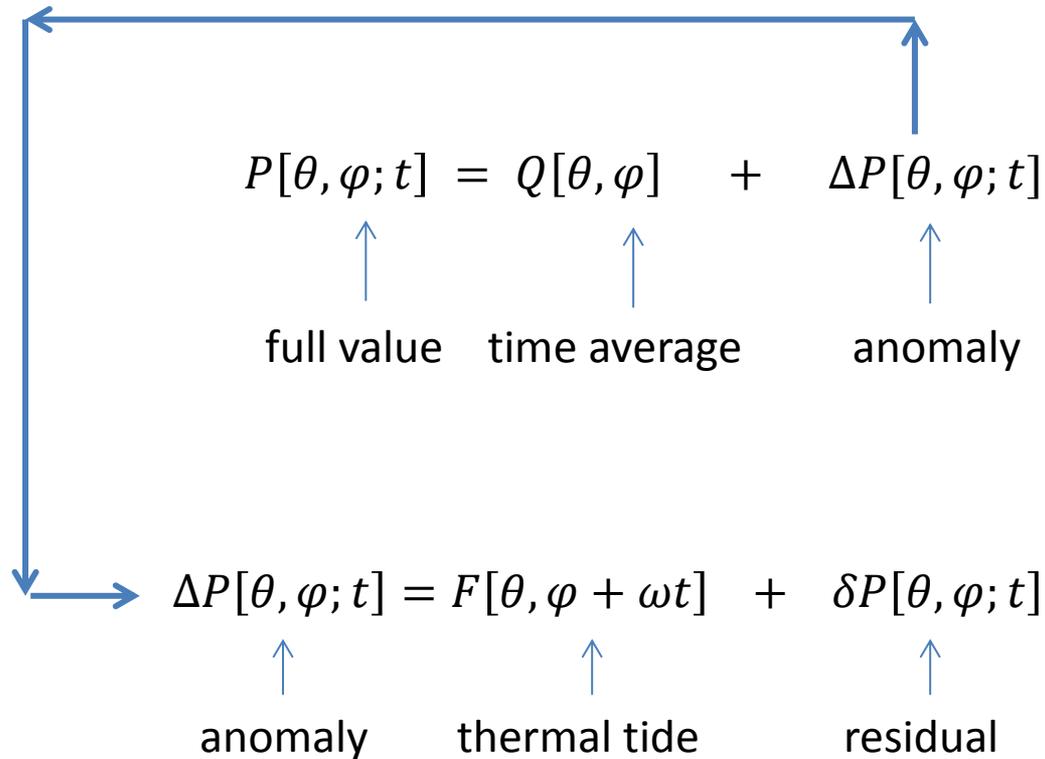
### Future Work

- constraints on key atmospheric dynamics parameters
- plausible mission designs

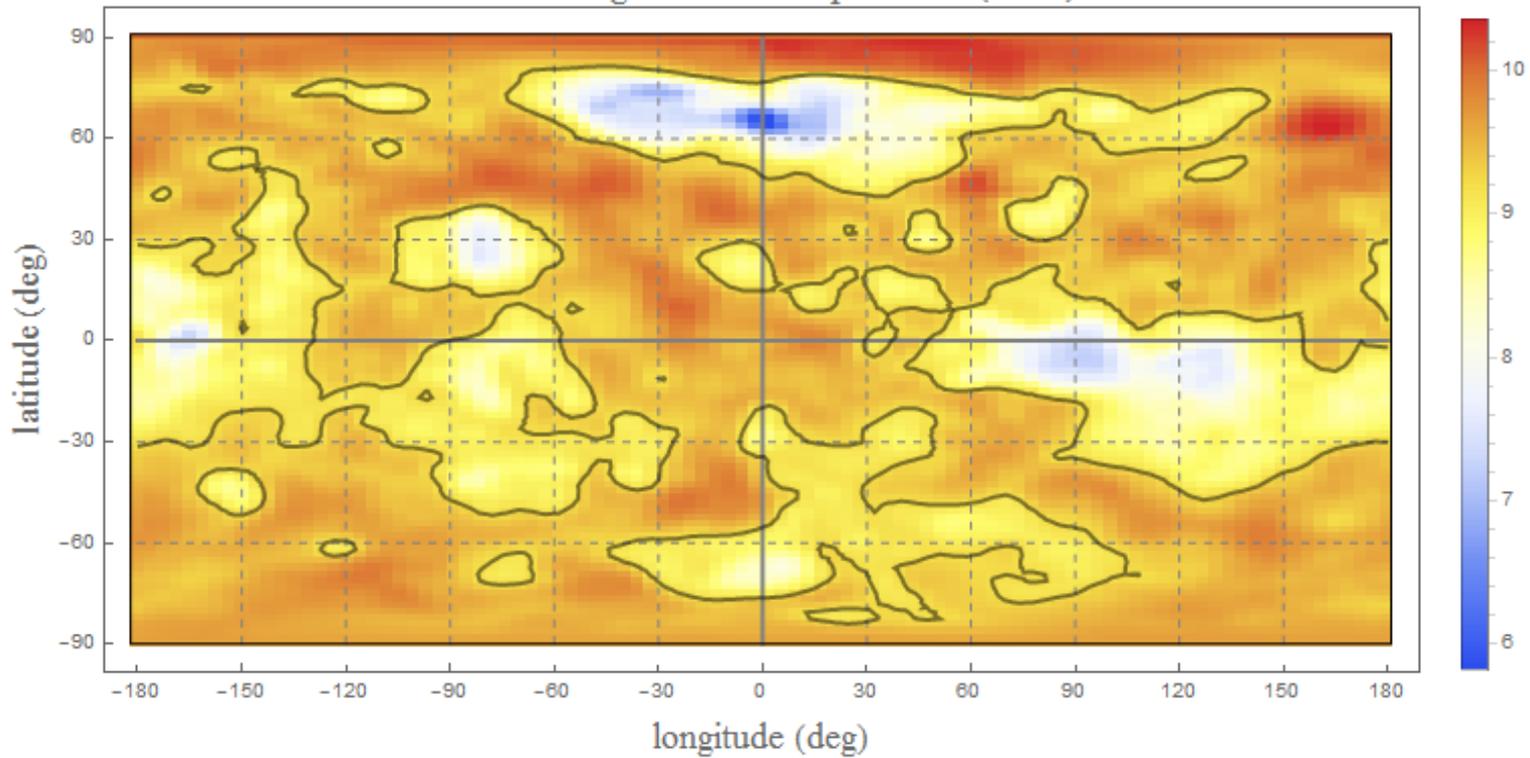
## Examine surface pressure field

- compute time average (in Venus-fixed frame)
- remove average → anomaly
- compute time average (in Sun-fixed frame)
- examine spatial pattern of thermal tide
- remove (back-rotated) thermal tide → residual

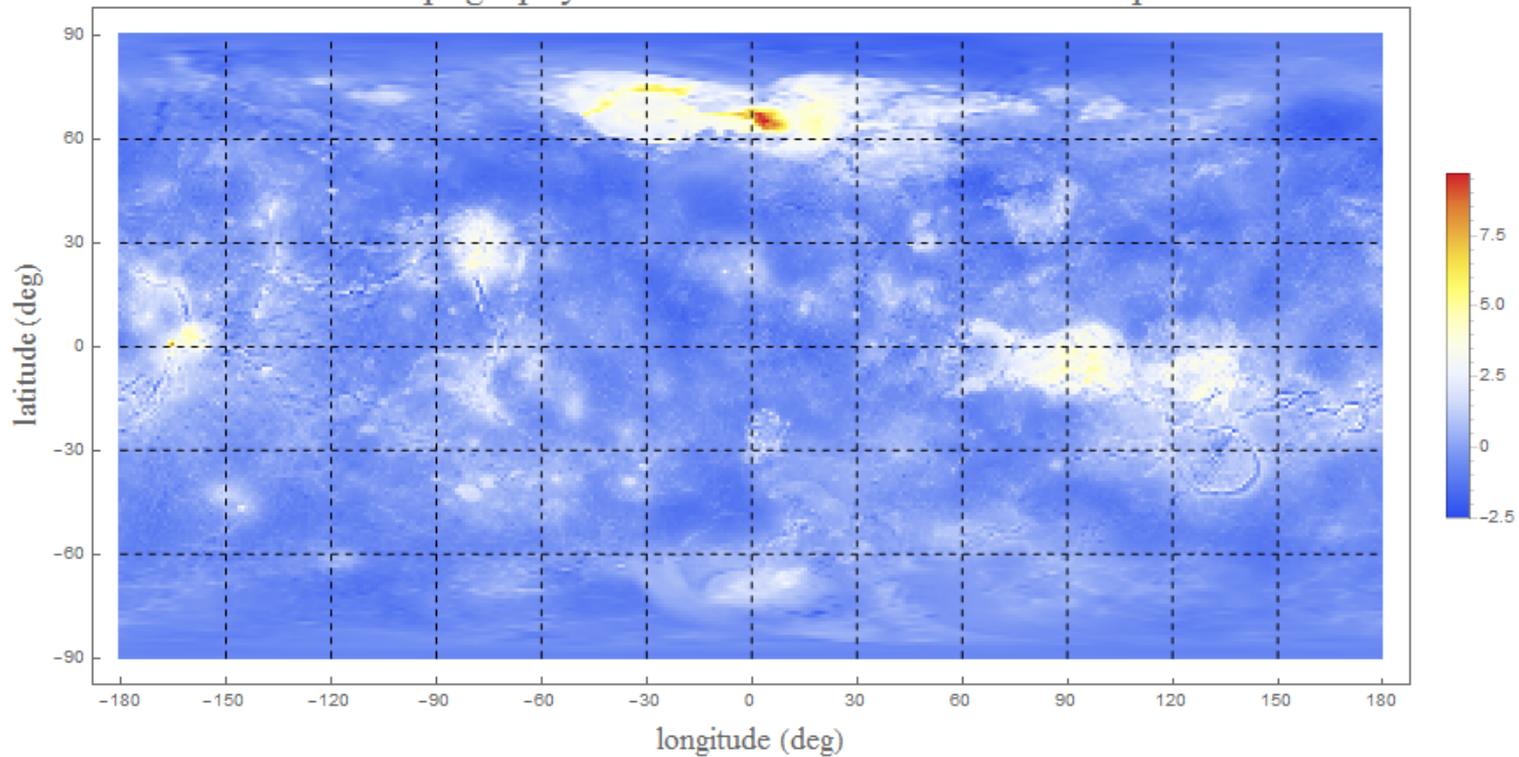
## components of the surface pressure field



time average of surface pressure (MPa)



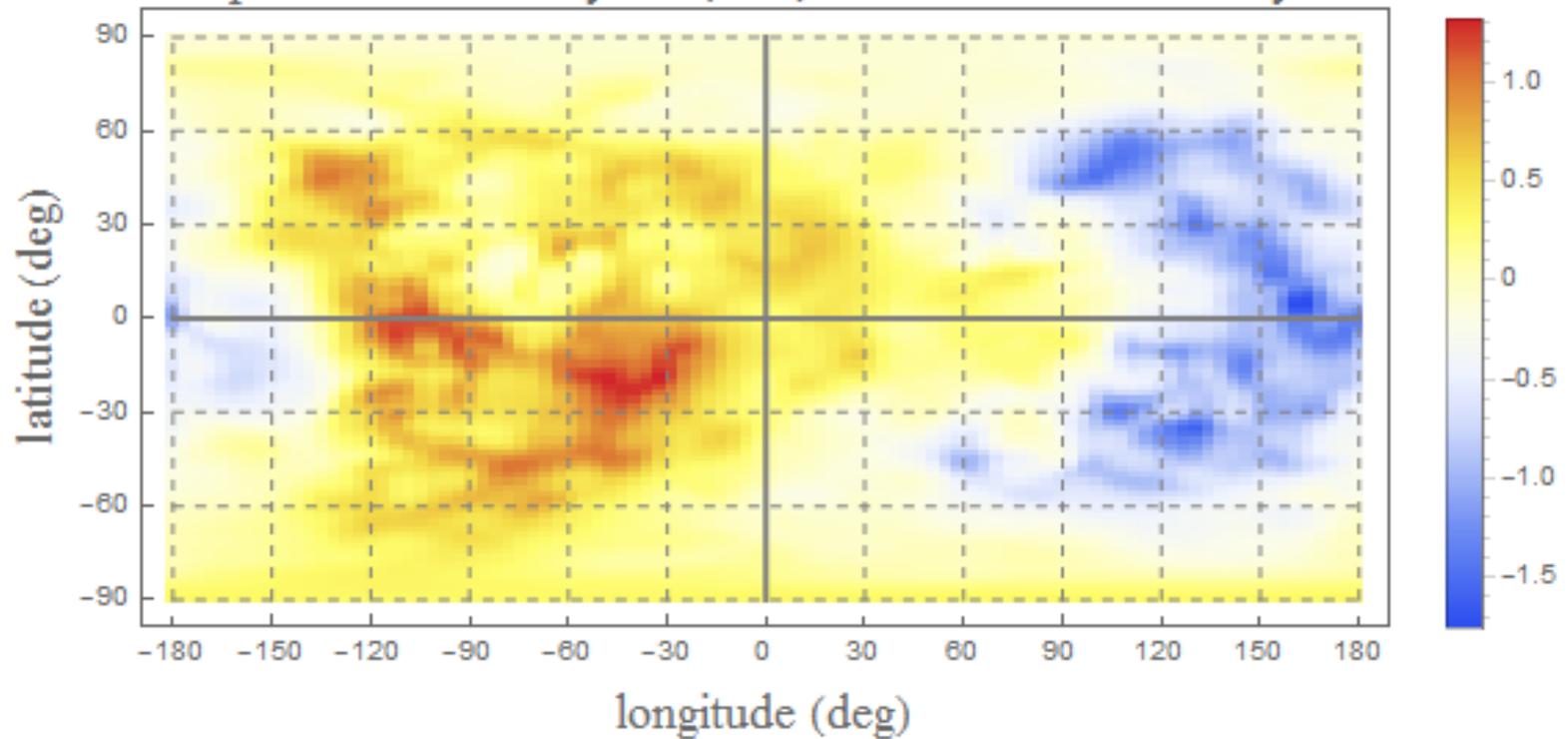
Venus topography: km relative to 6051 km radius sphere

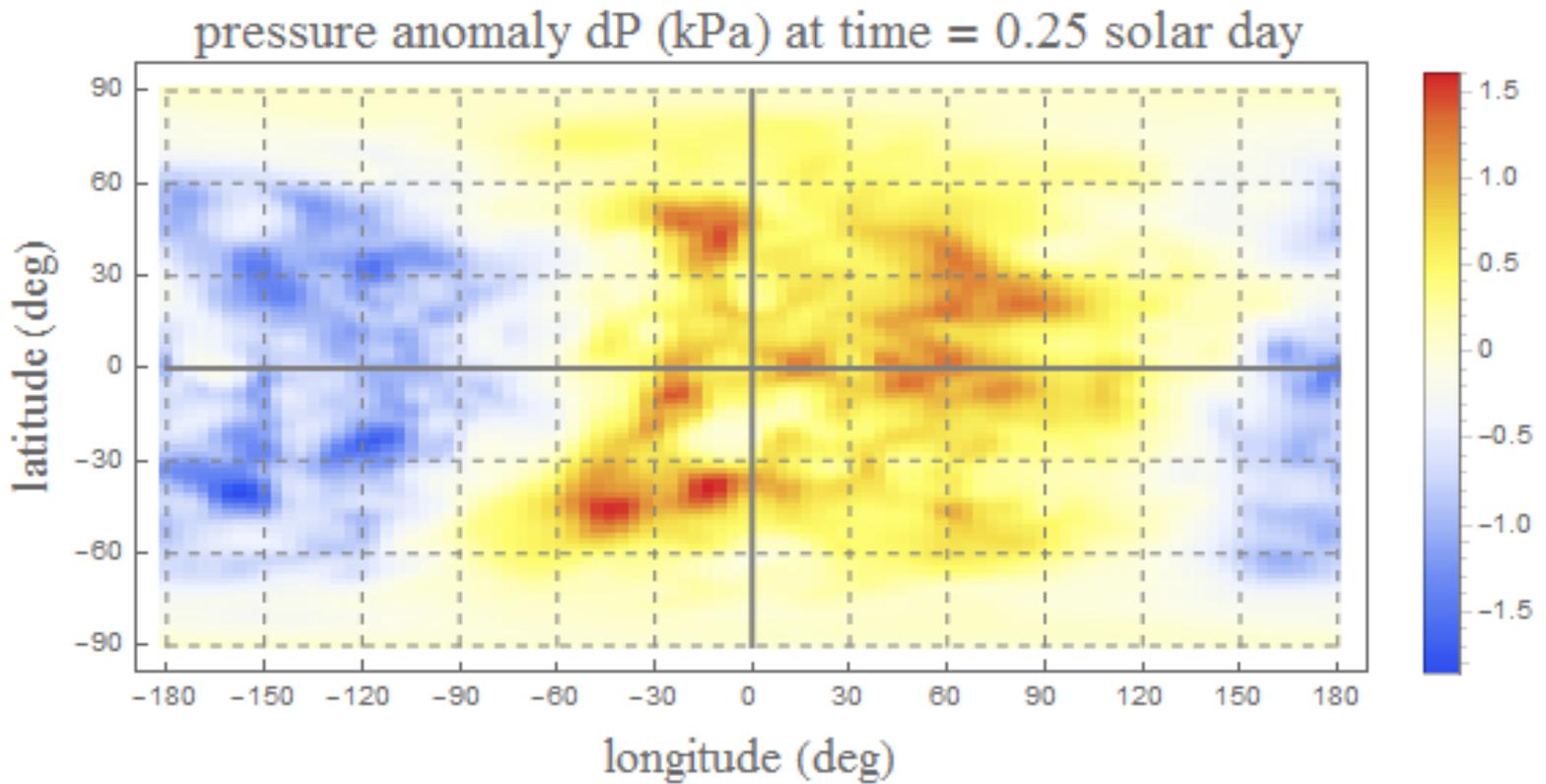


The next 4 figures show motions of the anomaly field,  
with time steps of  $\frac{1}{4}$  solar day.

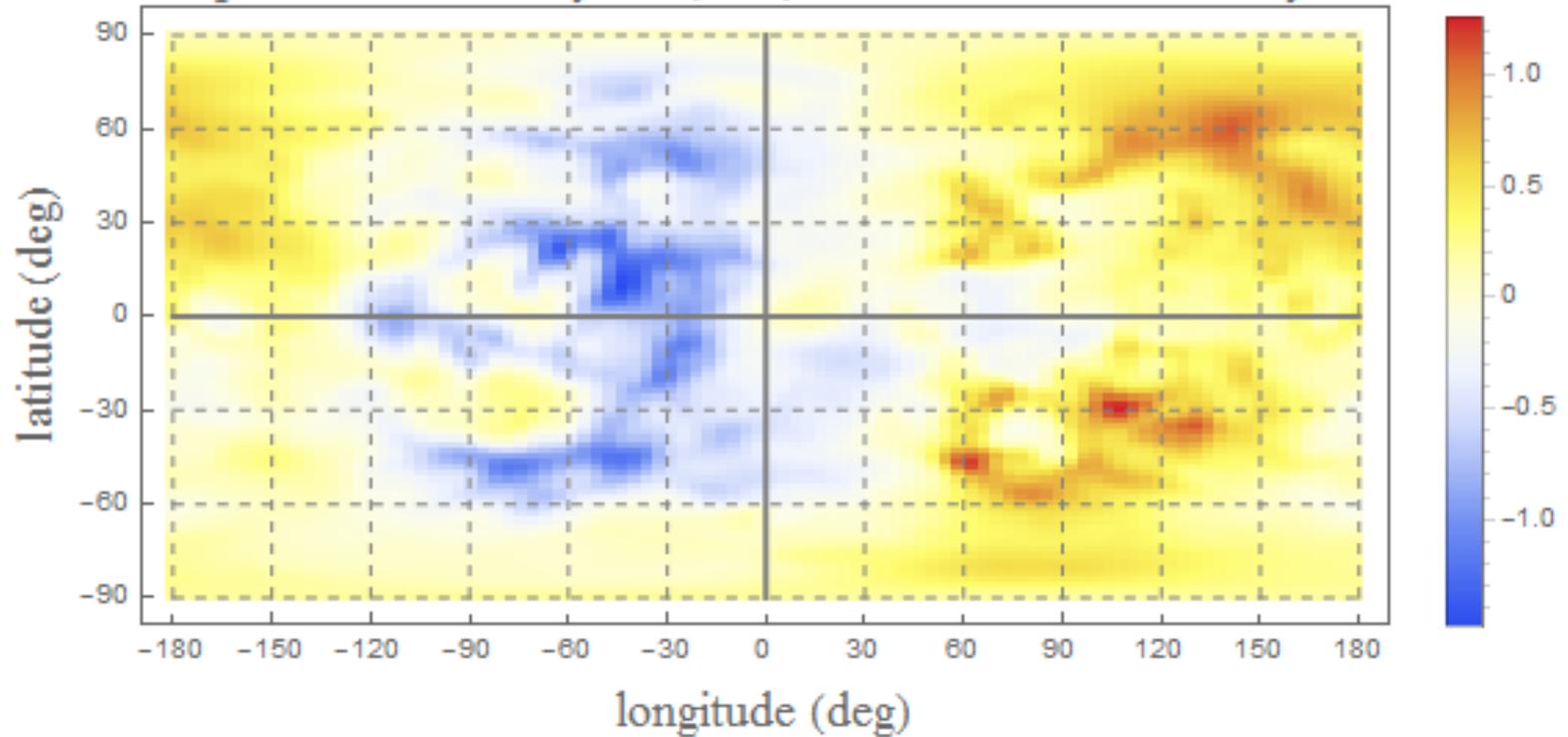
The pattern moves east, following the sub-solar point

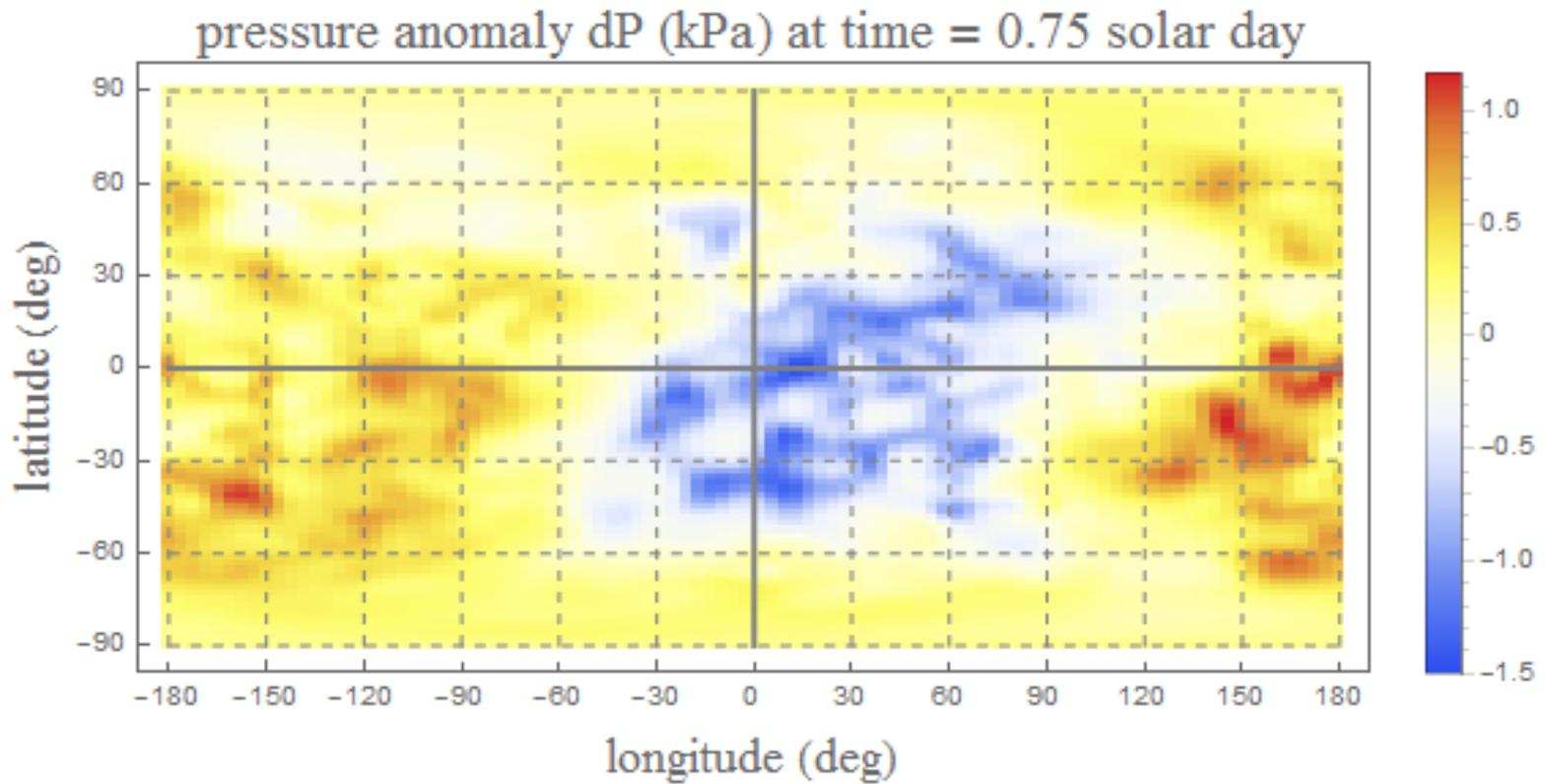
pressure anomaly  $dP$  (kPa) at time = 0. solar day





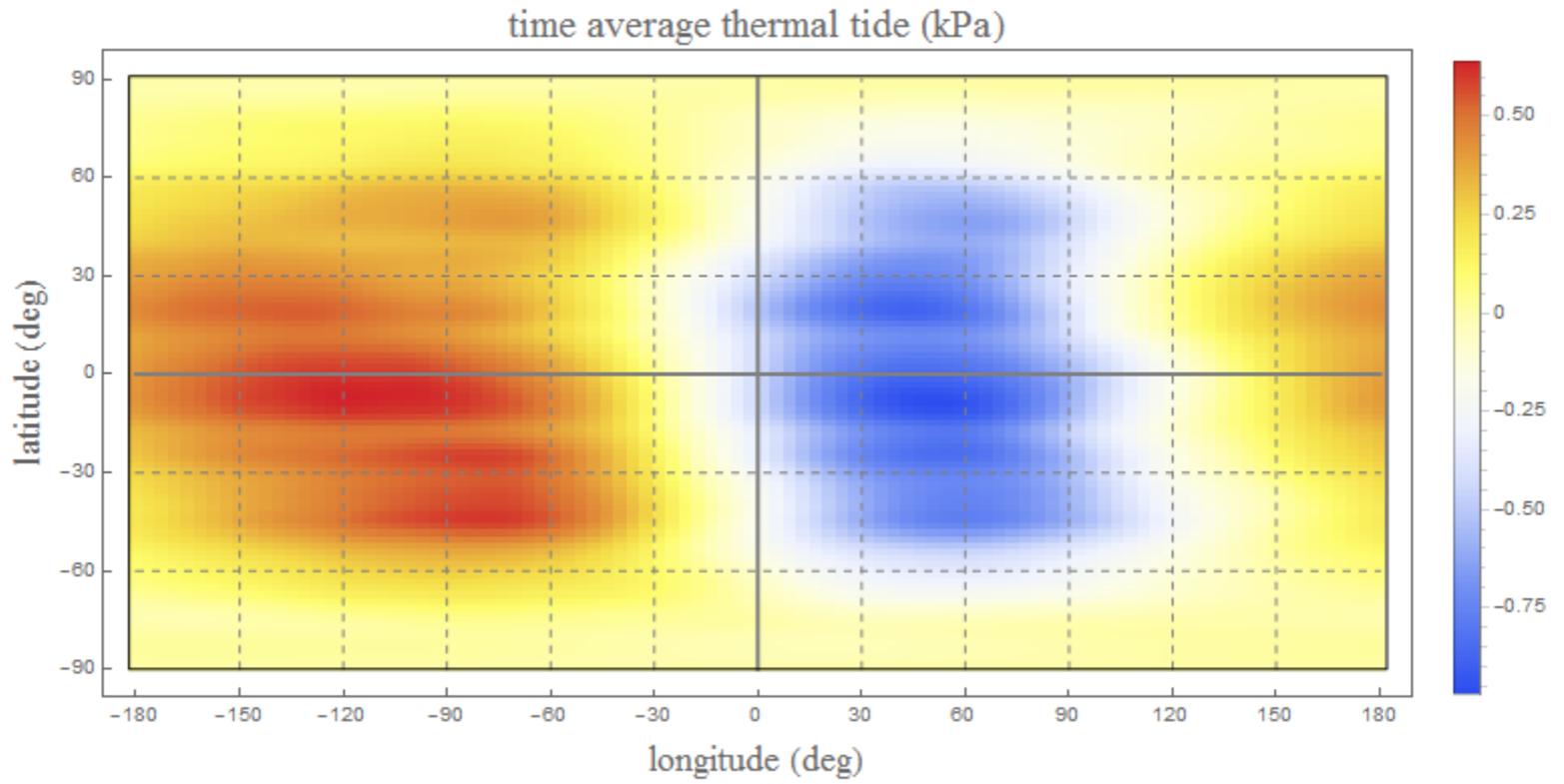
pressure anomaly  $dP$  (kPa) at time = 0.5 solar day





compute average thermal tide

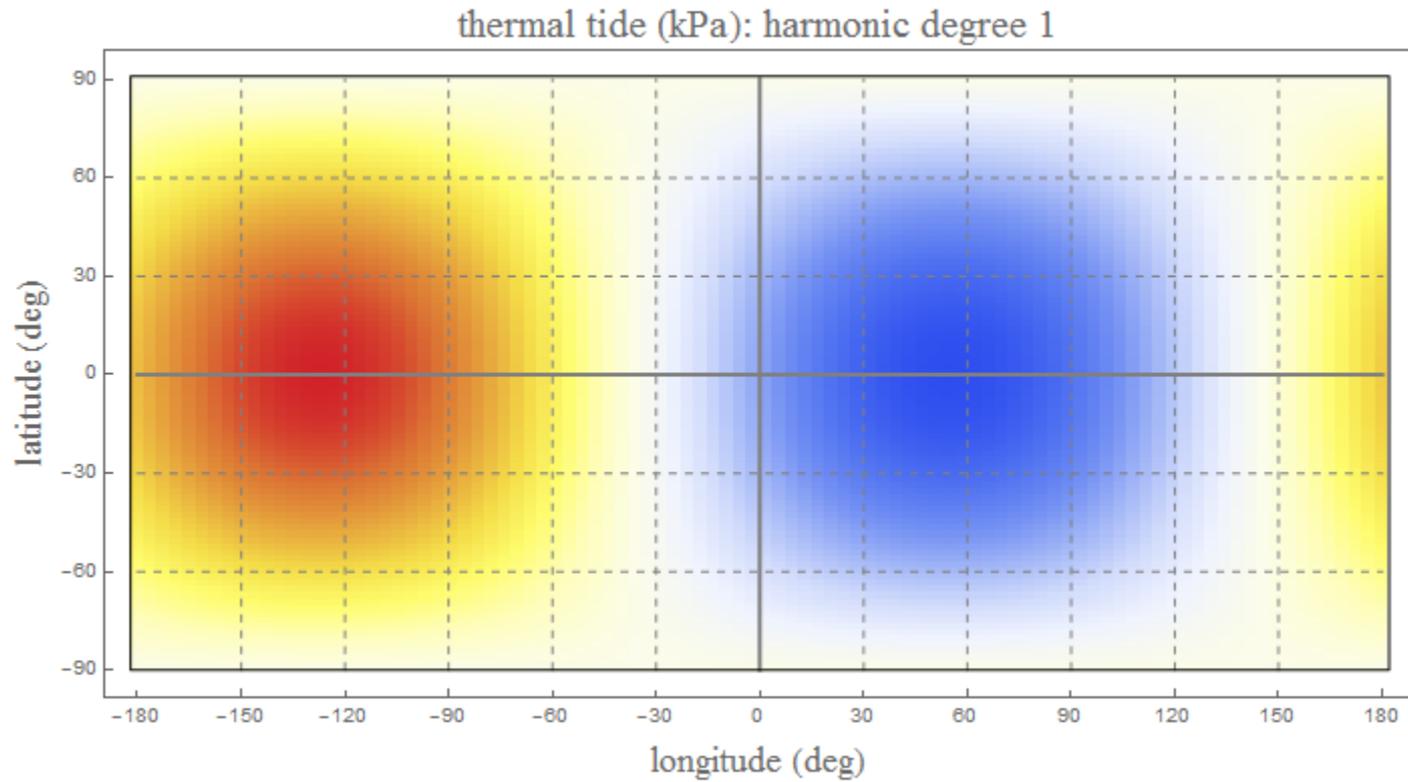
- sub-solar point moves east by 360 deg/solar day
- rotate each time-slice back to reference position
- average back-rotated values

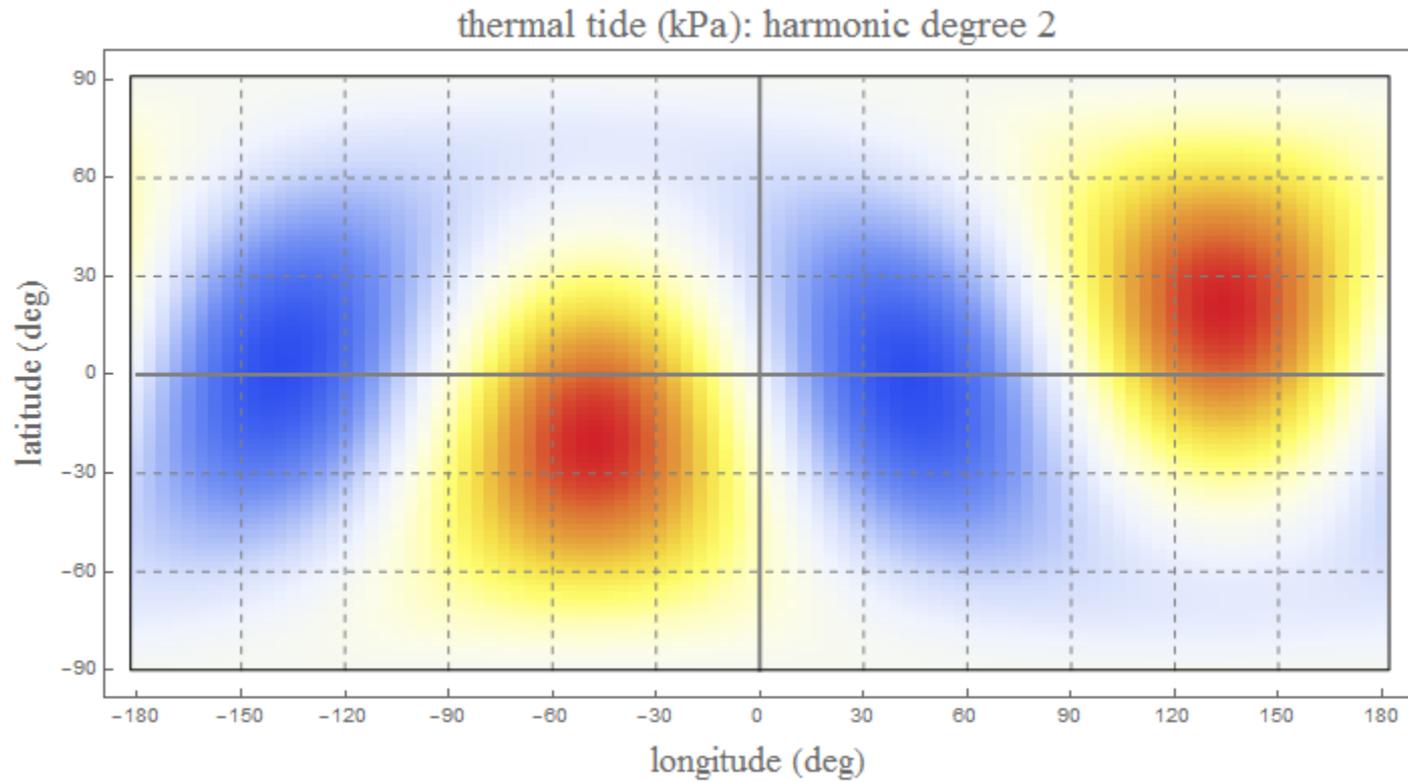


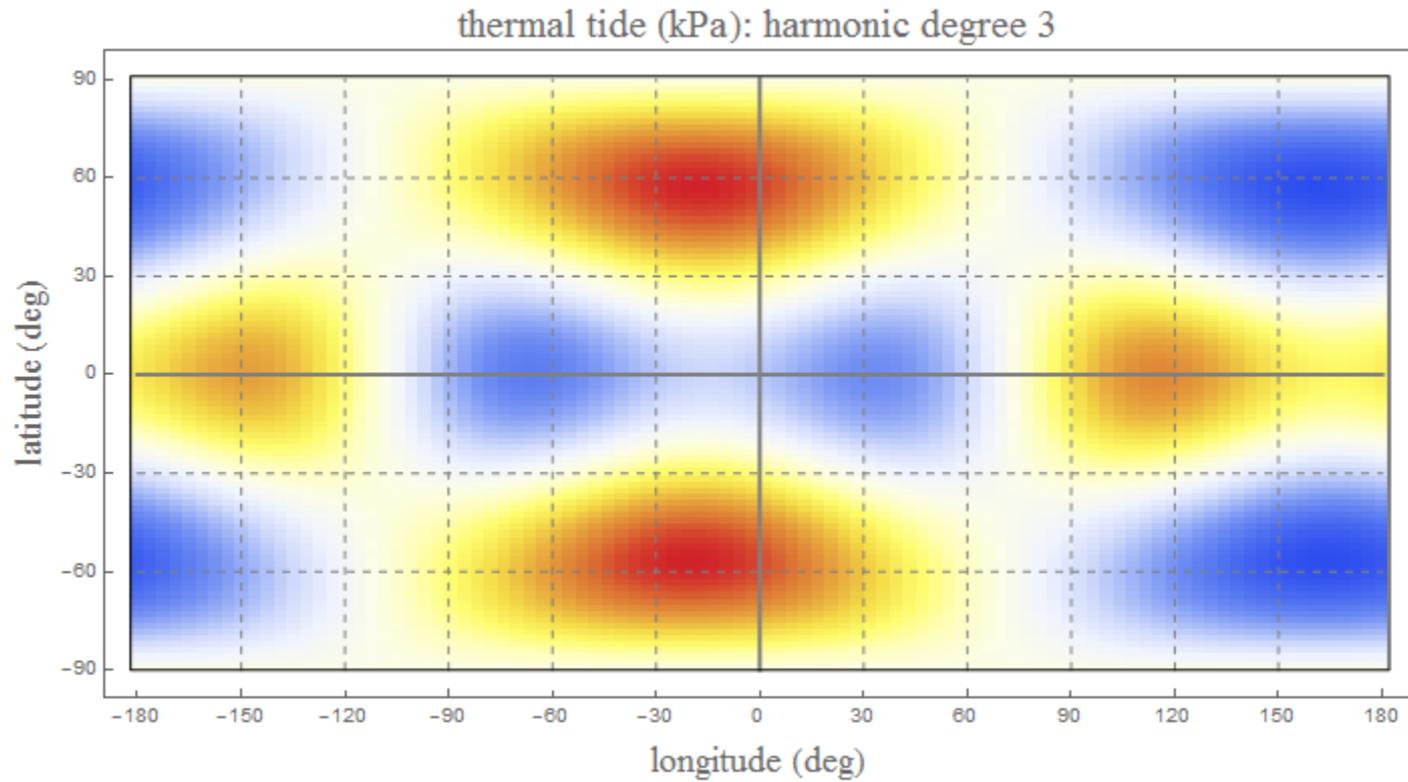
This pattern is, of course, equal to a sum of contributions from spherical harmonic functions.

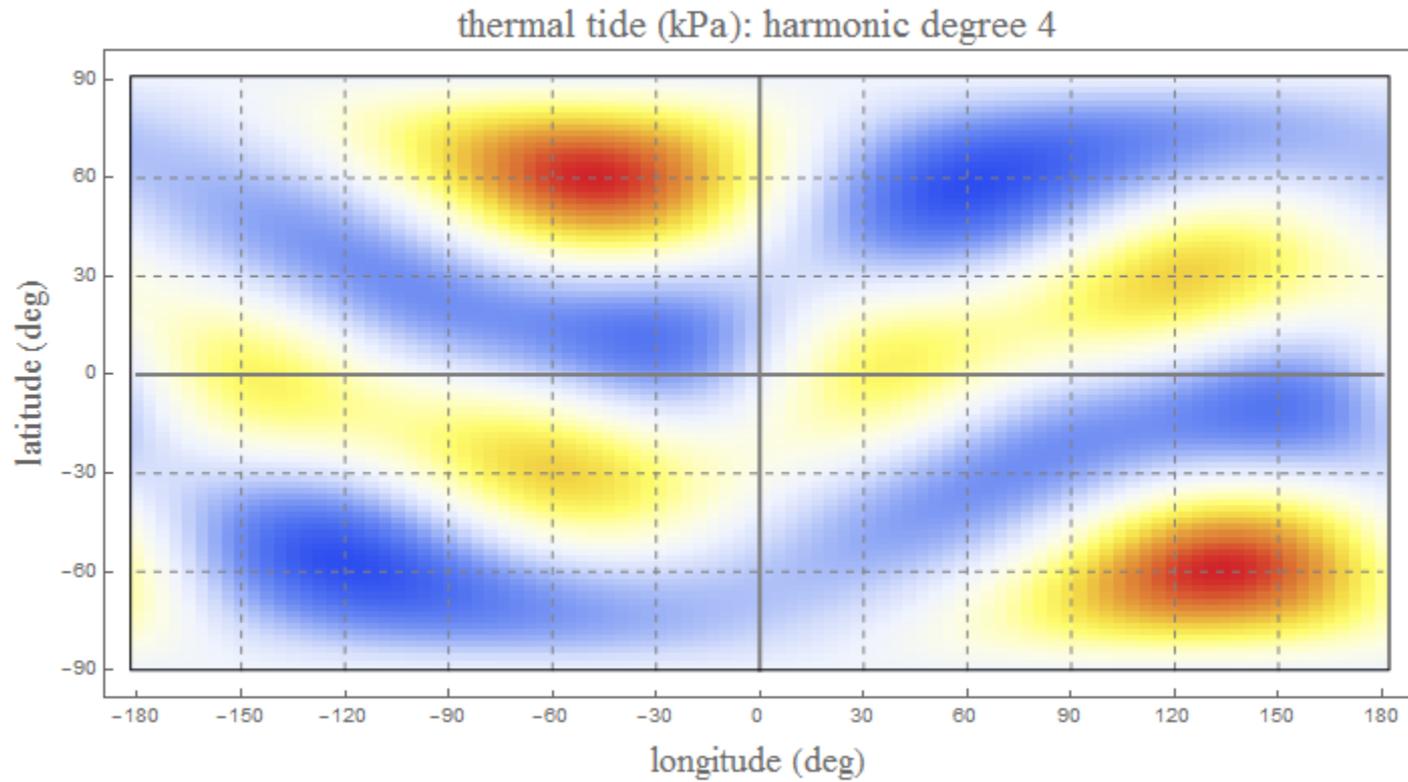
This harmonic decomposition:

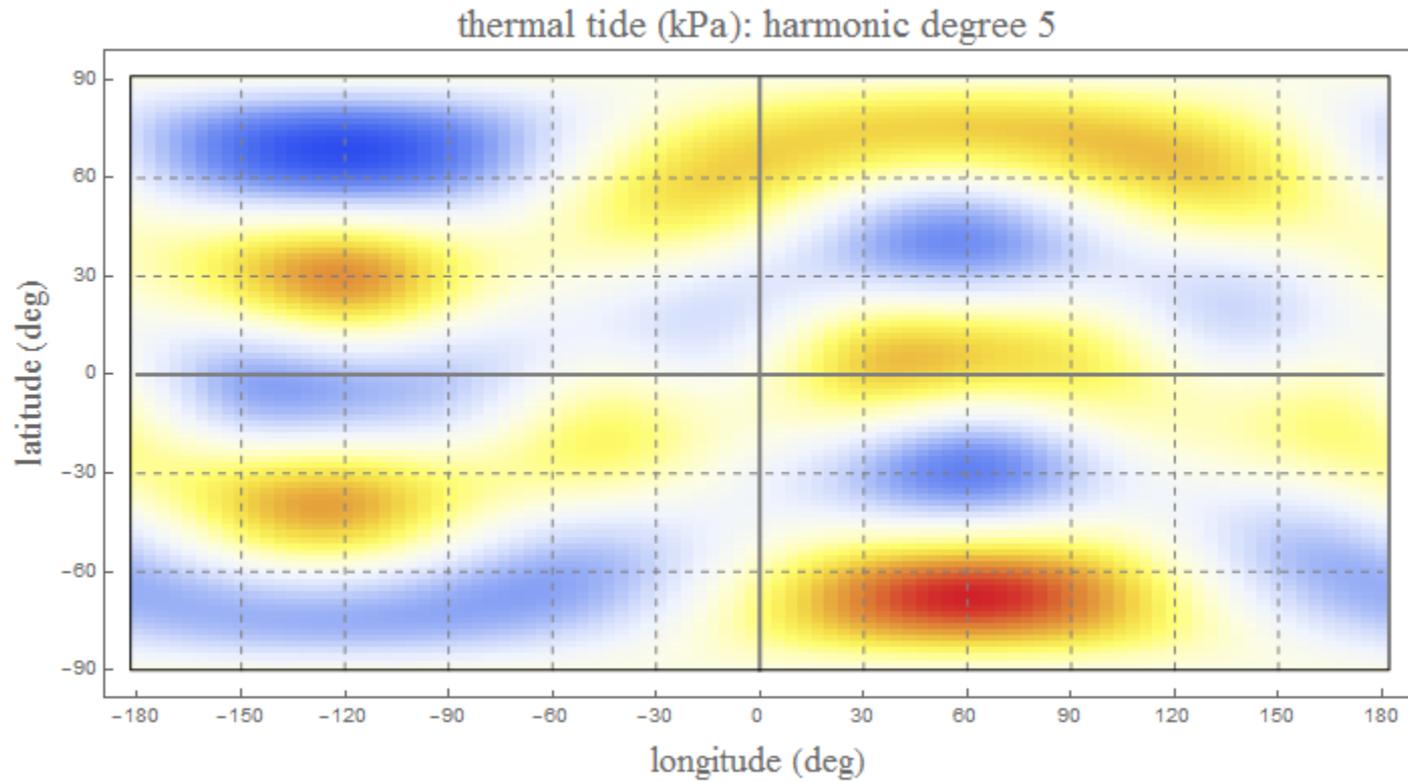
- helps understand the spatial pattern, and
- is a first step in the gravity analysis



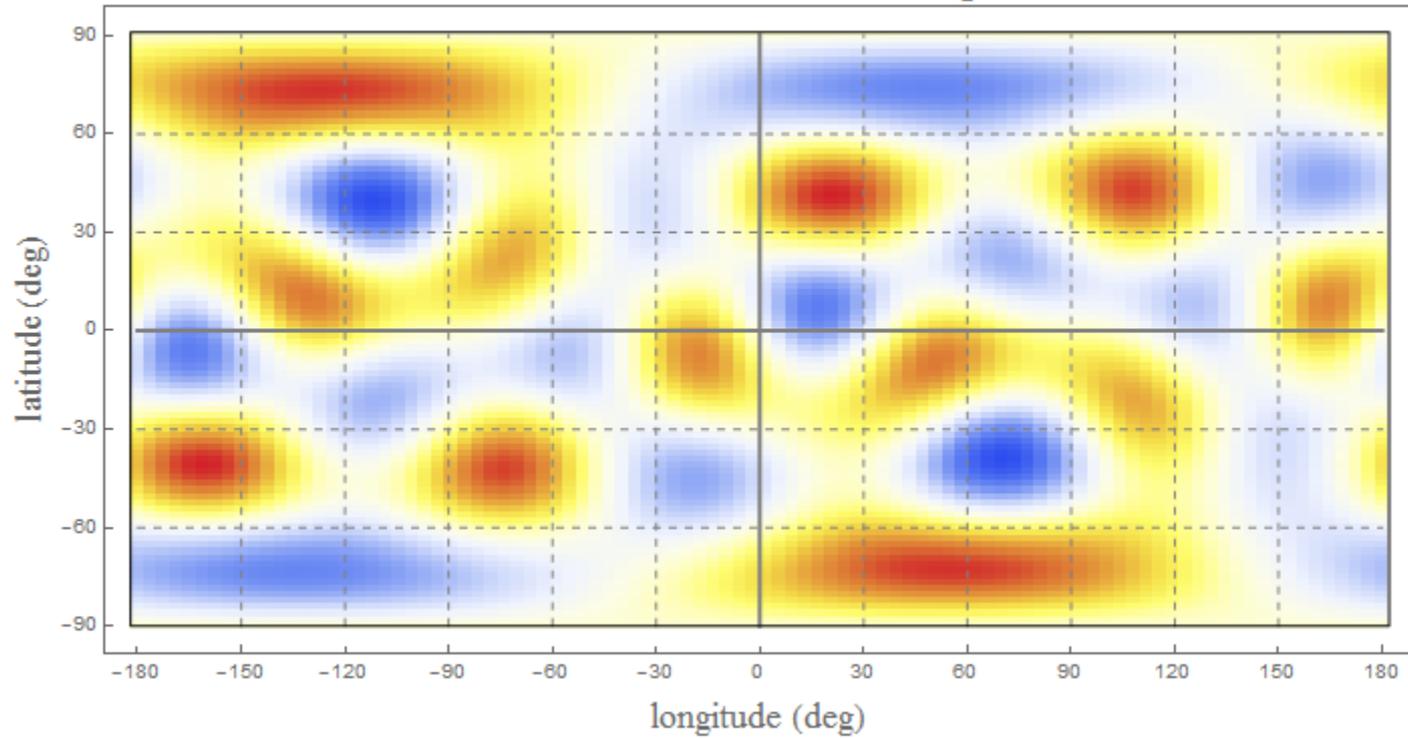




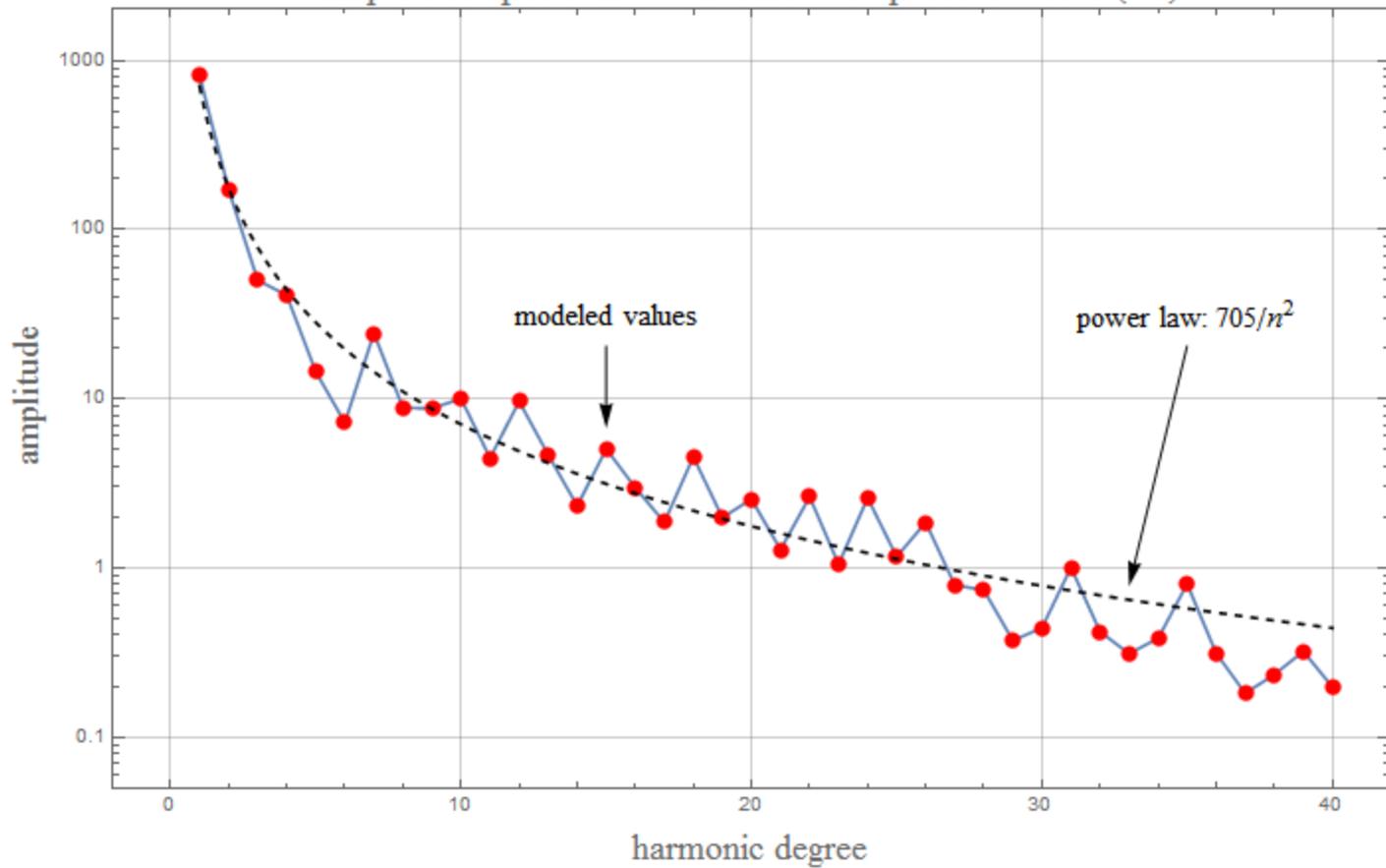




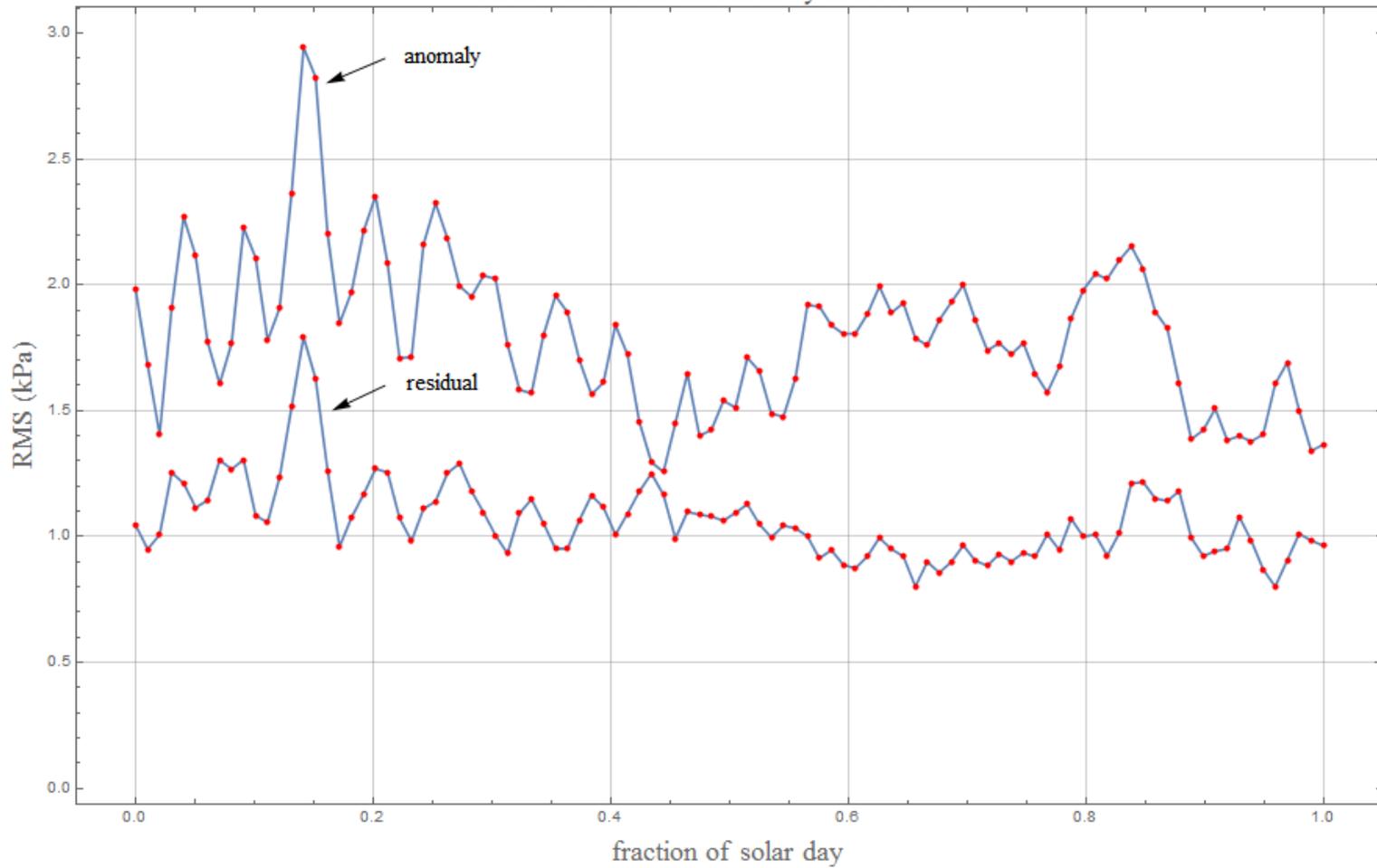
thermal tide (kPa): harmonic degree 6



amplitude spectrum for thermal tide pressure field (Pa)



RMS variations in anomaly and residual



## gravitational signature of thermal tide

- convert pressure to equivalent mass surface density
- expand density in spherical harmonic series
- convert mass density to gravitational potential

The gravitational potential  $\Phi$ , at an external point with spherical coordinates  $(r, \theta, \varphi)$ , can be written as a sum of spherical harmonic functions

$$\Phi[r, \theta, \varphi] = \frac{\mu}{r} \left( 1 + \sum_n \left(\frac{R}{r}\right)^n \sum_{m,k} Y_{n,m,k}[\theta, \varphi] G_{n,m,k} \right)$$

where

$\mu = GM$  is the monopole moment,  
R is the mean planetary radius, and  
 $G_{n,m,k}$  are dimensionless coefficients

In the present case, we first convert surface pressure  $P[\theta, \varphi]$  into an equivalent surface mass density ( $kg/m^2$ ) via

$$\sigma[\theta, \varphi] = \left(\frac{1}{g}\right) P[\theta, \varphi]$$

where  $g = 8.87 \text{ m/s}^2$  is the mean surface gravity.

Then expand the surface density in a harmonic series

$$\sigma[\theta, \varphi] = Z \left( 1 + \sum_{n,m,k} Y_{n,m,k}[\theta, \varphi] S_{n,m,k} \right)$$

where

$Z = \frac{M}{4\pi R^2} = 1.06 \times 10^{10} \text{ kg/m}^2$  is the monopole value

$S_{n,m,k}$  are dimensionless coefficients

In the last step of the conversion,  
the mapping from surface density to potential is

$$G_{n,m,k} = \left( \frac{1}{2n + 1} \right) S_{n,m,k}$$

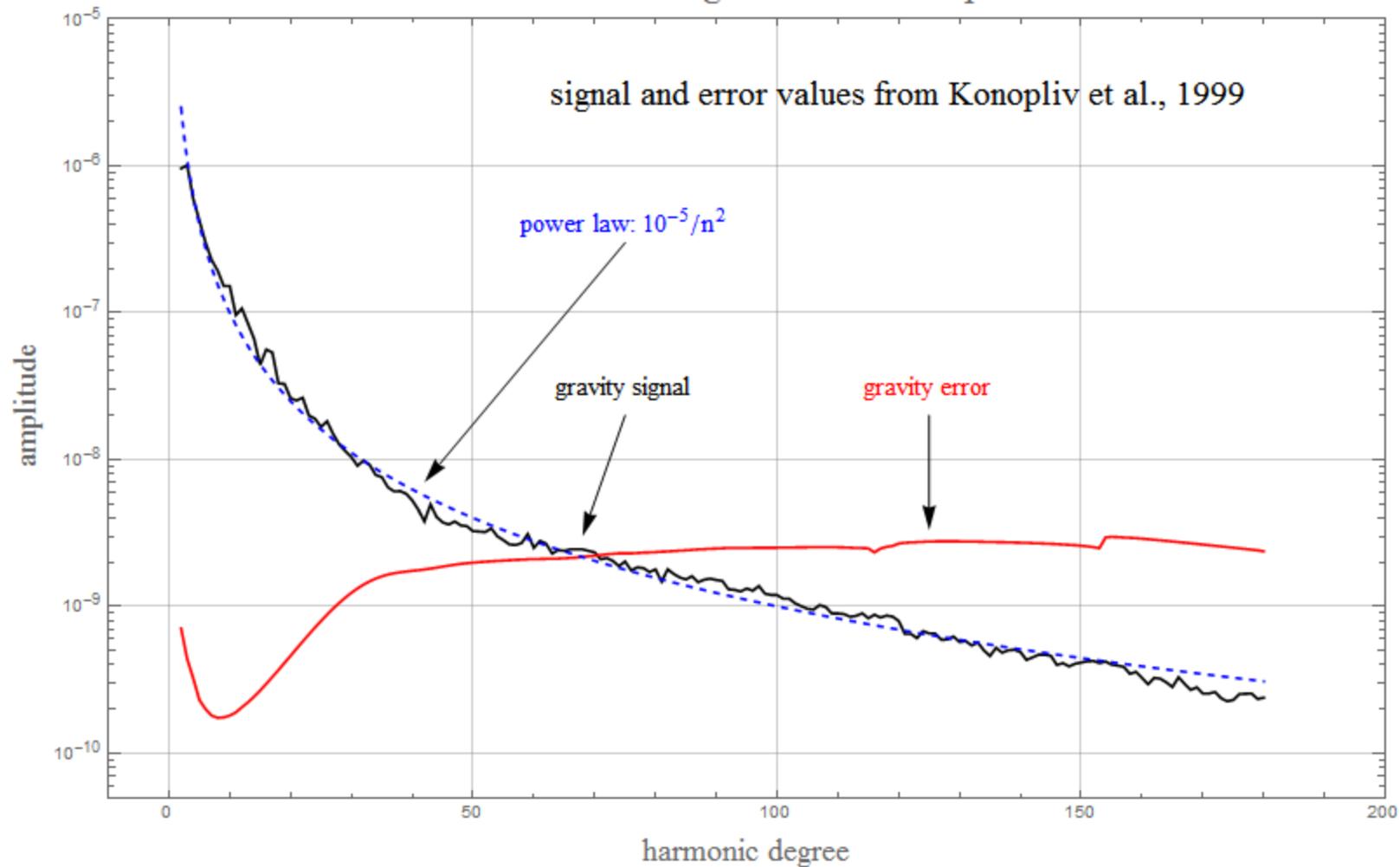
Within each harmonic degree  $\mathbf{n}$ , the spatial patterns of pressure, surface density, and potential are identical.

However, the potential is a smoother function than the pressure, because the higher degree terms are diminished in size.

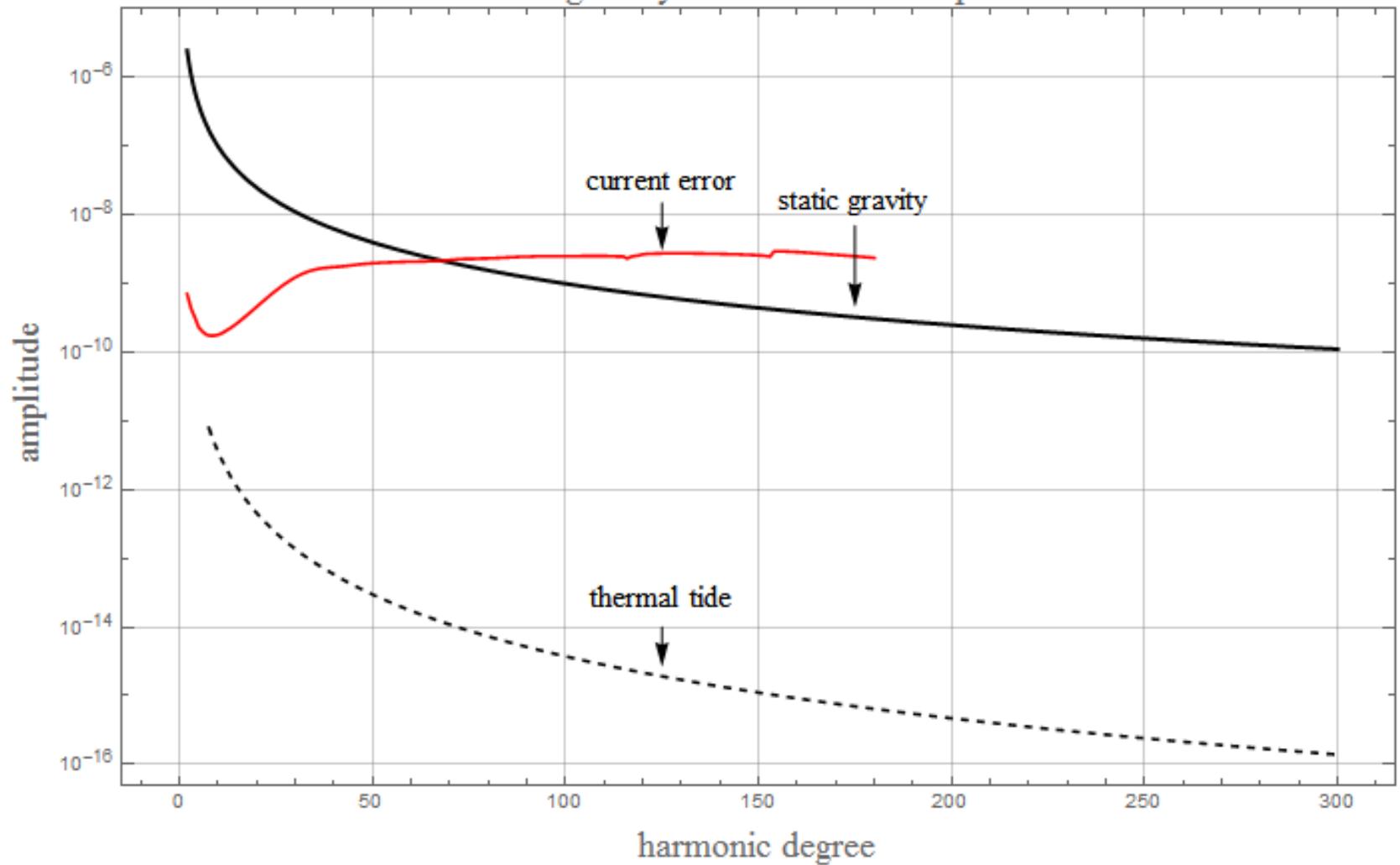
We now compare the spherical harmonic amplitude spectra of

- Venus static potential
  - signal
  - error
- Venus thermal tide

## Venus: current signal and error spectra



### Venus gravity: static and tidal spectra



The modeled amplitude spectrum of the gravitational signature of the Venus thermal tide is small.

It is well below:

- static gravity field signal
- current measurement errors

Is it observable by future missions?

We now examine the accuracy to which gravitational potential can be estimated, from a series of

- $N$  independent measurements,
- each with accuracy  $\varepsilon$ .

In general, we expect the recovered gravity accuracy to scale with

$$\sigma[n] = \frac{\varepsilon}{\sqrt{N}} \left(\frac{r}{R}\right)^n F[\mu, R, r, n]$$

where

- $\mu = GM$  is the monopole moment
- $R$  is the mean radius of the target body
- $r$  is the mean radius of the orbit
- $n$  is the harmonic degree

and  $F[\mu, R, r, n]$  is a function which depends upon mission orbit configuration.

We consider 3 spacecraft orbit configurations for gravity missions.

- The classic case involves Doppler tracking, from Earth, of a single satellite orbiting the target body.
- Another approach, used by GRACE and GRAIL, measures changes in relative speed between a pair of co-orbital satellites
- The third approach uses a gravity gradiometer.

In the first 2 cases, the measurement is a velocity ( $m/s$ ).  
In the third case, it is a gradient of acceleration ( $1/s^2$ ).

The standard unit for gravity gradients is

$$Eotvos = E = 10^{-9} s^{-2}$$

Modern gradiometers have accuracy of

$$\varepsilon_{grad} = \frac{10^{-3} E}{\sqrt{Hz}}$$

Ka-band (32 GHz) Doppler measurements  
have accuracy

$$\varepsilon_{Dop} = \frac{10^{-6} m/s}{\sqrt{Hz}}$$

Based upon a simple covariance analysis, we find

- for single satellite tracking, the configuration function is

$$F_{dop} = \sqrt{\frac{r}{\mu}} \left( \frac{\sqrt{n^2 + n + 1/2}}{n + 1} \right)$$

- for a pair of co-orbital satellites, with angular separation  $\gamma$ , the configuration function is

$$F_{co-orb} = \sqrt{\frac{r}{\mu}} \left( \frac{1}{2 \sin[n\gamma/2]} \right) \left( \frac{\sqrt{n^2 + n + 1/2}}{n + 1} \right)$$

- for a gradiometer, the configuration function is

$$F_{grad} = \left( \frac{r^3}{\mu} \right) \sqrt{\frac{(2 + 2n + n^2)(1 + 2n + 2n^2)}{n^2(5 + 6n + 2n^2)(4 + 12n + 13n^2 + 6n^3 + 2n^4)}}$$

A challenge at Venus, compared to Mars and Earth, is the slow rotation.

It takes more time to obtain complete spatial sampling.

In the present context, we are also attempting to sample, and separate, two different patterns:

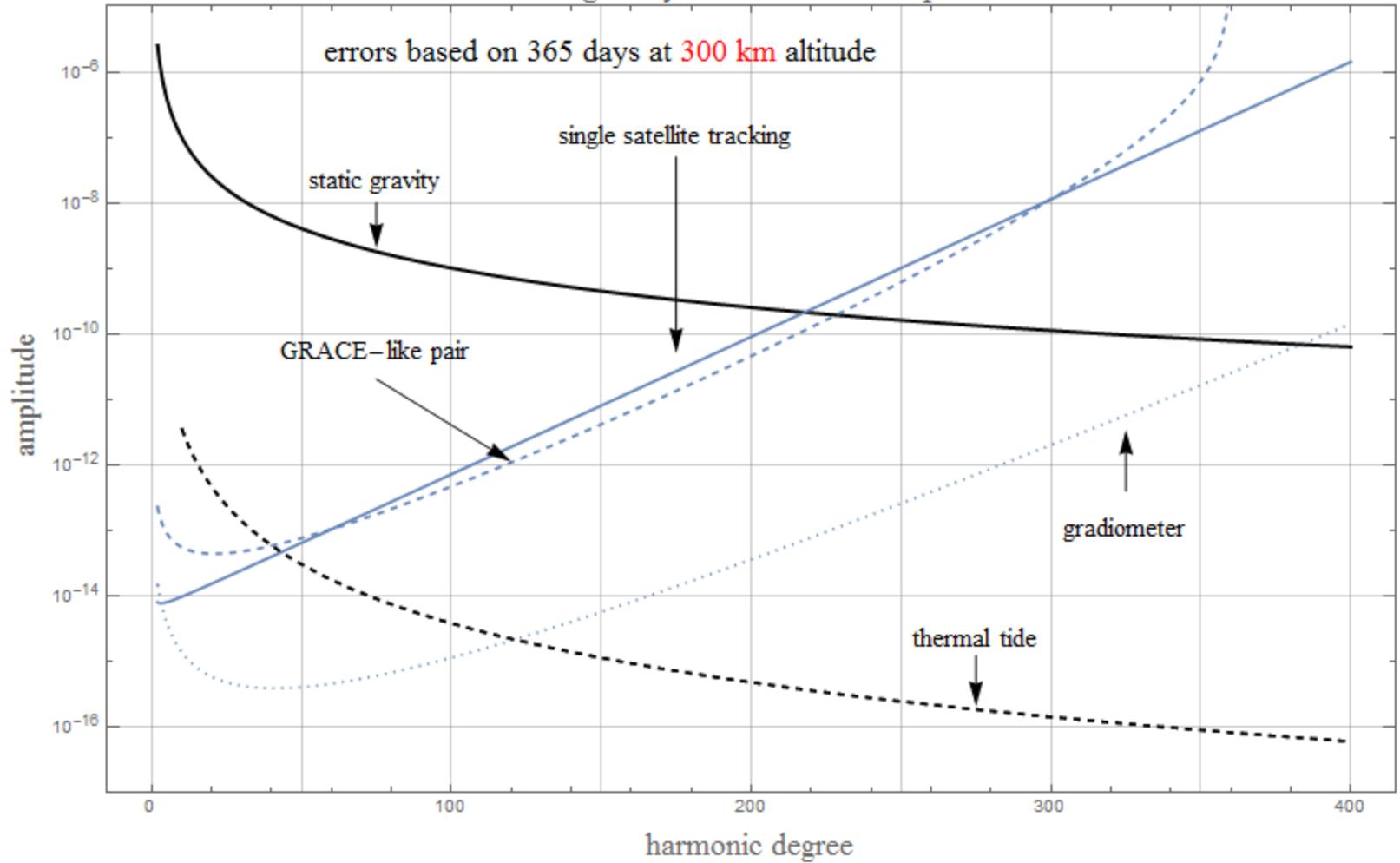
- one fixed to Venus
- another fixed to Sun

The next figure shows

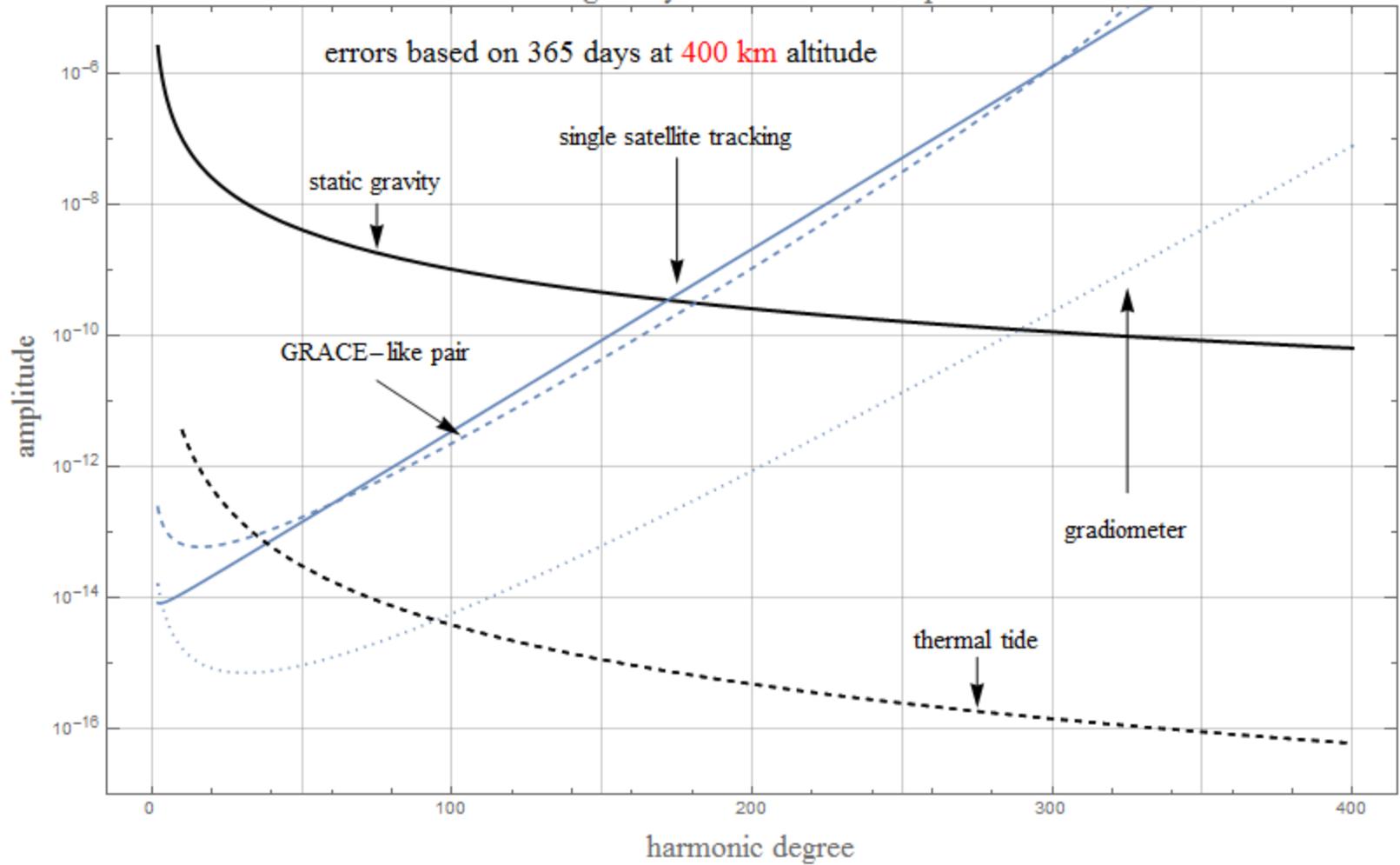
- Venus static gravity signal spectrum
- thermal tide signal spectrum
- error spectra for the 3 measurement configurations

We show results for 2 orbit geometries, with altitudes above the mean surface of 300 and 400 km.

### Venus gravity: static and tidal spectra



### Venus gravity: static and tidal spectra



## summary and conclusions

### Thermal tide on Venus:

- important aspect of atmospheric dynamics
- gravitational signature
  - has not yet been measured
  - can clearly be measured with future missions